

# Temporal and Spatial Coherence of Shallow Water Acoustic Propagation

Harry DeFerrari  
Jennifer Whyllie

University\_of Miami  
[hdeferrari@rsmas.miami.edu](mailto:hdeferrari@rsmas.miami.edu)

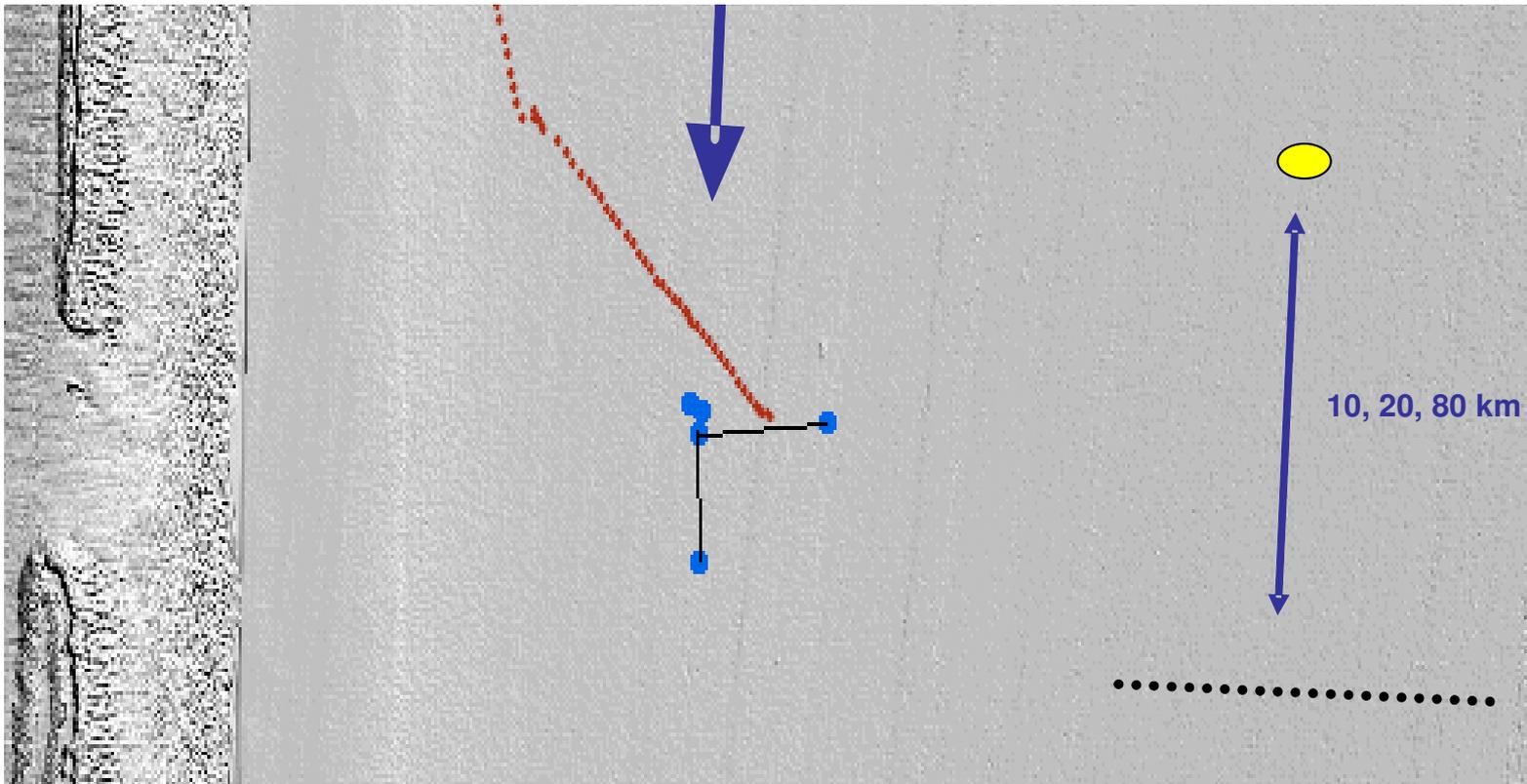
# Data Sets

(M-sequence  $q=4$ )

- **SW06**
  - Continuous transmission to SHRU receivers. 50 hours  
→ temporal properties – fluctuations, coherence in time
  - Periodic transmission to SHARK VLA and HLA  
→ spatial properties
- **FSPE** - Florida Straits Propagation Experiment
  - Continuous Transmission 2 -30 day periods.  
→ temporal properties
- **AO** - Acoustic Observatory
  - Short 20 min Transmission 500 element - HLA  
→ spatial properties 20 to 80 km.

# Acoustic Observatory CALOPS Sept 07

## Shipboard Suspended and Towed Transmissions



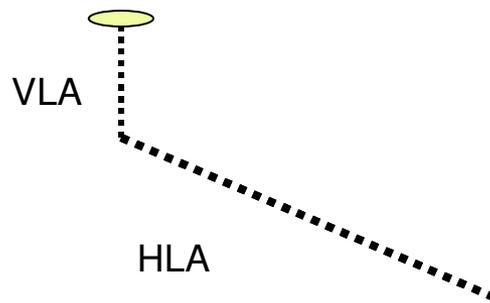
# SW06 Experiments – Mid-Atlantic Bight

MSM



19.7 km Range

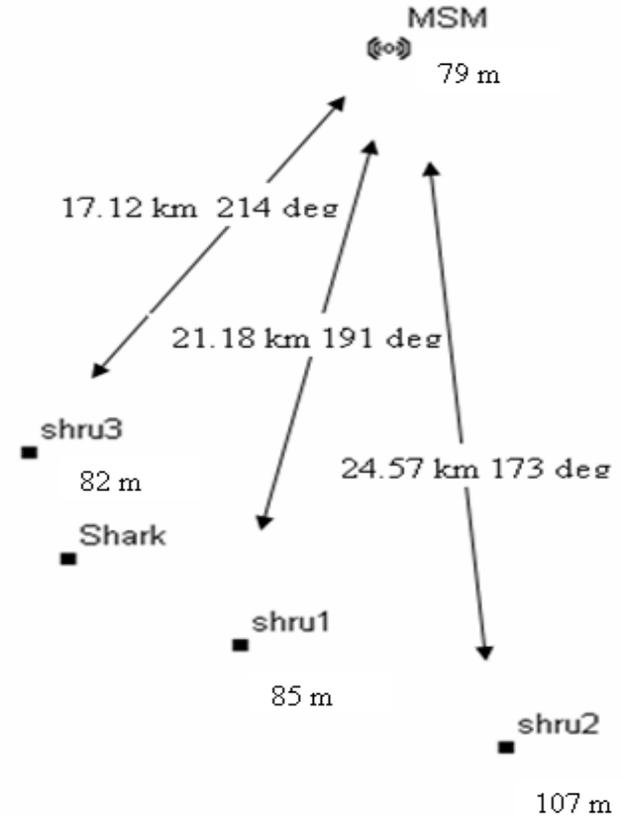
85 m Depth



SHARK

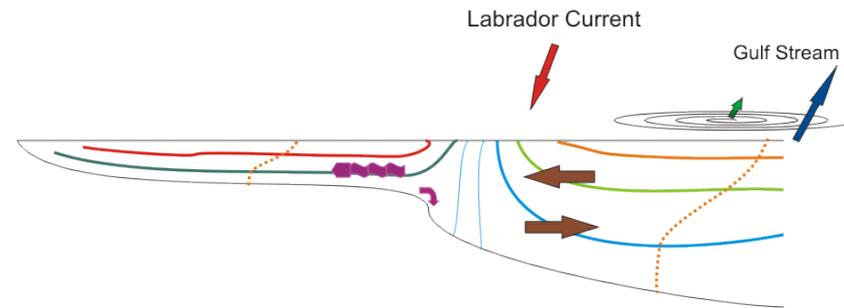
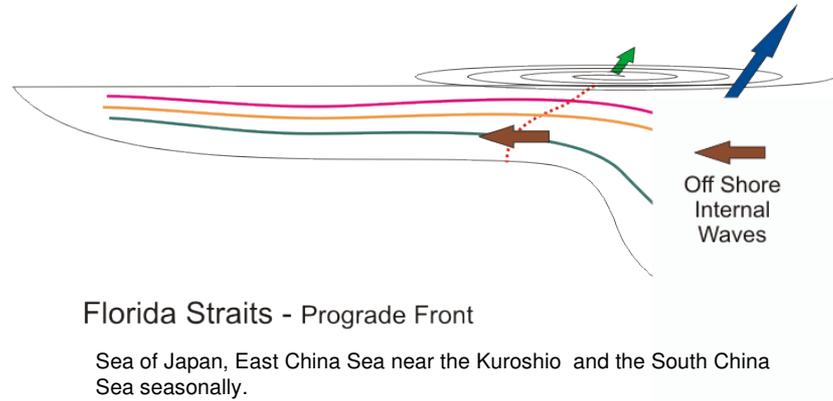
VLA 16 phones

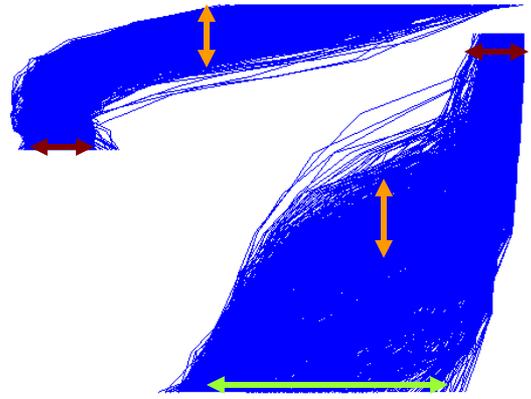
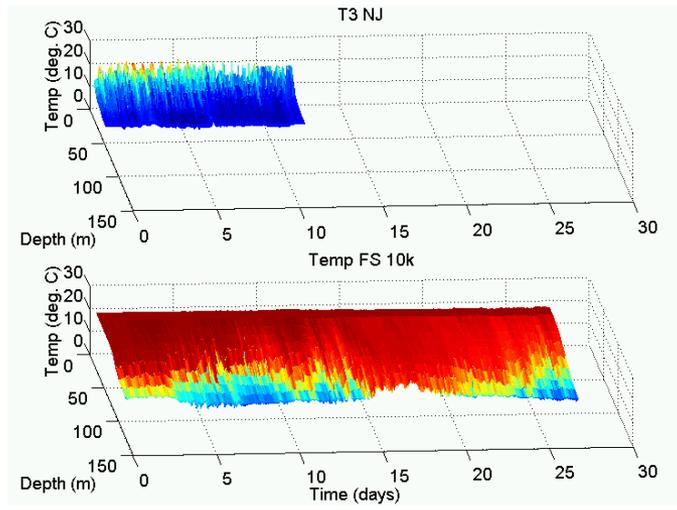
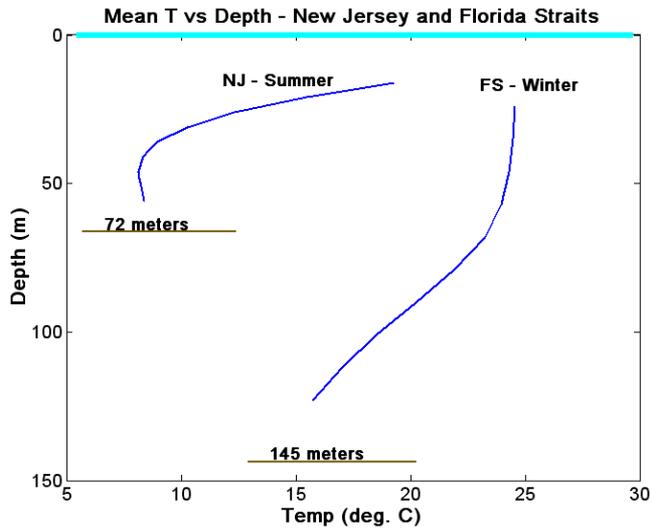
HLA 32 phones 468 m (15 m spacing)



# Acoustic propagation shallow shelves inside of western boundary currents

## Prograde vs Retrograde fronts

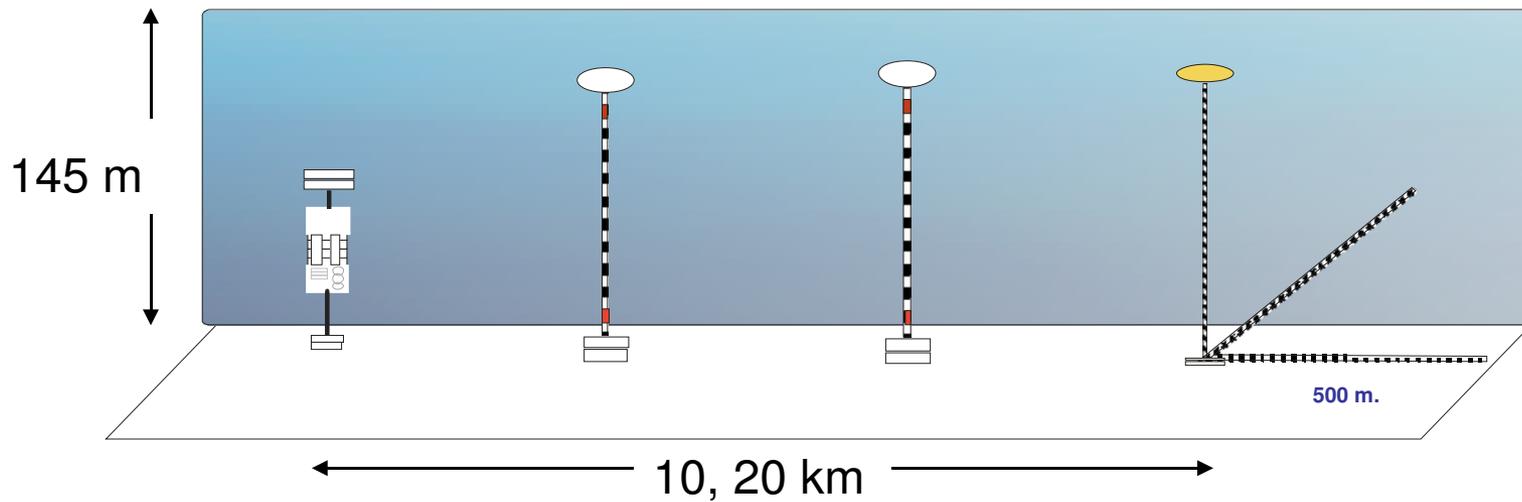
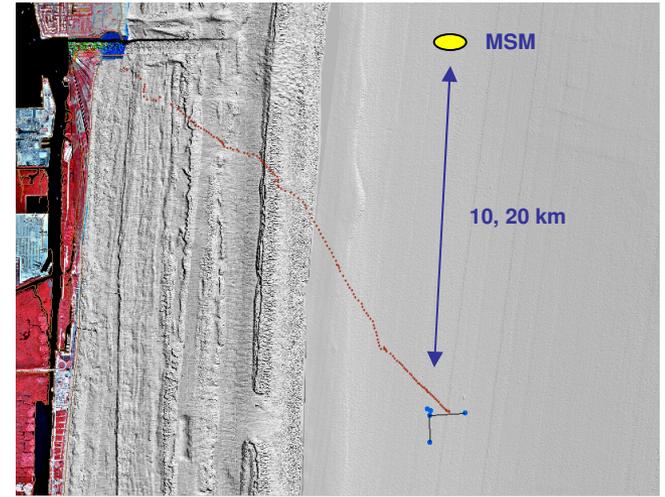
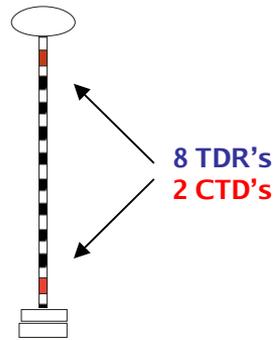
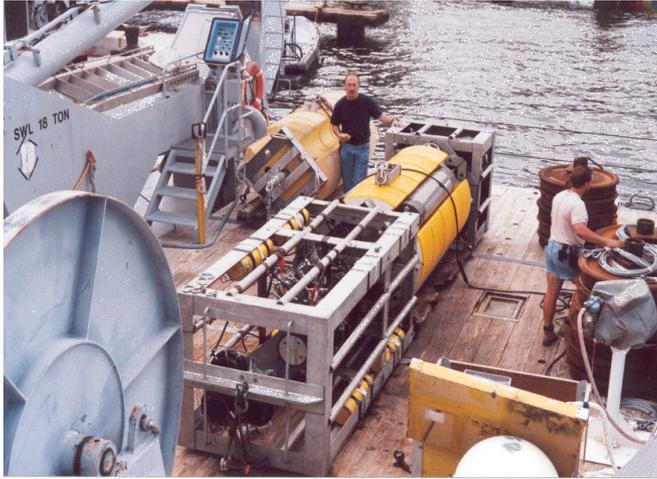




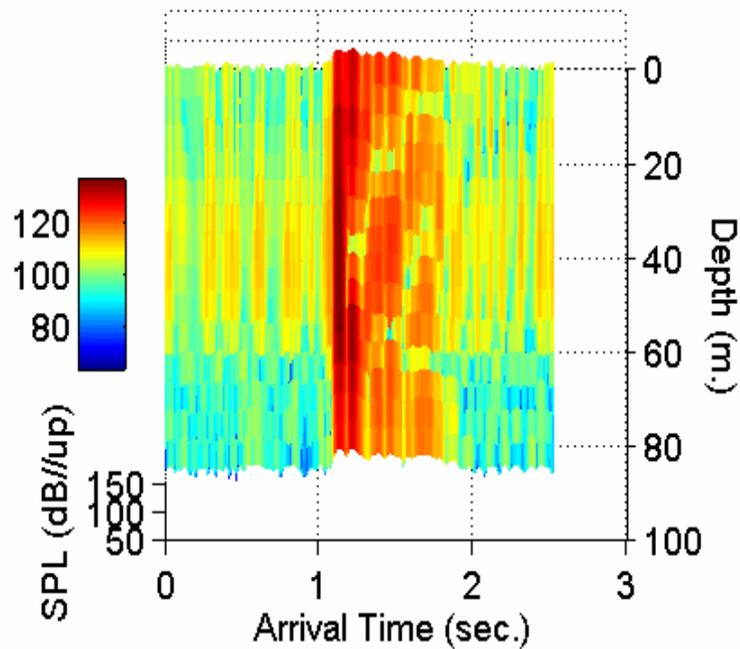
# Miami Sound Machine

$F_c = 100, 200, 400, 800, 1600, 3200$ . Hz.

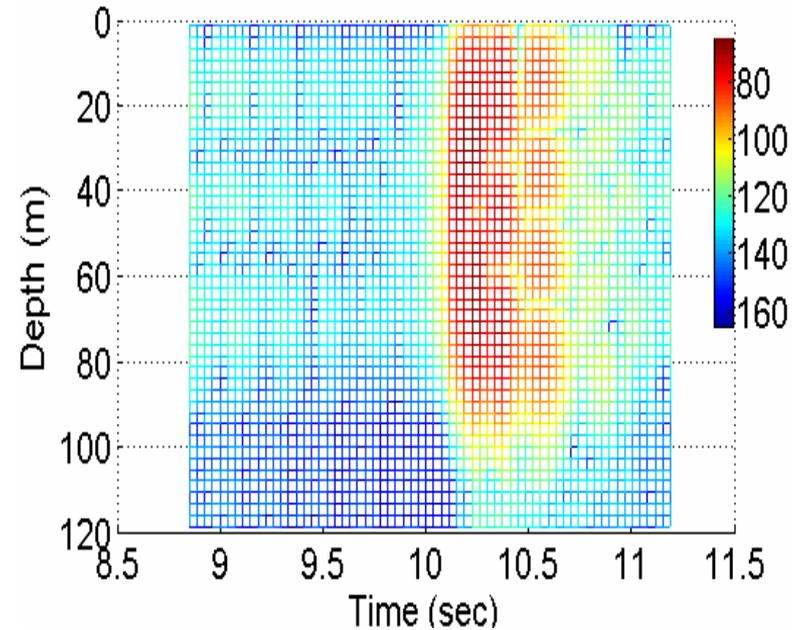
$B_w = 25, 50, 100, 200, 400, 800$ .



Shark VLA 100 Hz. m-sequence



Transmission Loss (dB re 1m)



PE Model (first try)

→

Several extra modes

$C_b = 1715$  m/s Inversion

by K. Smith and J. Miller

(In the vicinity)

PE (second try)

→

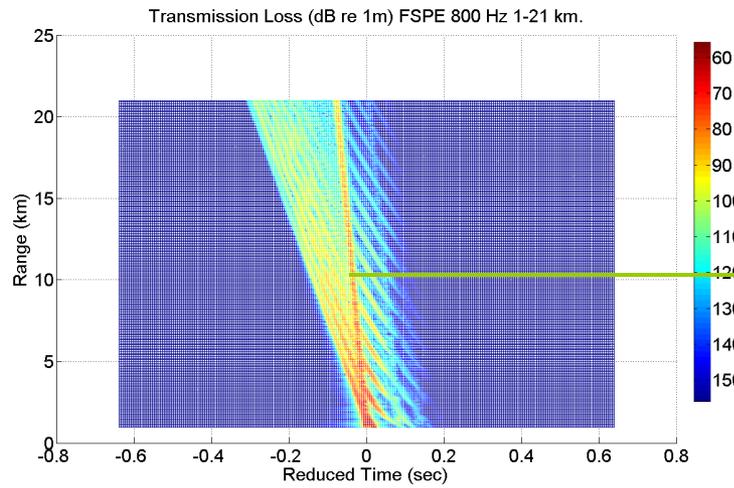
Good Fit ! Above)

1595 m/s

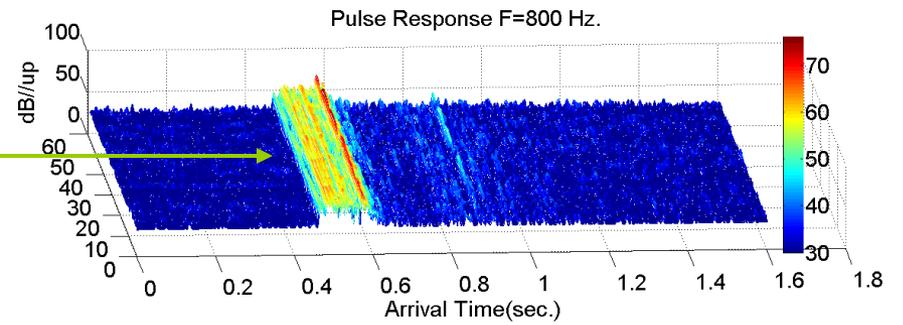
Measurements by UW (direct method) sediment pool at site of experiment

1600 m/s !

## PE Prediction of 800 Hz. Pulse Response



## Measured - 1 Hour





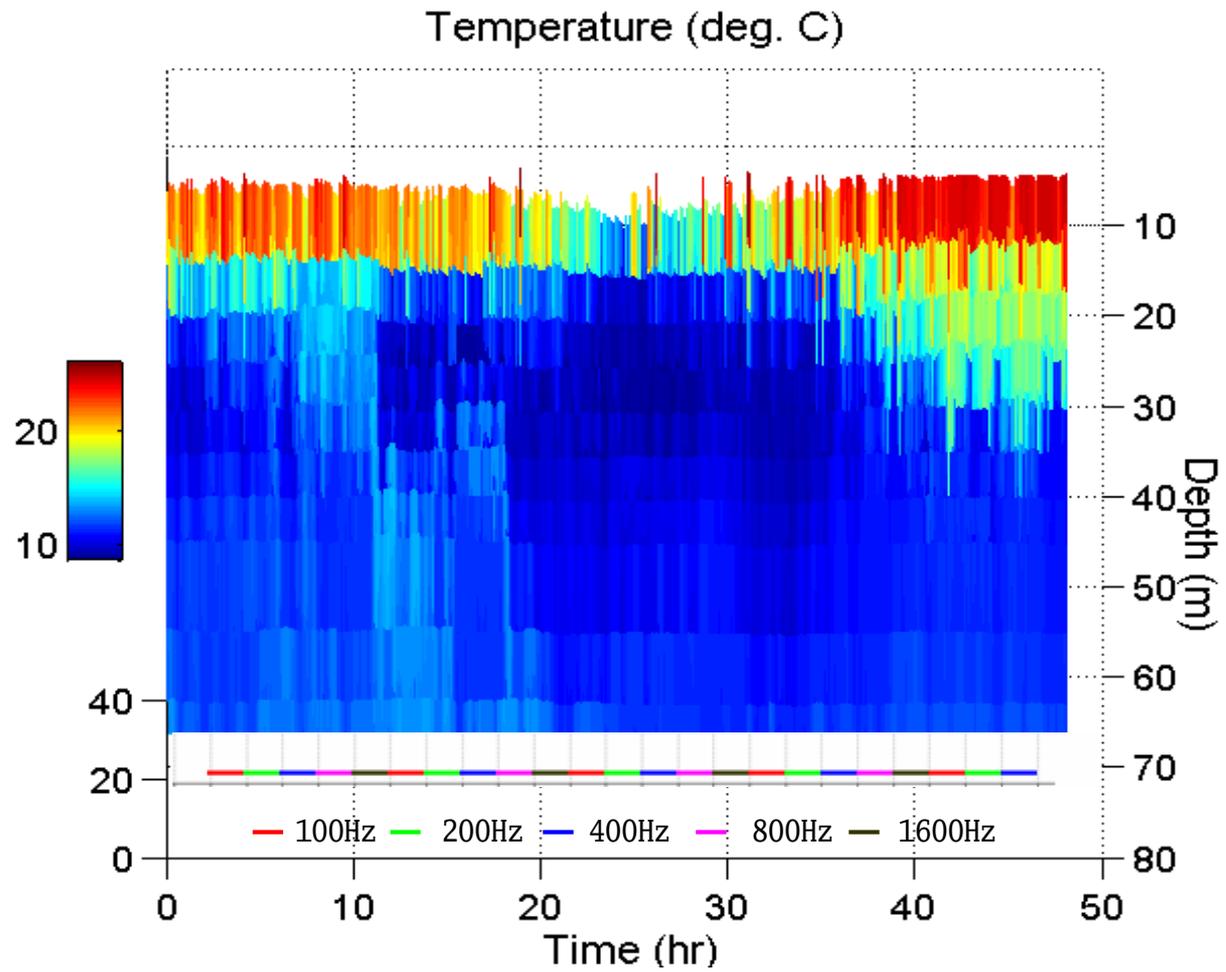
# Temporal Coherence and Phase Wrapping

$$COH(t, \tau) = \frac{\langle (p(t) * p(t + \tau))^2 \rangle_{\Delta t, \Delta T}}{\langle p(t)^2 \rangle_{\Delta t, \Delta T} \langle p(t + \tau)^2 \rangle_{\Delta t, \Delta T}}$$

Coherence is a statistical measure of the change of a waveform with time

## Causes:

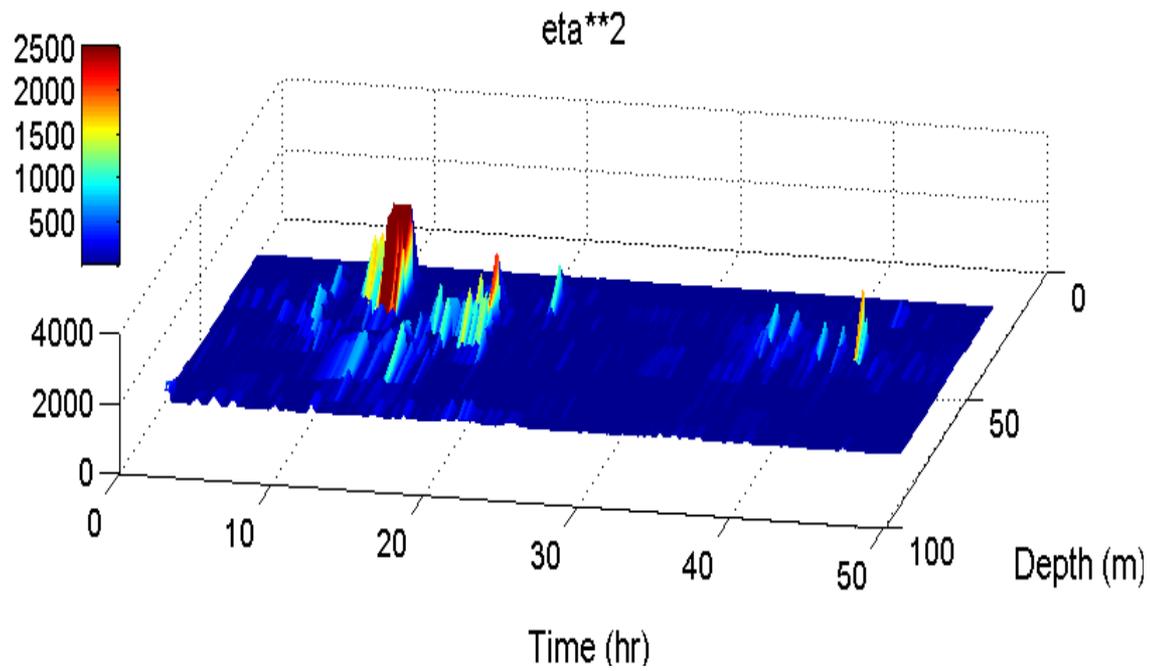
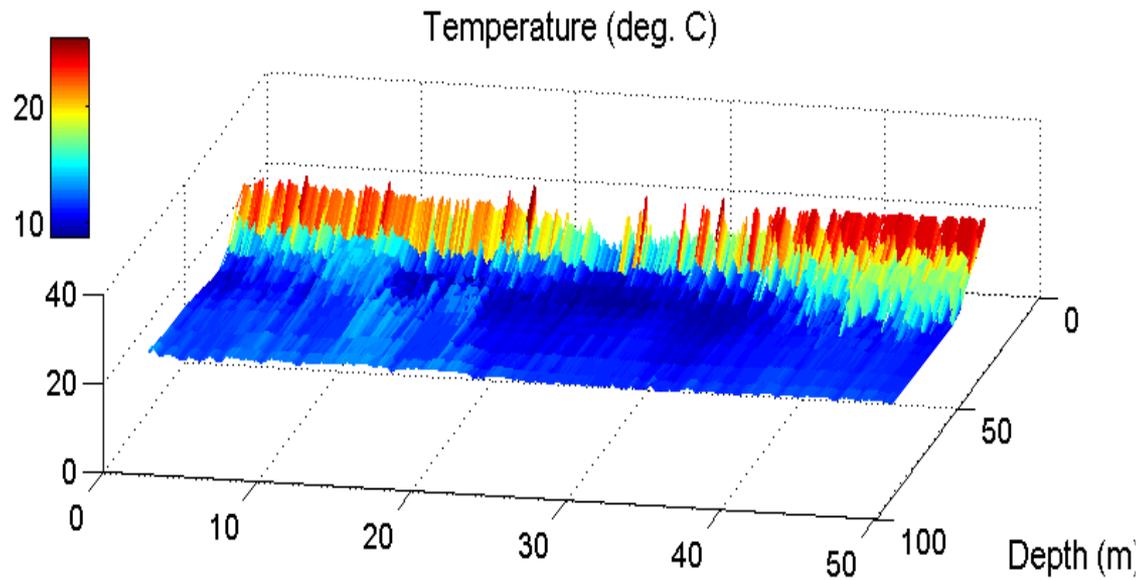
2. Multimode interference
    - Separate modes
  3. Slow phase shifts of undistorted waveform
    - Compute for all phase shifts or phase track.
  4. Random waveform distortion
    - Unrecoverable
- COH varies from both slow phase shifts in time that cause multipath/mode cancellation and from true randomizing effects.
  - Both usually happen at the same time (Phase wrapping, Flatte)



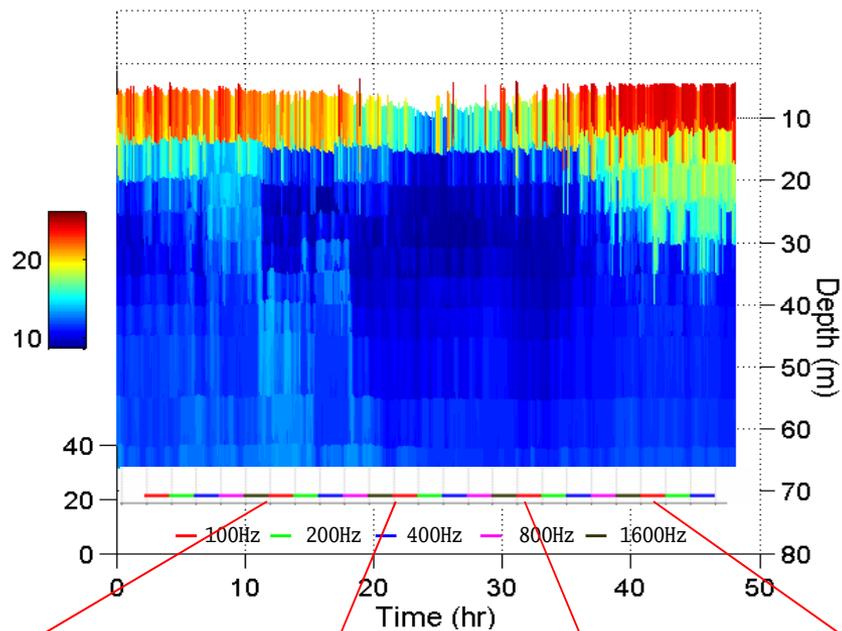
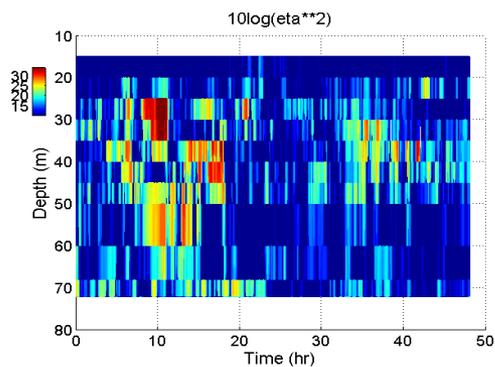
$$PE = (\rho/2)\eta^2 N^2,$$

Where, N is the buoyancy frequency,

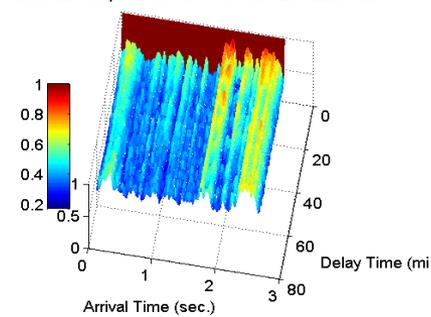
$$\text{and } \eta = T' / dT / dz.$$



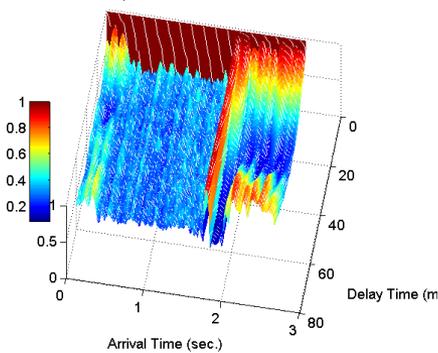
# Temperature (deg. C)



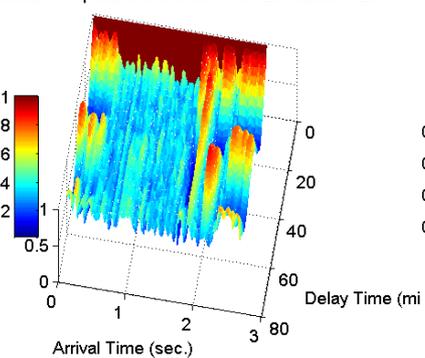
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



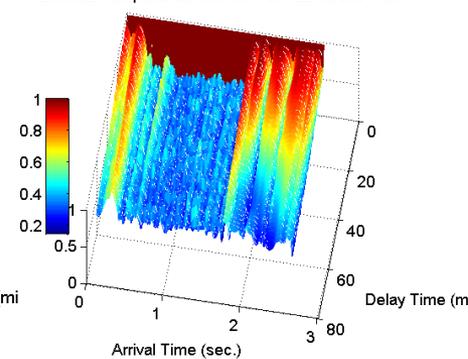
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



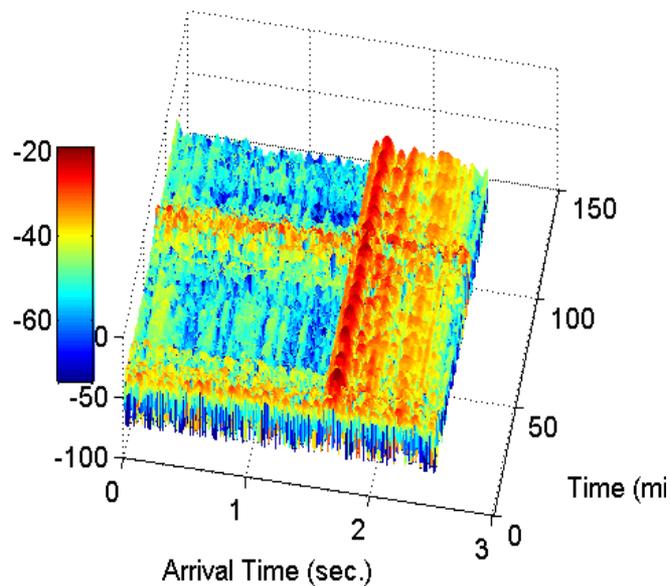
shru2252 Temporal Coherence 100 Hz.Hr 2200 7/29



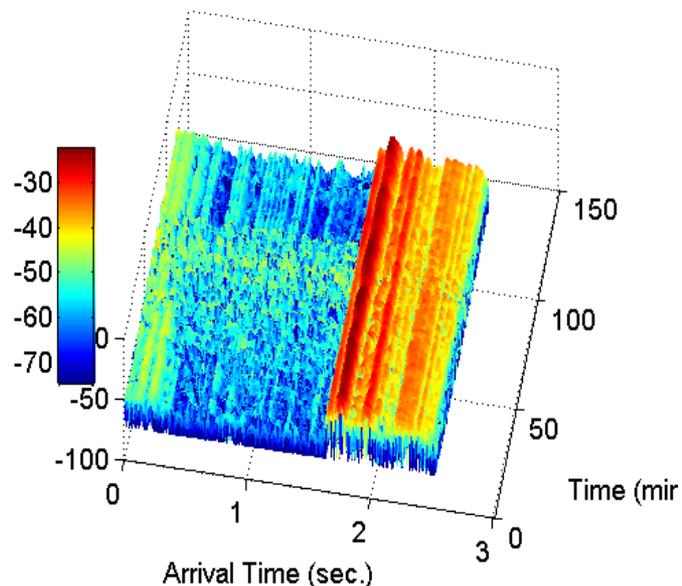
shru852 Temporal Coherence 100 Hz.Hr0800 7/30



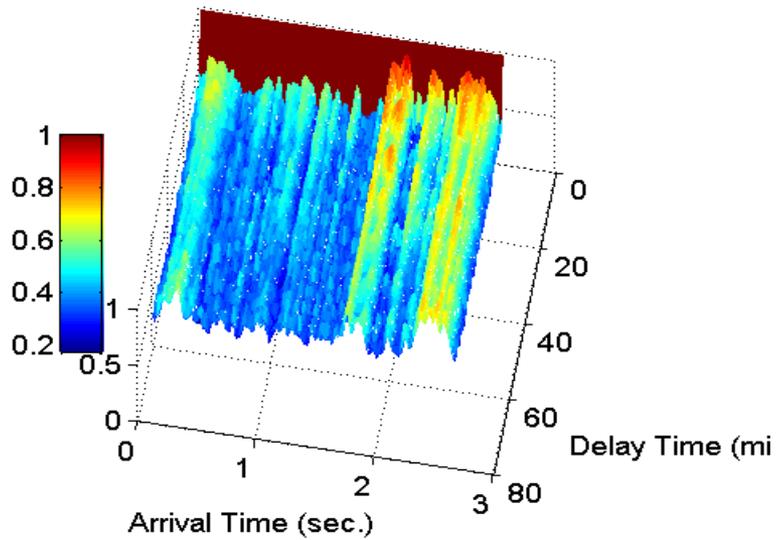
shru852 Pulse Response 100 Hz. Hr 200 7/29



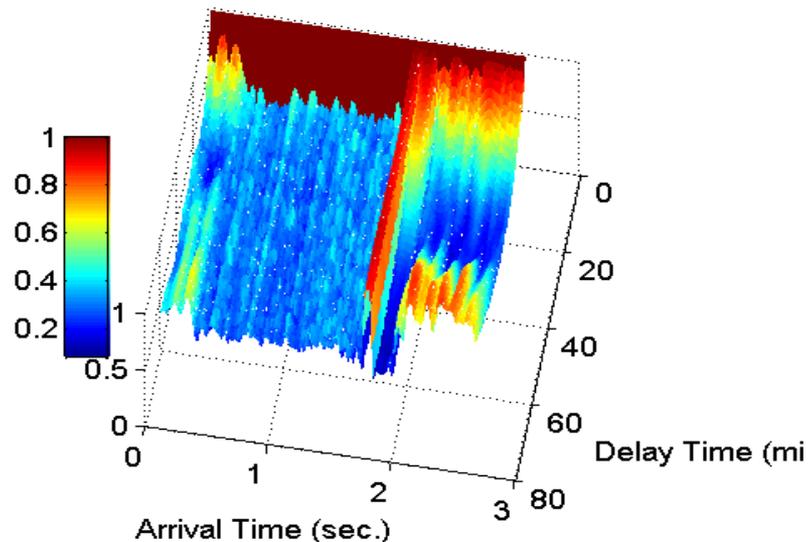
shru852 Pulse Response 100 Hz. Hr 1200 7/29



shru852 Temporal Coherence 100 Hz.Hr0200 7/29



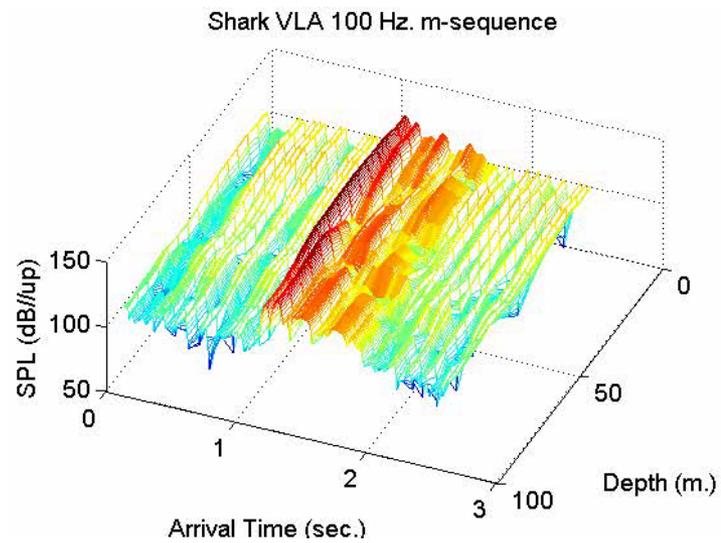
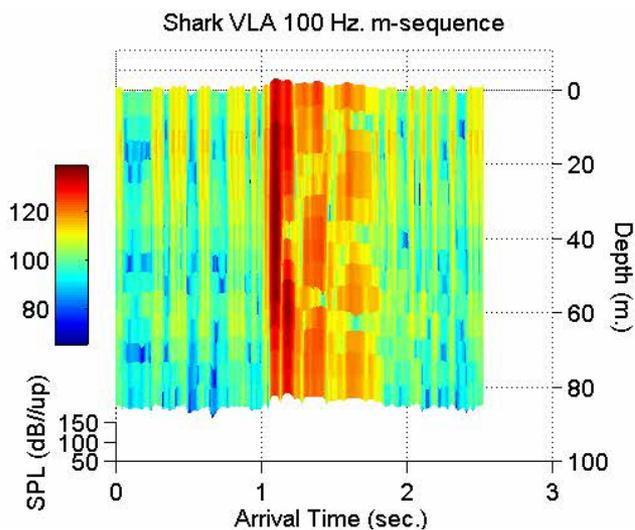
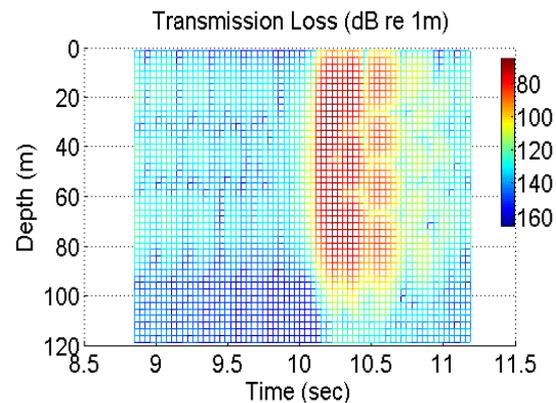
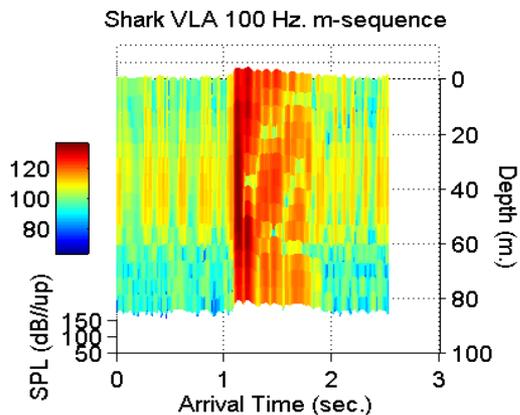
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



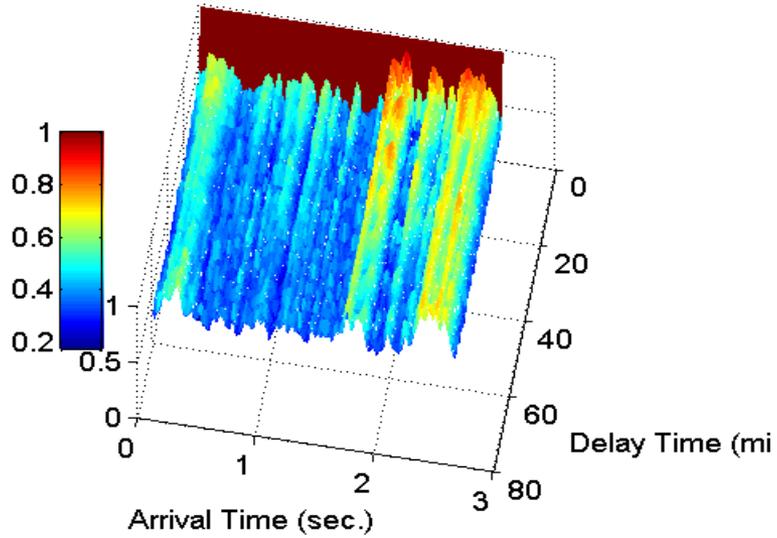
# SW06 Modes and Arrivals

Observed

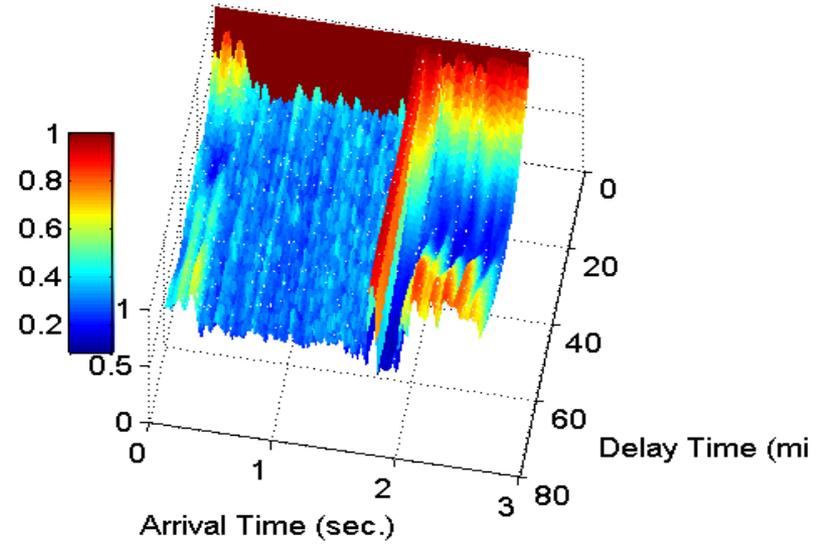
Modeled



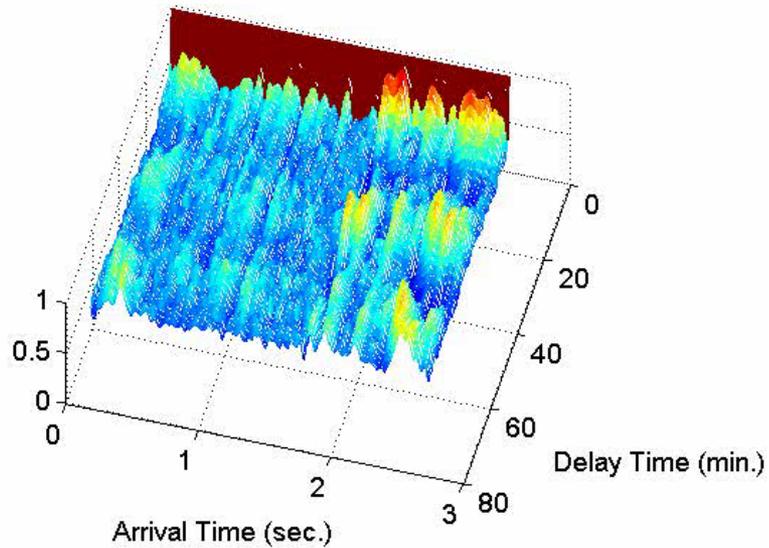
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



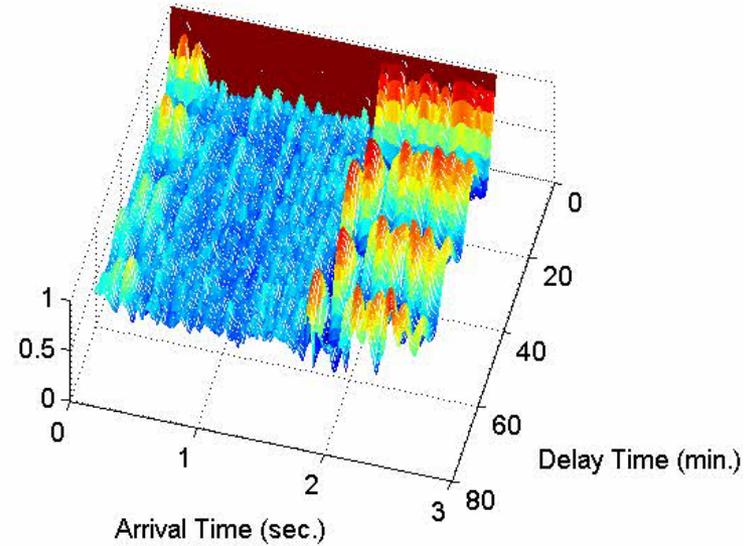
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29

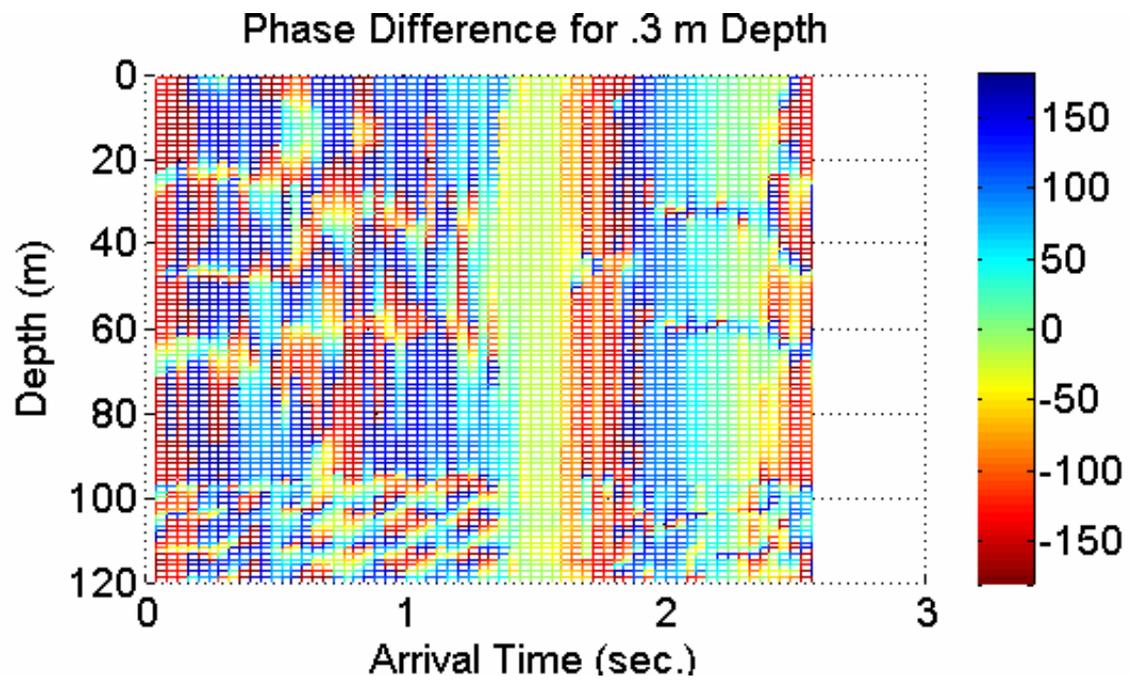


shru252 Temporal Coherence 100 Hz.

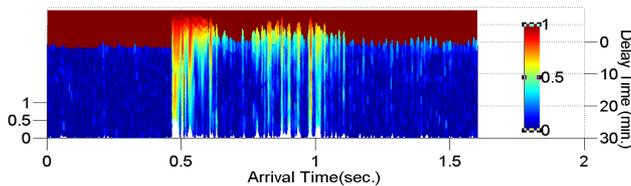
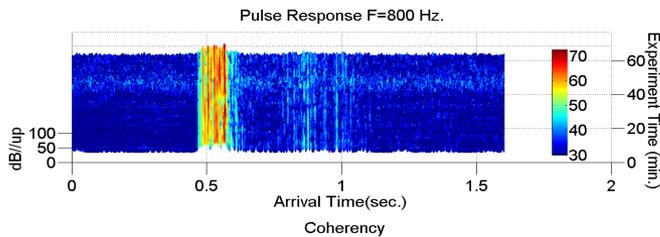
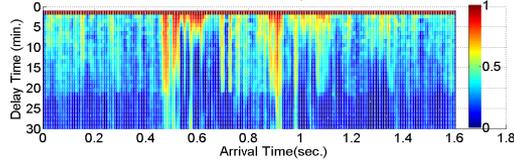
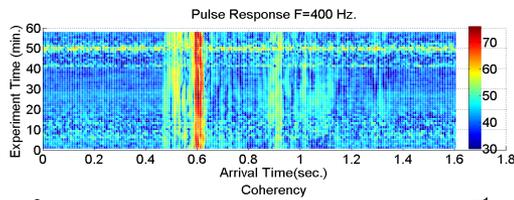
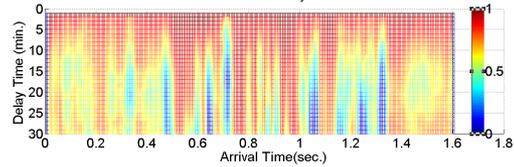
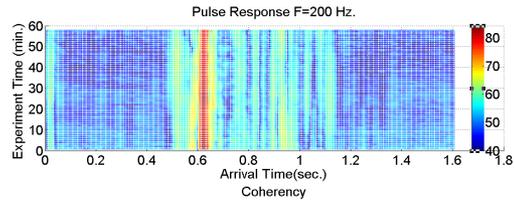


shru853 Temporal Coherence 100 Hz.

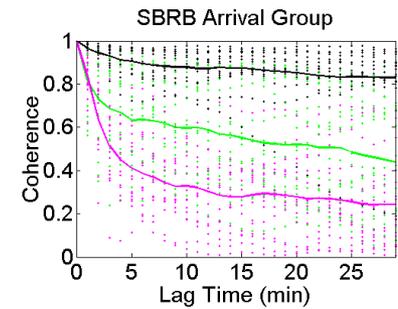
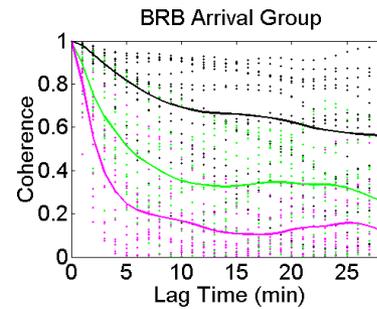




# Temporal Coherence



# Temporal Coherence

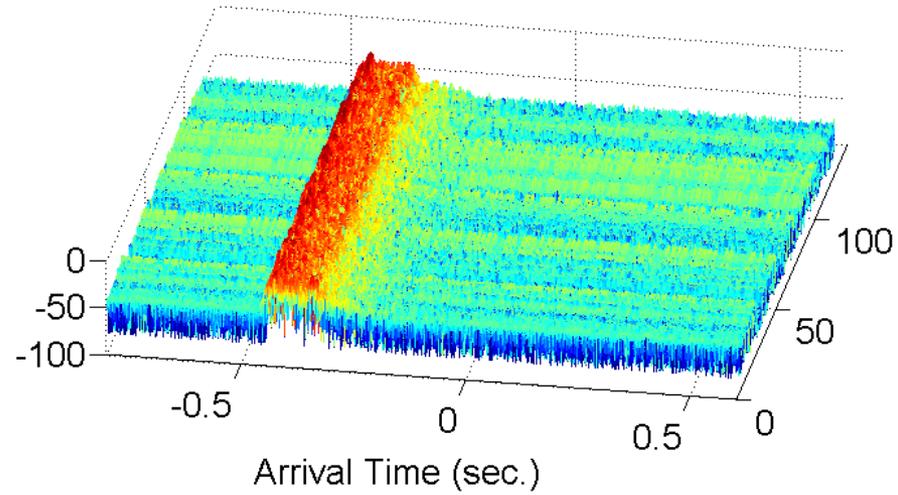


## Coherence time (.75 level)

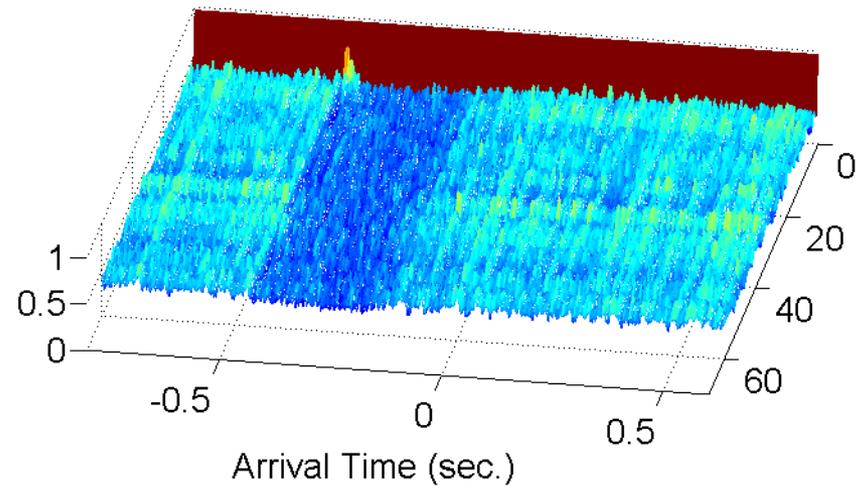
	BRB Group		SBRB arrival	
800Hz.	mean → 2.1	max → 6.5 minutes	800Hz. mean → 2.8	max → 6.5 minutes
400Hz.	3.4	12.0	400Hz. 4.2	>30
200	8.3	> 30	200	15.0 >> 30

# 800 Hz.

shru3 sw53 Pulse Response 800 Hz.



shru3 sw53 Temporal Coherence 800 Hz.



# Temporal Coherence

Low Frequency  $< 100$  Hz.

Bottom appears smooth.

No mode distortion from scattering

IW caused mode coupling is evident.

Mid – Frequencies  $100 >, < 800$  Hz.

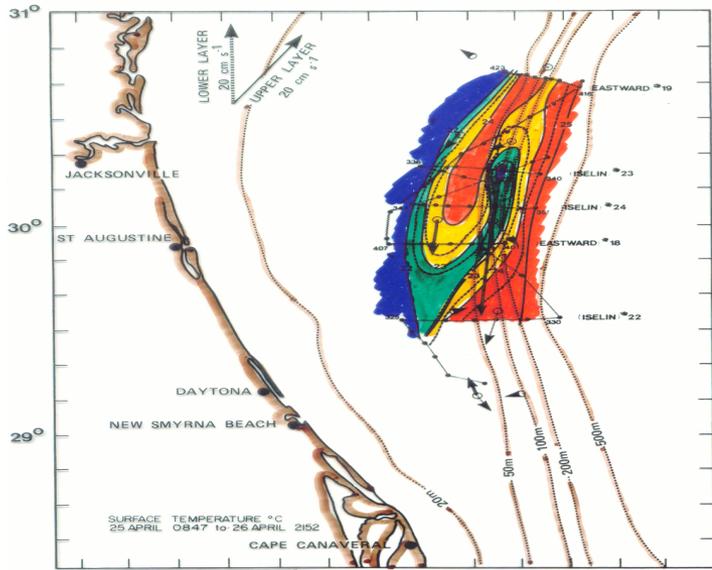
Bottom scattering become important.

Coherence times decrease with frequency

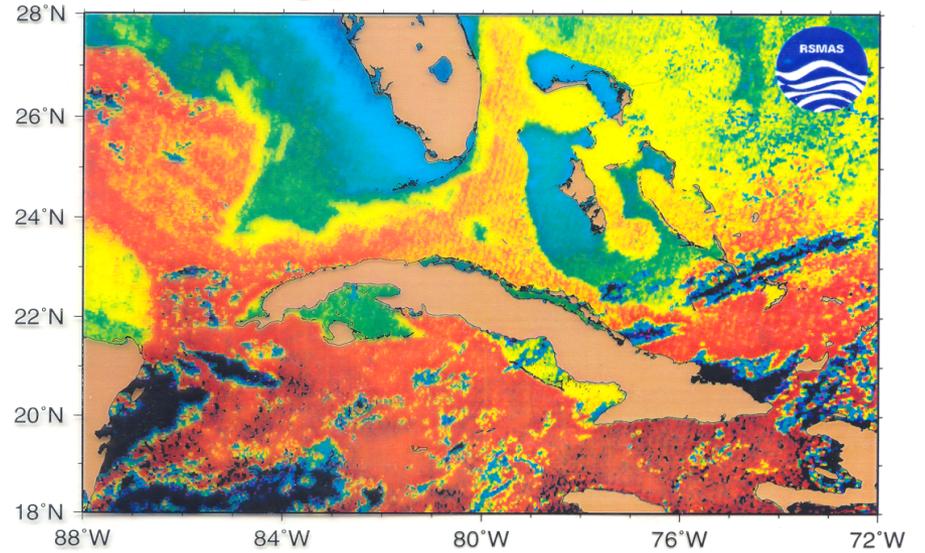
Coherence times decrease with increasing mode number

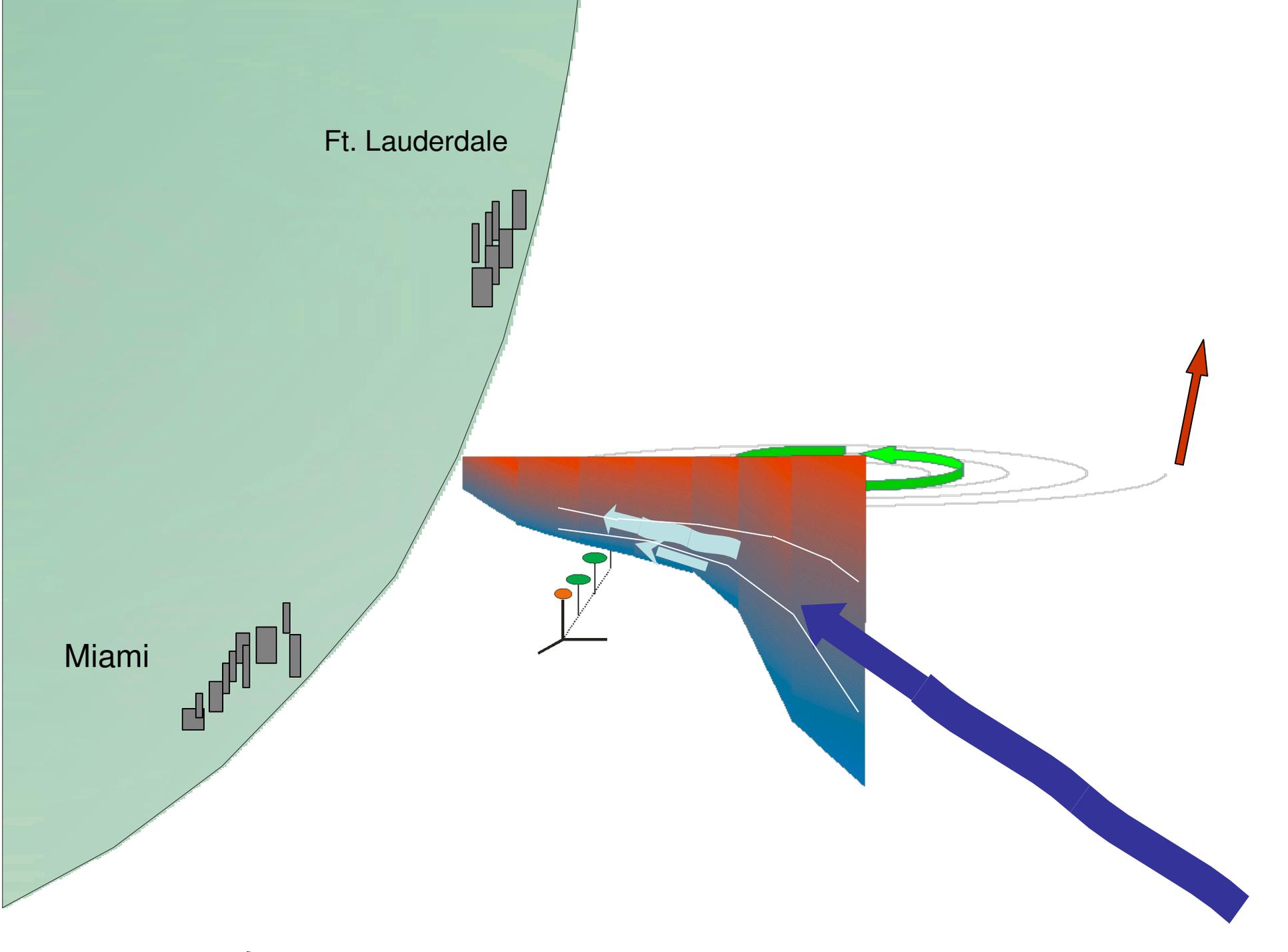
High frequency  $> 1000$  Hz.

Signals are randomized by bottom scattering



NOAA 14 AVHRR - 3 Feb 1995

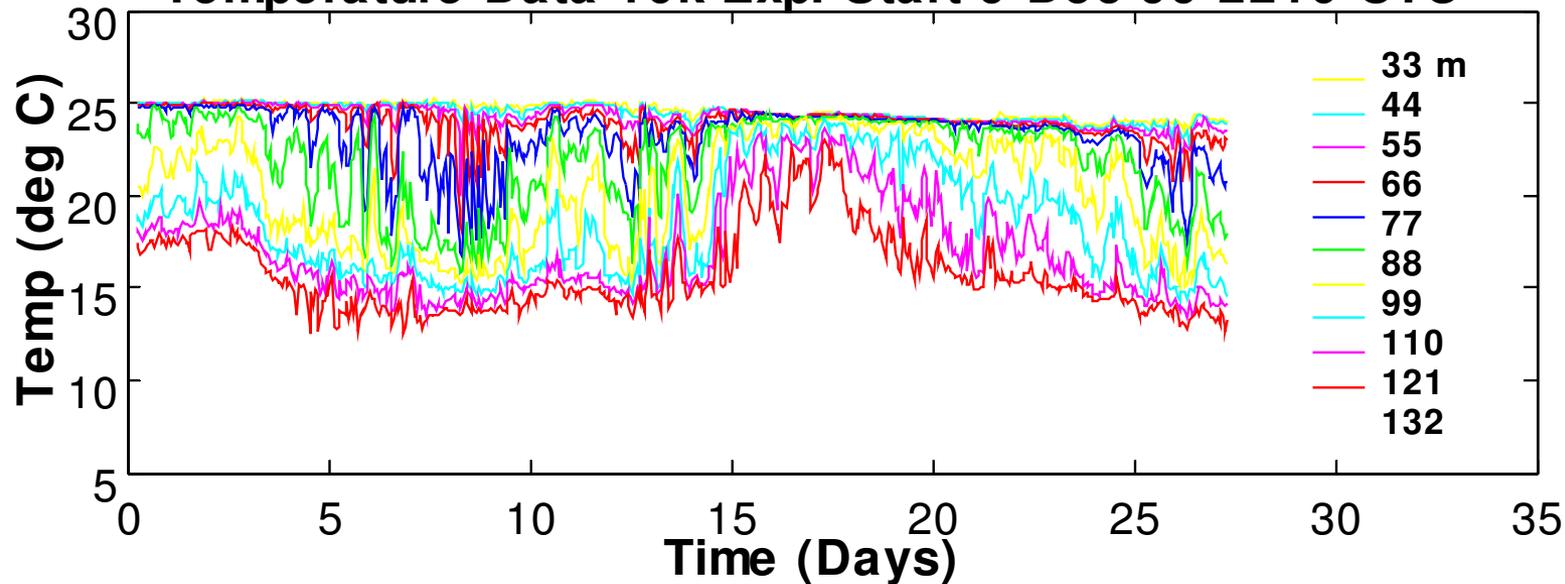




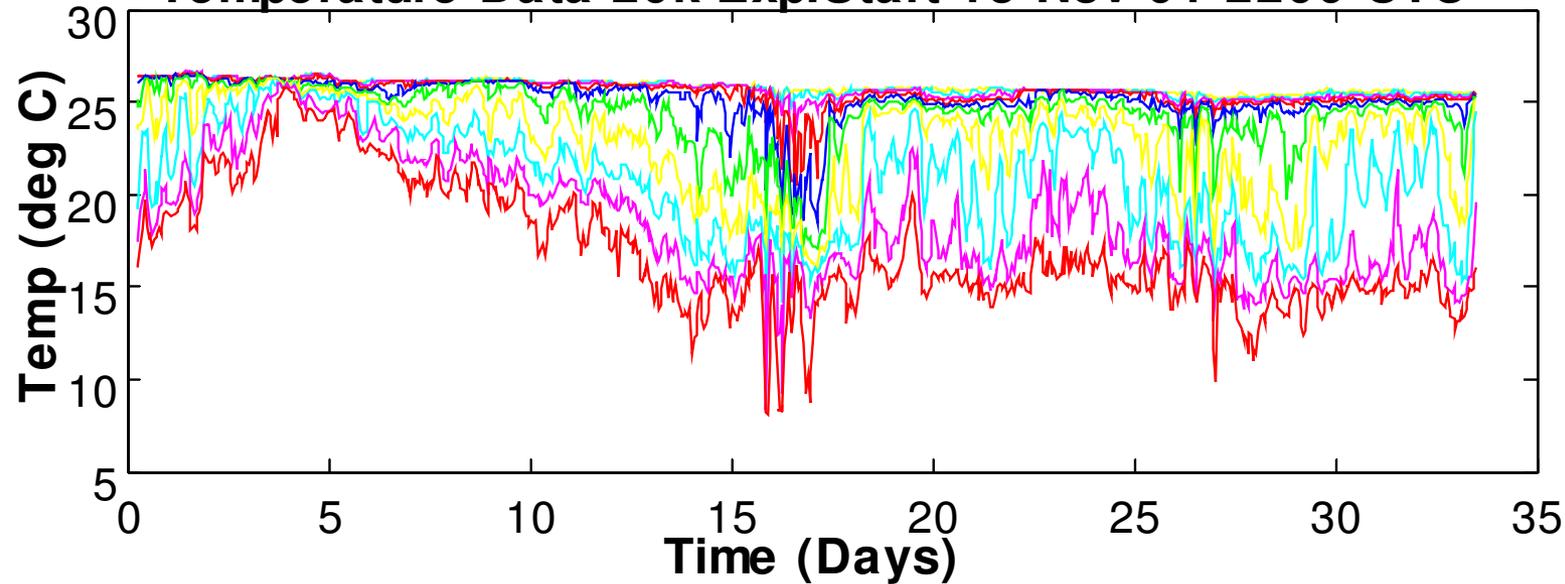
Ft. Lauderdale

Miami

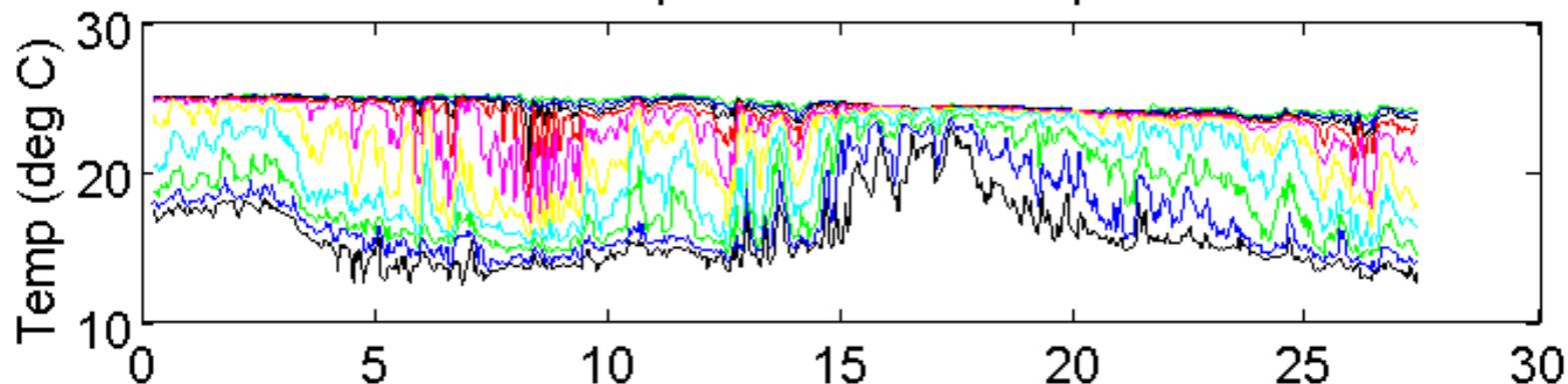
**Temperature Data 10k Exp. Start 9 Dec 99 2210 UTC**



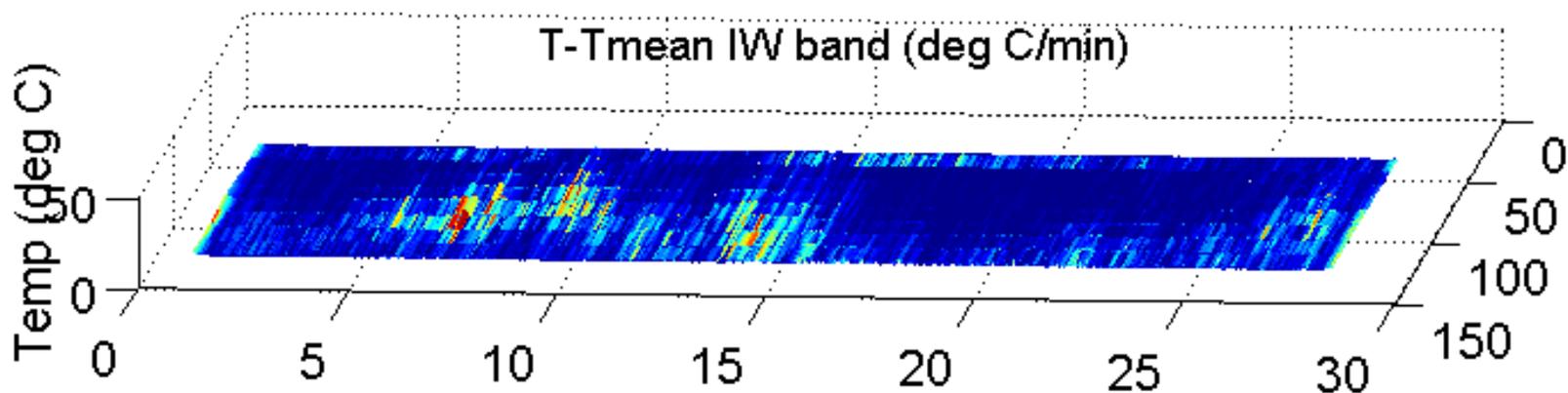
**Temperature Data 20k Exp. Start 13 Nov 01 2200 UTC**



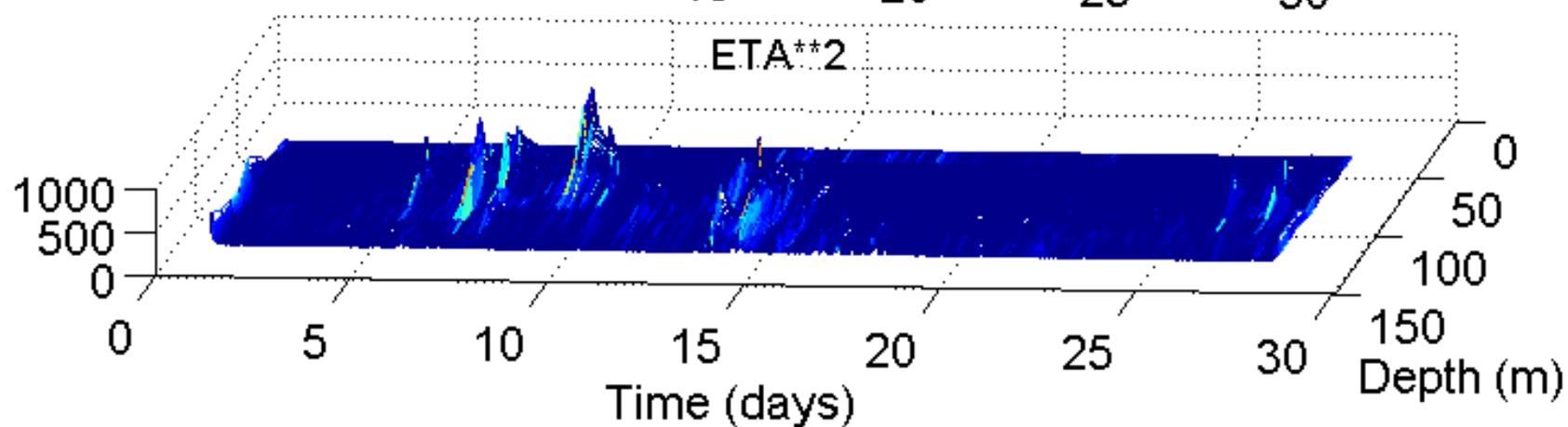
Temperature Data 10k Exp.



T-Tmean IW band (deg C/min)



ETA\*\*2



# Florida Strait Propagation Experiments

## Transmissions

M-Sequences

Hour	Frequency
------	-----------

1	100
---	-----

2	200
---	-----

3	400
---	-----

4	800
---	-----

5	1600
---	------

6	3200
---	------

7	100
---	-----

repeat

\*

\*

28 days



## Reception

VLA

32 – Phones

Coherent Averaging  
(1 min)

SHARP  
Pulse compression

**Pulse Responses**  
One per minute

## Signal Processing of M-sequences:

- Synchronous sampling  $n \times f$ ,  $n = > 4$ .
- Coherent averaging for 1 minute.
- Sharp Pulse Compression (SPC) - Hadamard Transforms - a matched filter operation that yields the pulse response instead of the correlation of the pulse response.

## Result:

- Gain =  $10 \log(M \times L)$ , =36dB @400 Hz.
- 2x Improvement in time resolution.
- Transparent to end user - no time leakage.
- Robust and well documented.

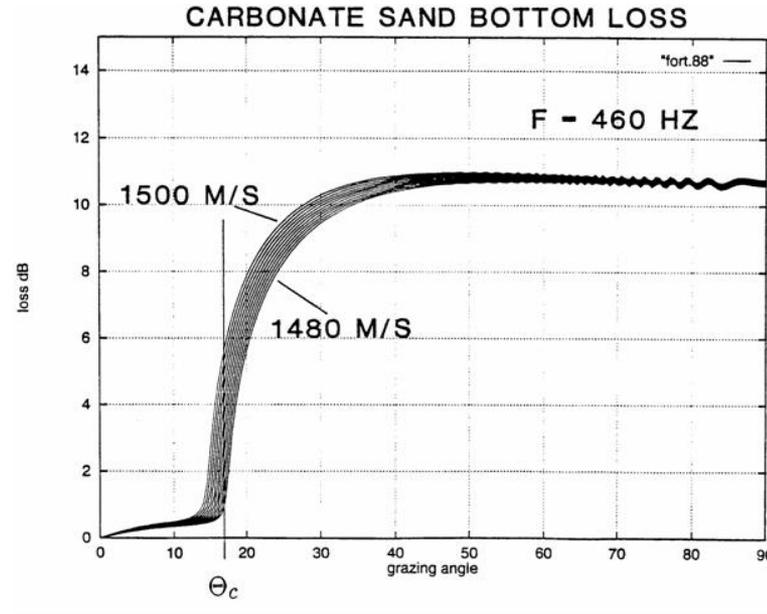
# Propagation Modeling

## Identifying modes and arrivals

# Propagation Modeling

## Propagation Models

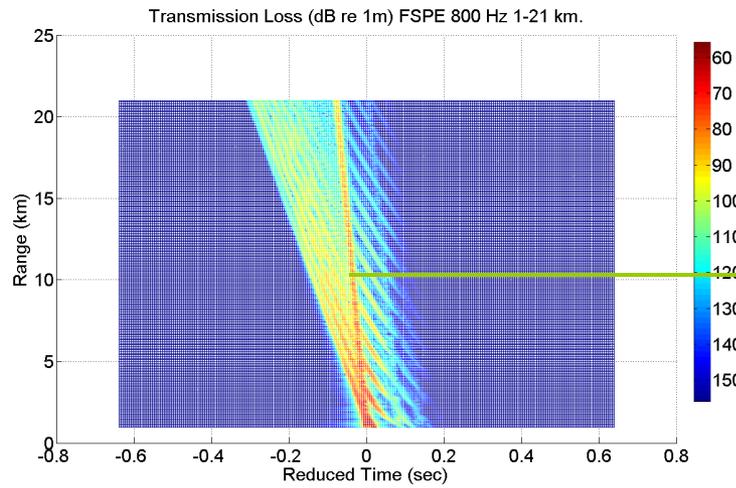
- PE
  - MMPE
- Normal Mode
  - PROSIM
  - SNAP
- SAFARI



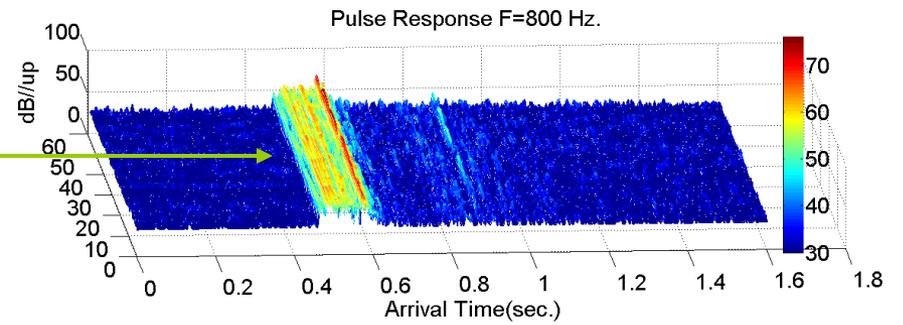
## Bottom Models

	Velocity (m/s)	Gradient (1/s)	Density	Loss (dB/km/Hz)	Shear (m/s)	Shear Loss (dB/km/Hz)
MONJO	1585	1.4	1.85	.30	300	3.3
MEASURED (cores)	1640	1.4	1.95	.30	300	6.3
CHAPMAN (inv)	1720	1.4	2.06	.60	300	6.3

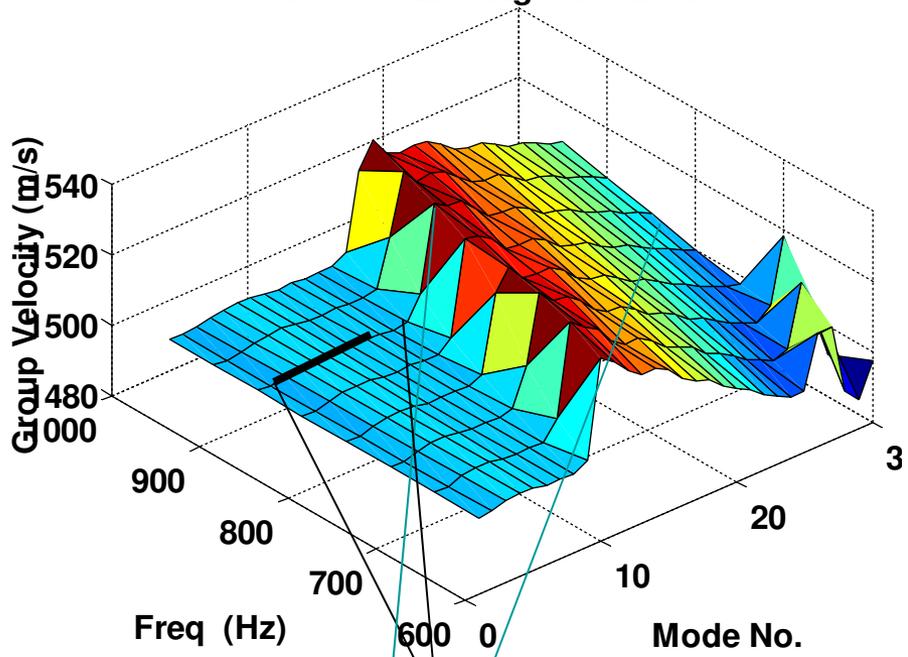
## PE Prediction of 800 Hz. Pulse Response



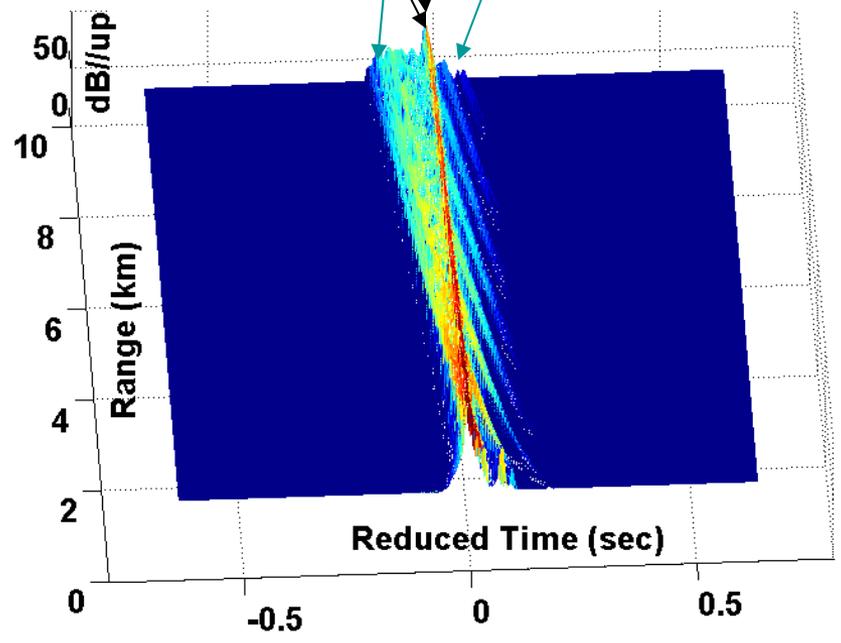
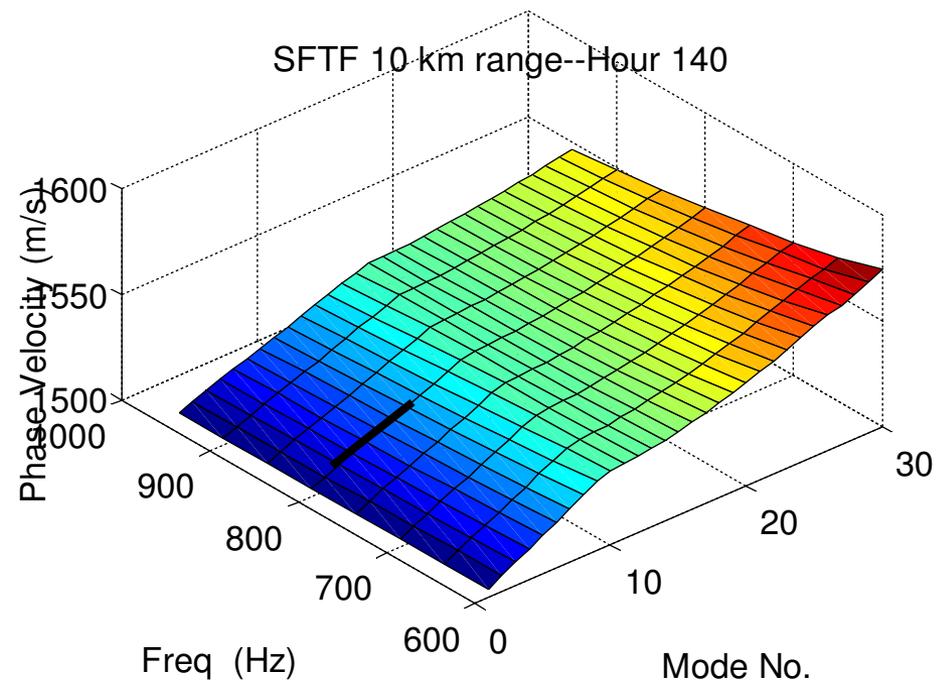
## Measured - 1 Hour



SFTF 10 km range--Hour 140



SFTF 10 km range--Hour 140



$$\beta^{-1} = - \frac{\Delta S_{g,mn}}{\Delta S_{p,mn}}$$

# Effects of an eddy

## **3. Produces a focusing sound speed profile for RBR Modes**

- Deep source is amplified relative to shallow source
- Near perfect multipath recombination

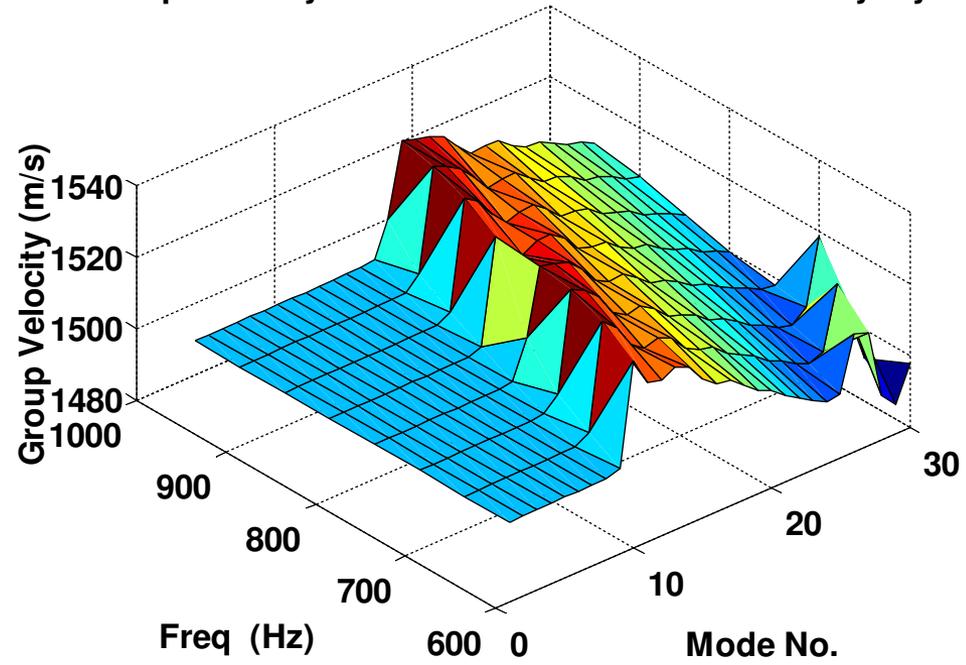
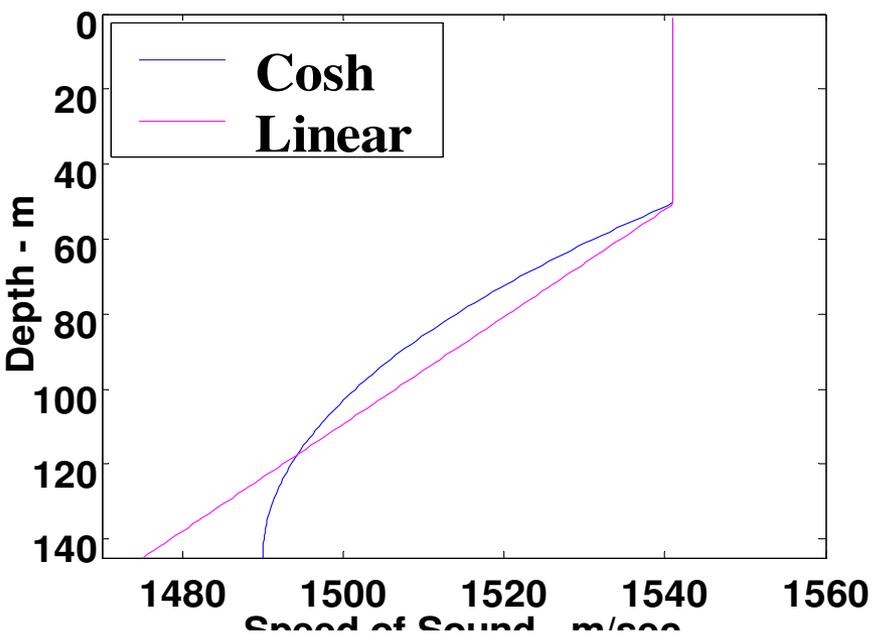
## **4. Forms a duct for internal waves to propagate onto the shelf**

- Orders of magnitude increase in IW energy
- Corresponding increase in sound speed variability –degrades signal coherence

**Mesoscale modulation of cross shelf exchange in the Straits of Florida**  
**D. Olson, H. DeFerrari, N. Shay and W. Johns**  
**Progress in Oceanography**

**Focused arrivals in shallow water propagation in the Straits of Florida**  
**H. DeFerrari, N. Williams and H. Nguyen**  
**ARLO 4, 106 (2003)**

Group Velocity COSH Profile w/ 75 m isovelocity layer



$$\beta^{-1}$$

SRBR      BRB

Linear

1.0

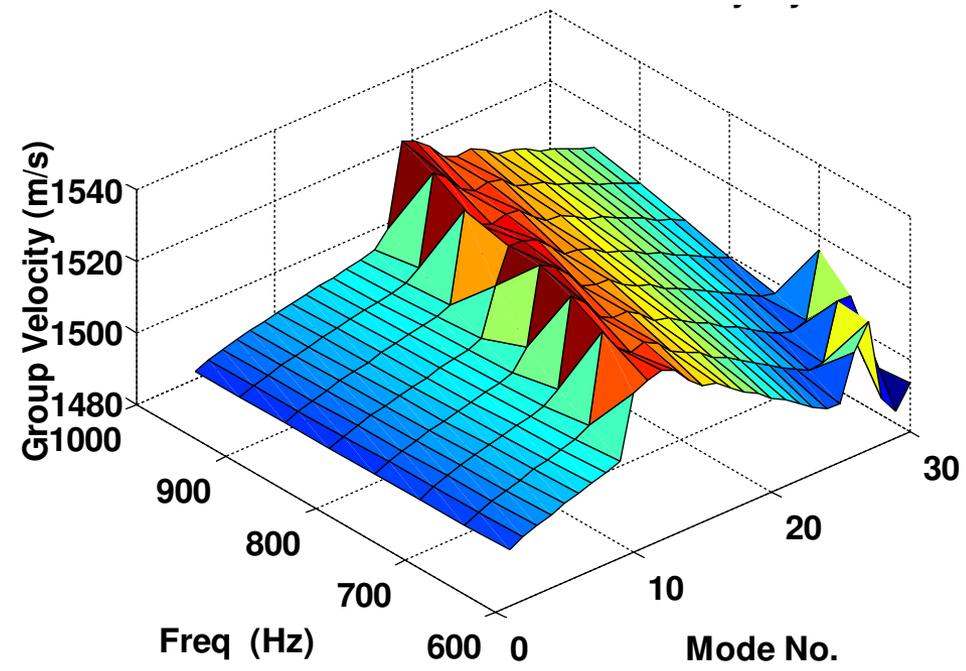
-0.5

Cosh

1.2

0.0

$$c_o \cosh(g(1-z/D))$$



## Ray/Mode Equivalence for $\beta^{-1}$



$$\text{Travel Time} = \int \frac{ds}{c(s)} \propto \frac{PL}{\langle c \rangle}$$

### Travel Time dependence on Launch Angle:

Linear Profile  $\langle c \rangle > \text{PL}$ ,  $\beta^{-1} = -.5$   $\text{PL} > \langle c \rangle$ ,  $\beta^{-1} = 1.0$

Cosh Profile  $\langle c \rangle = \text{PL}$ ,  $\beta^{-1} = 0.0$   $\text{PL} > \langle c \rangle$ ,  $\beta^{-1} = 1.2$

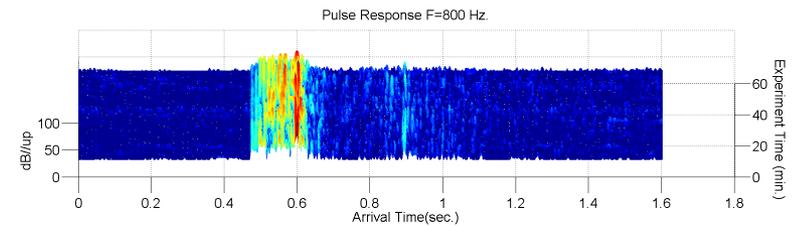
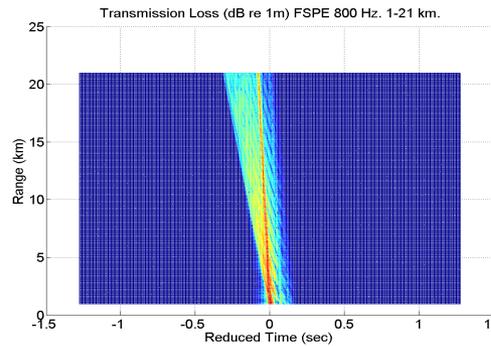
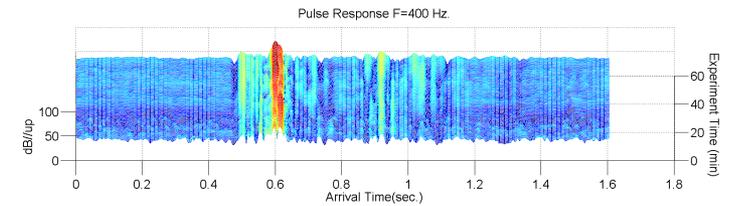
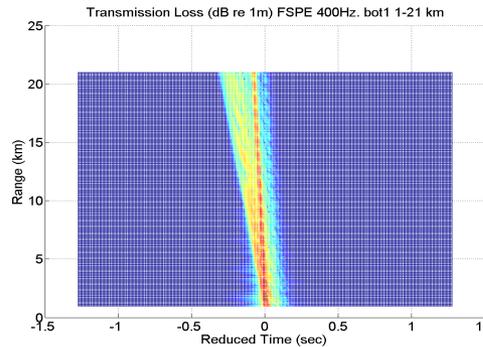
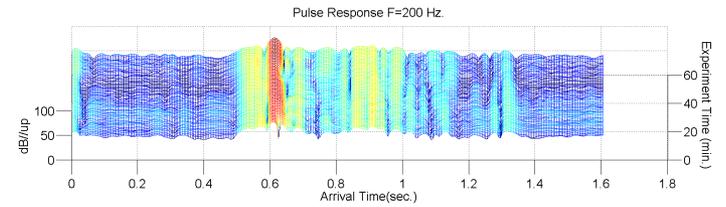
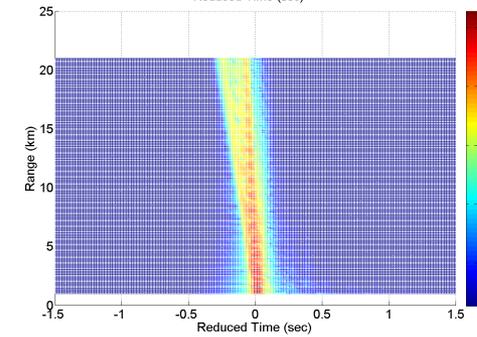
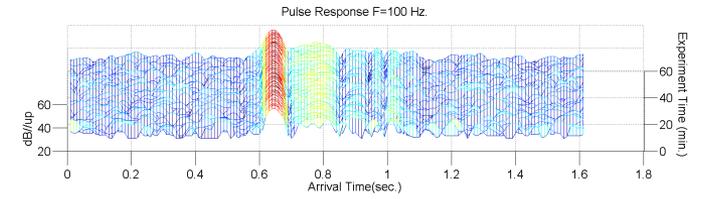
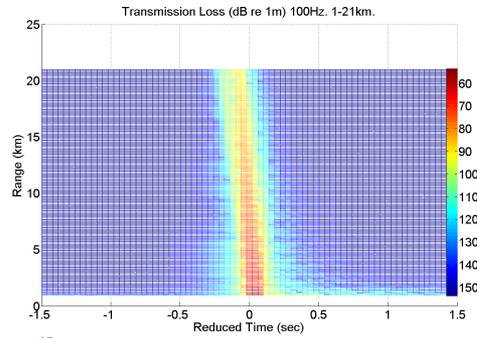
**Conclusion: All BRB eigenrays have exact same travel time at each range.**

# Frequency Dependence Model < > Measurements

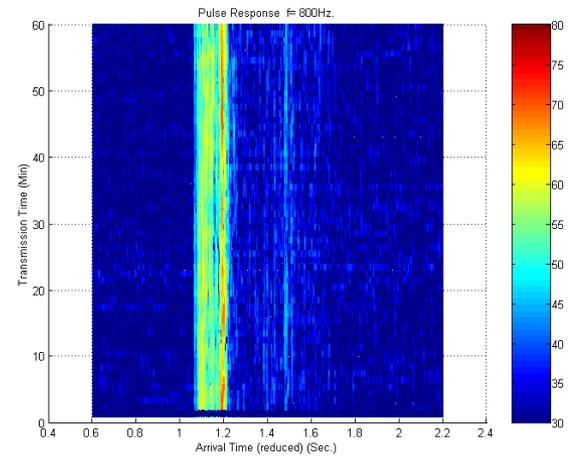
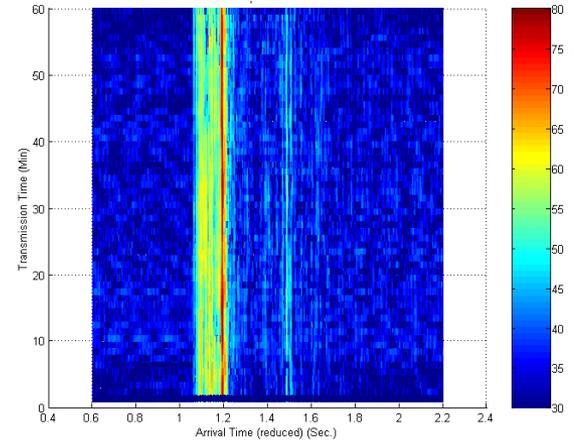
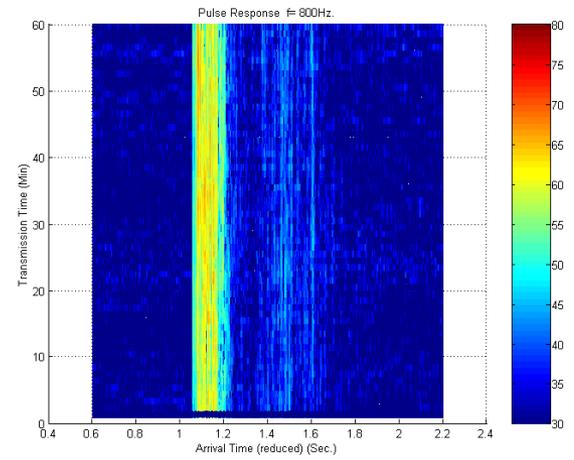
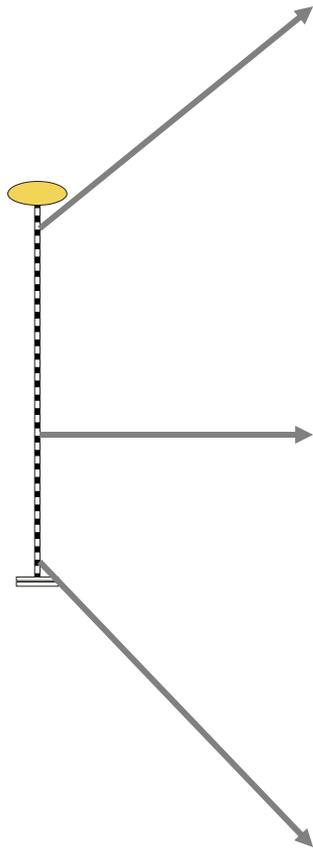
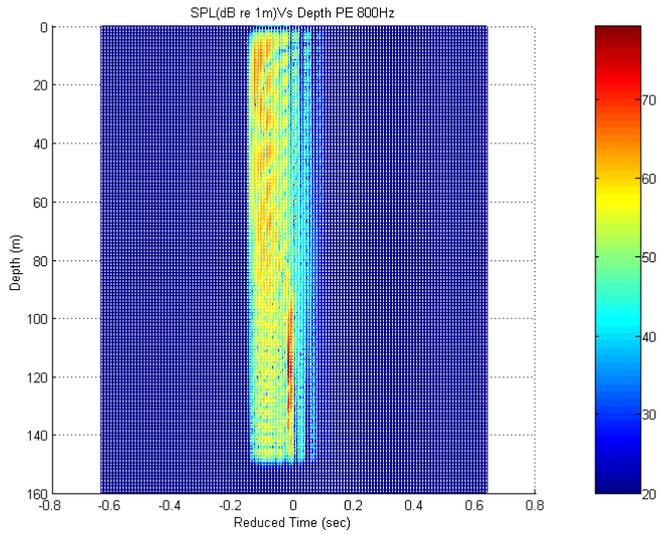
## FSPE

10 km range - f/100 RBR/SRBR modes

- 8 RBR and 8 SRBR @800Hz.
- 4 RBR and 4 SRBR @400 Hz.
- >
- 1 total @50 Hz.



# Depth Dependence

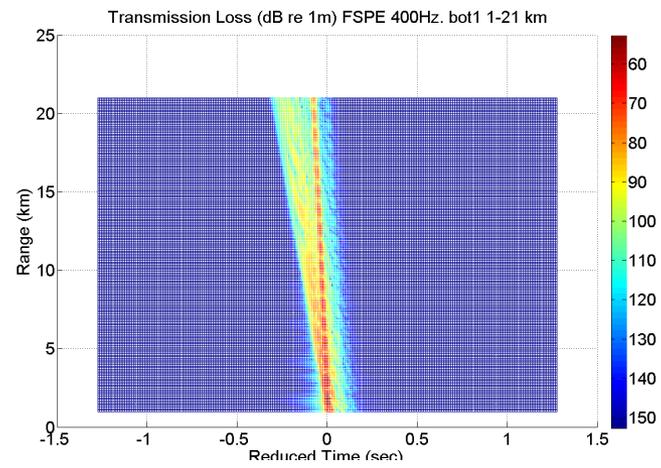


PE Prediction: Pulse Response vs. Depth

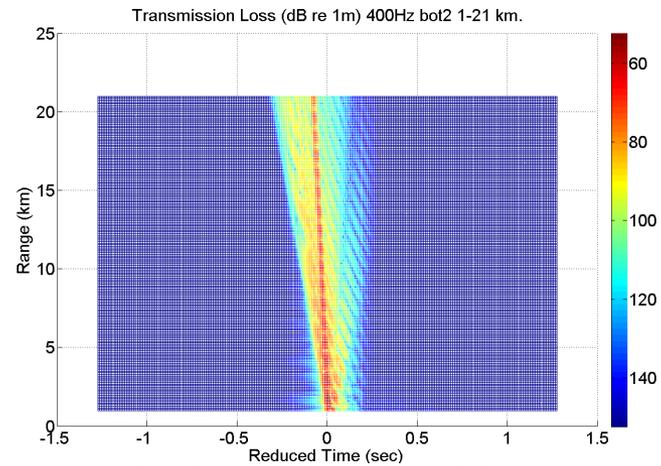
# PE Predictions for 3 Bottom Models

## Monjo Bottom

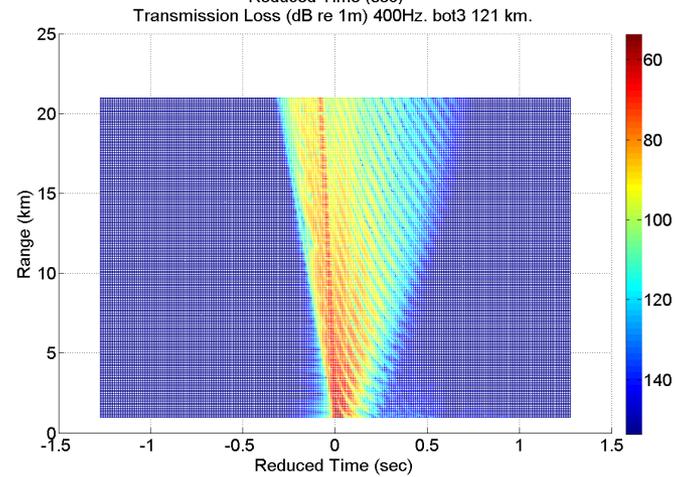
Bottom C = 1580 m/sec.



Bottom C = 1620 m/sec.



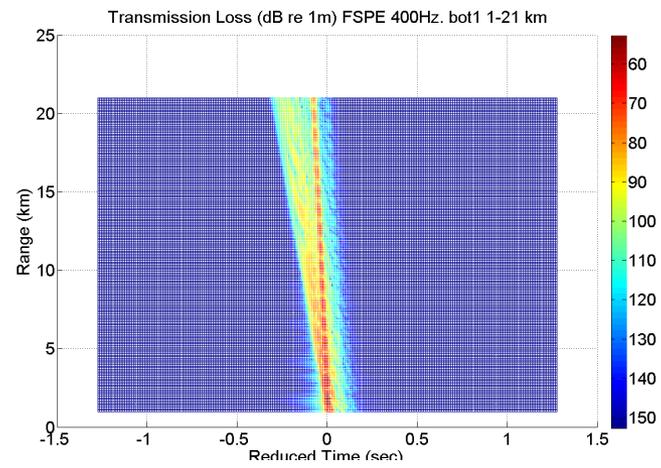
Bottom C = 1720 m/sec.



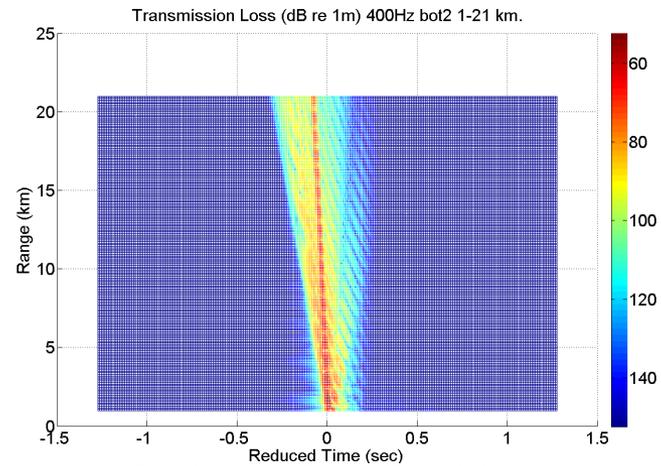
# PE Predictions for 3 Bottom Models

## Monjo Bottom

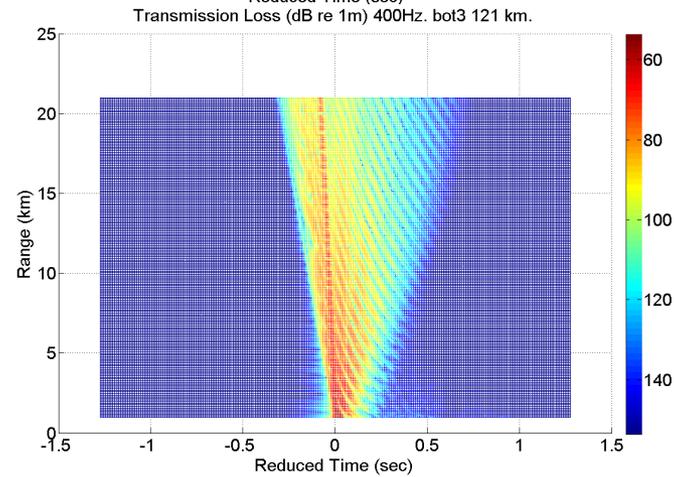
Bottom C = 1580 m/sec.



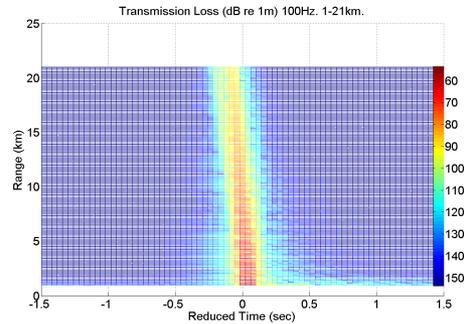
Bottom C = 1620 m/sec.



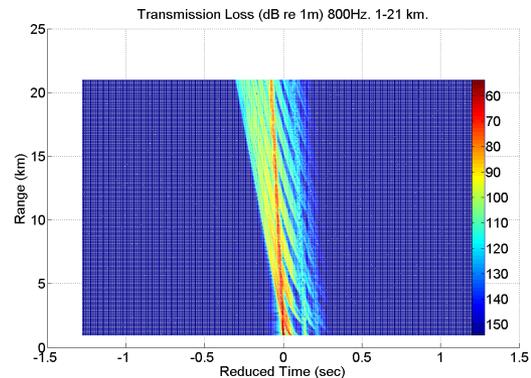
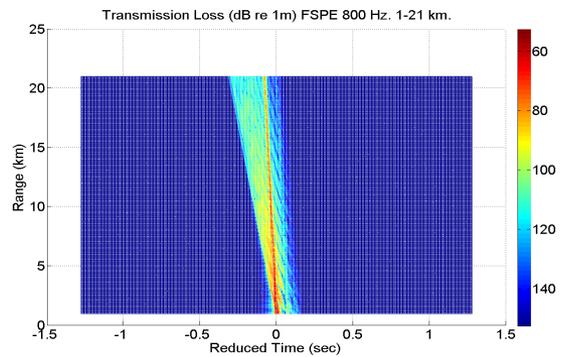
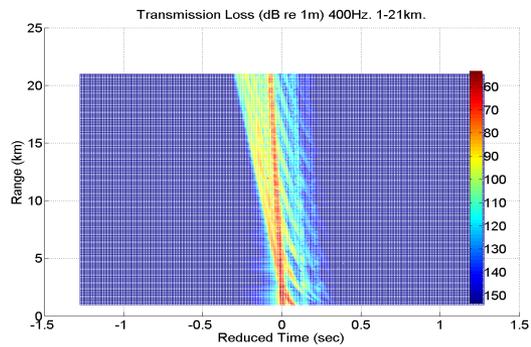
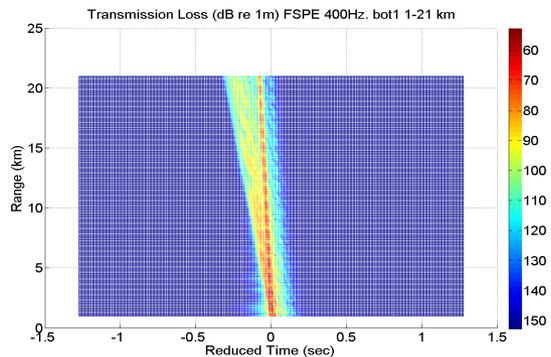
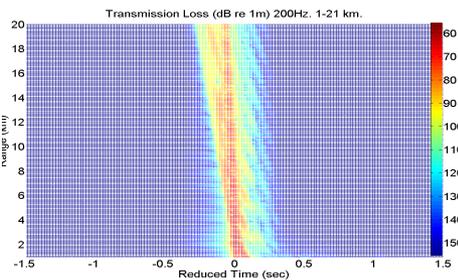
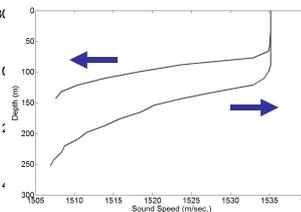
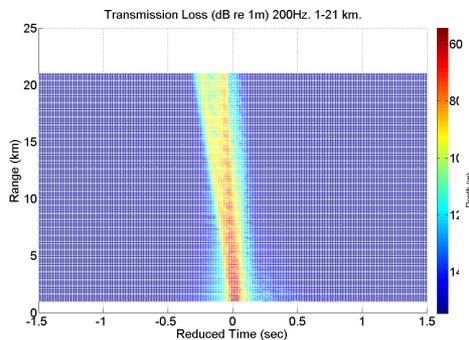
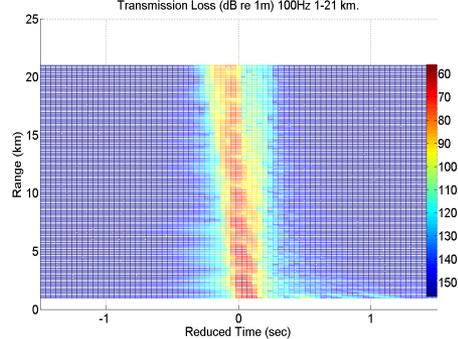
Bottom C = 1720 m/sec.



FSPE



AO



## AO Predictions:

2. Propagation by RBR and SRBR modes/rays. AO interested in SRBR as noise carrying paths.
3. Summer SS profile will narrow the arrival time spread of SRBR's
4. Total number of observable SRBR modes - approx =  $f/100$ . e.g. 4 @ 400 Hz. Only 1 mode for frequencies below 100 Hz.
5. Strong downward  $C(z)$  gradients and absorbent bottom will result in very large TL for SRBR paths - difficult to measure at long ranges > 30km!
6. Temporal coherence times = >10 min  $\rightarrow$  1 hour+ for lower frequencies with SRBR 50% longer than RBR.
7. Horizontal coherence (radial, bottomed HLA) = > 100wavelengths. e.g. 1500m @100HZ.
8. Propagation model predictions match FSPE measurements best with slower 'Monjo' bottom model than with observed fast "Chapman" bottom. Geo-acoustic reasons unknown.
9. Many low-loss out-of-plane arrivals observed that possibly obscure the detection of low-level late SRBR arrivals. A potential practical problem for noise canceling algorithms.
10. AO measurements results may not differ much from those at FSPE site, (a modeling conclusion!)

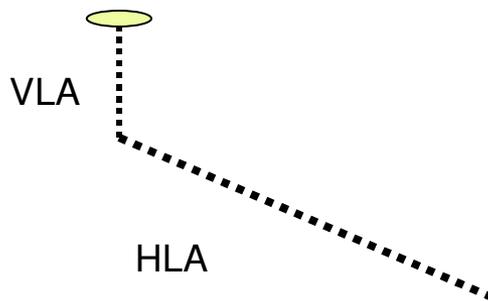
# SW06 Experiments – Mid-Atlantic Bight

MSM



19.7 km Range

85 m Depth



SHARK

MSM

M-Sequences

Center freq.	Band
4 Hz.	25
200	50
400	100
800	200
1600	400

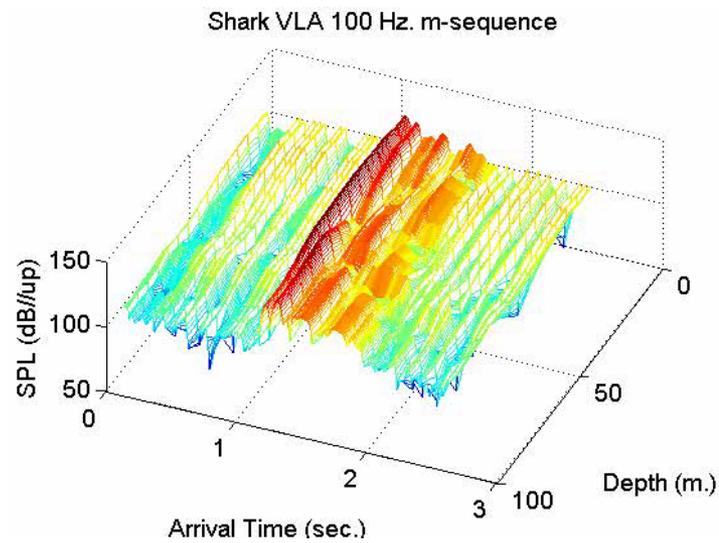
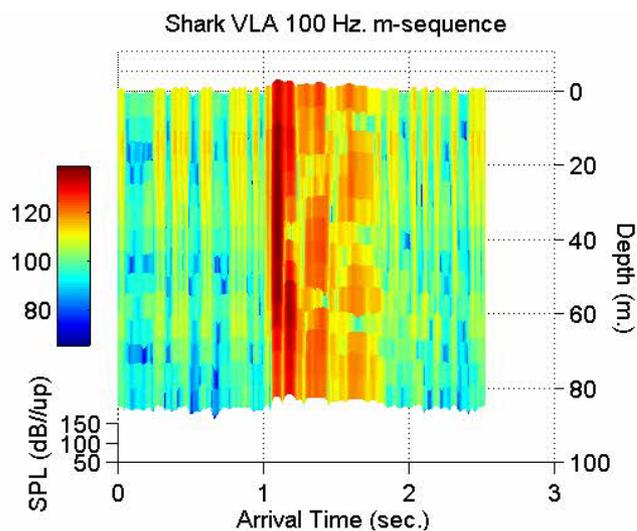
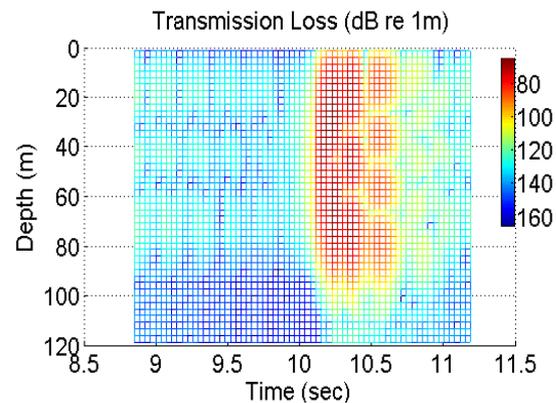
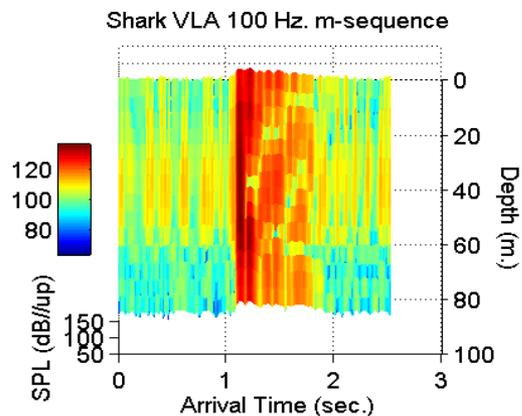
VLA 16 phones

HLA 32 phones 468 m (15 m spacing)

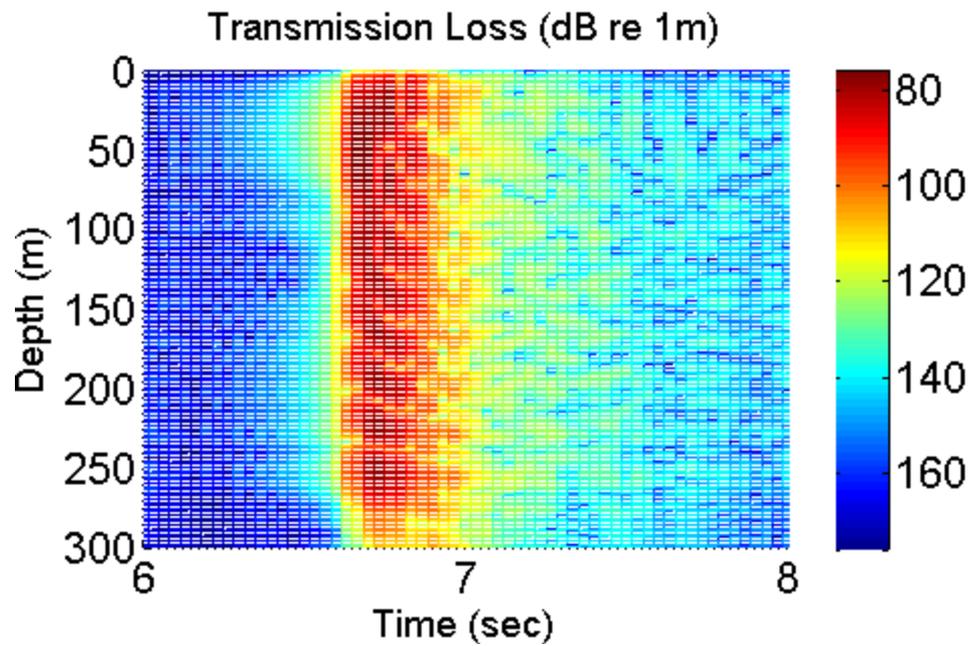
# SW06 Modes and Arrivals

Observed

Modeled



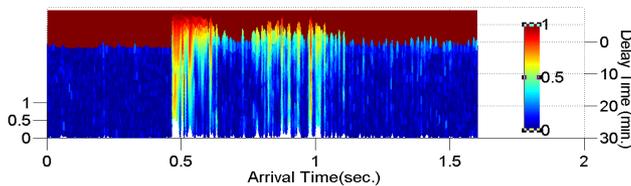
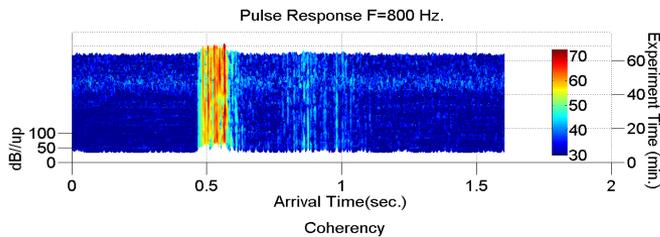
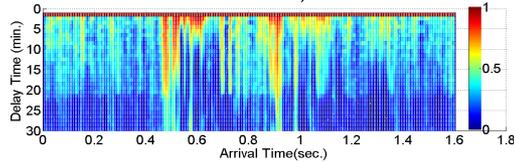
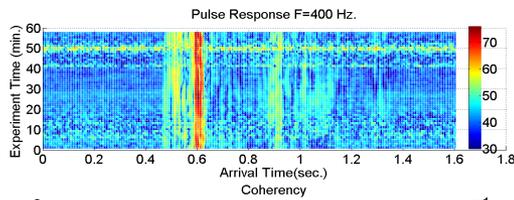
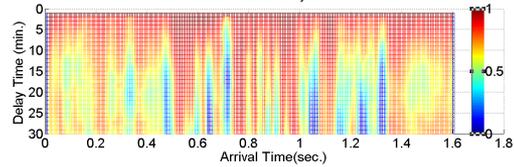
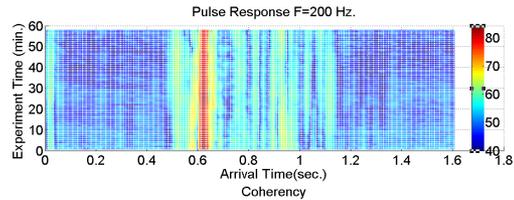
PE Prediction for AO  
100 Hz. 25 Hz band 10 km.



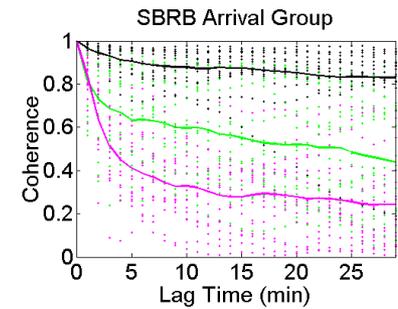
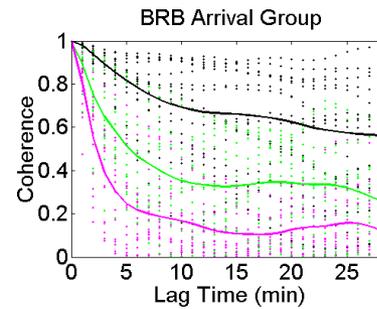
# Temporal Coherence



# Temporal Coherence



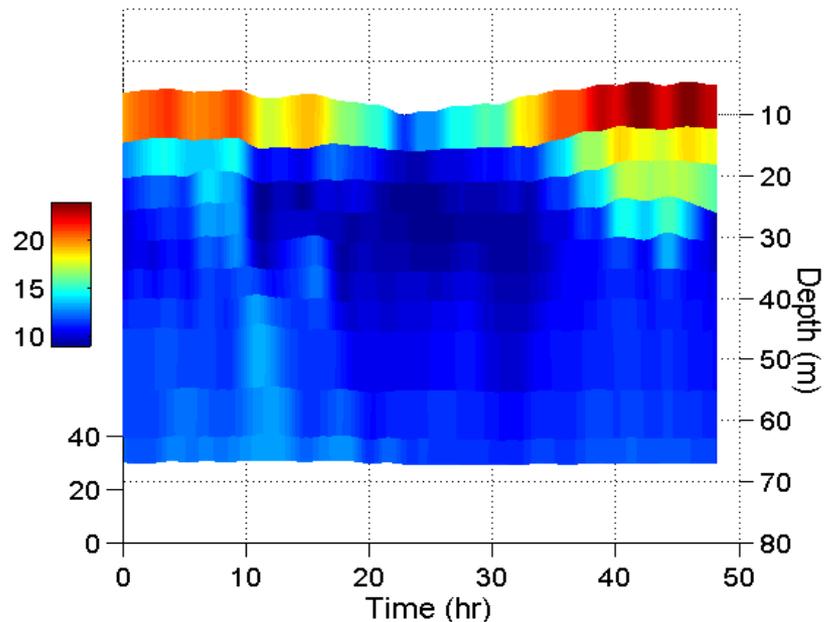
# Temporal Coherence



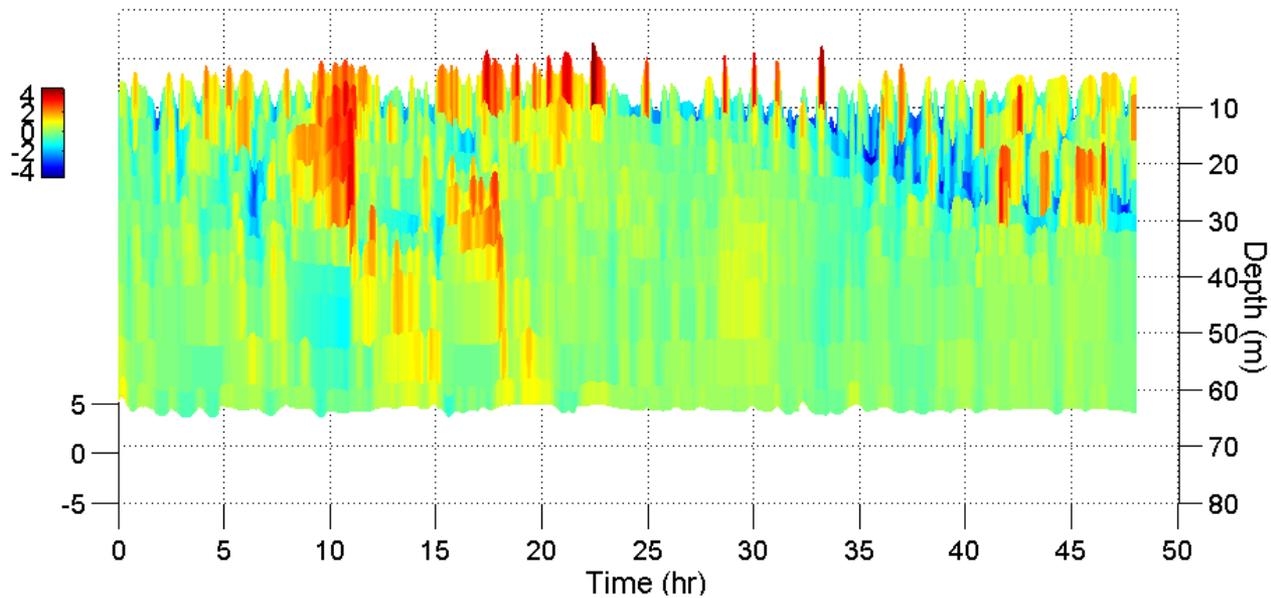
## Coherence time (.75 level)

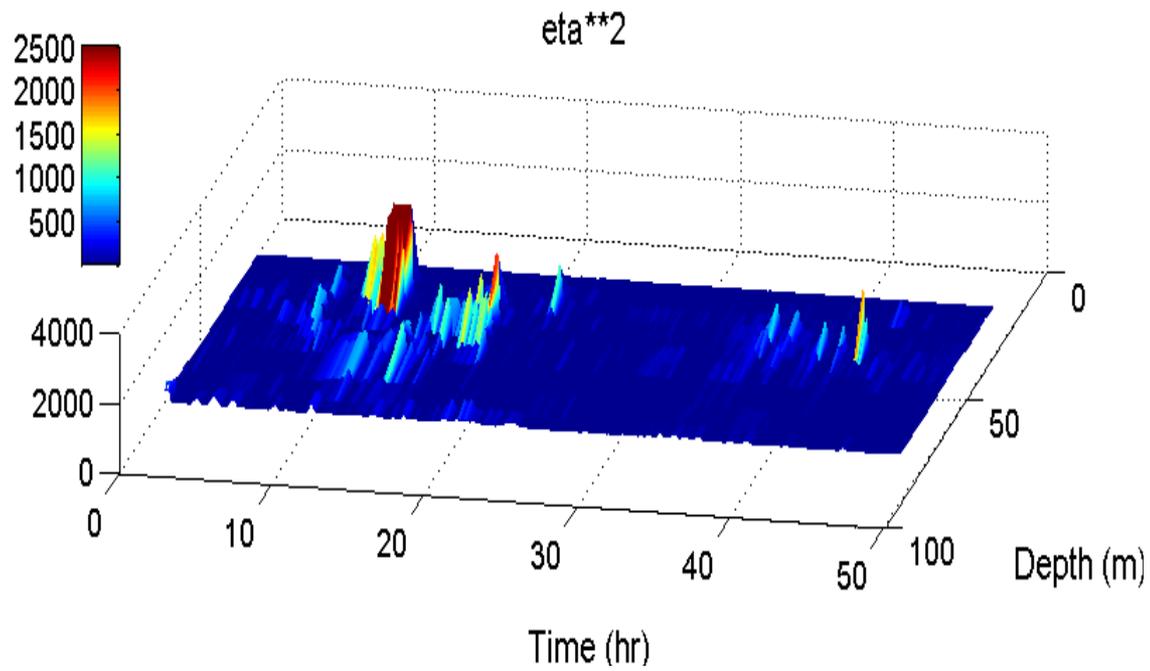
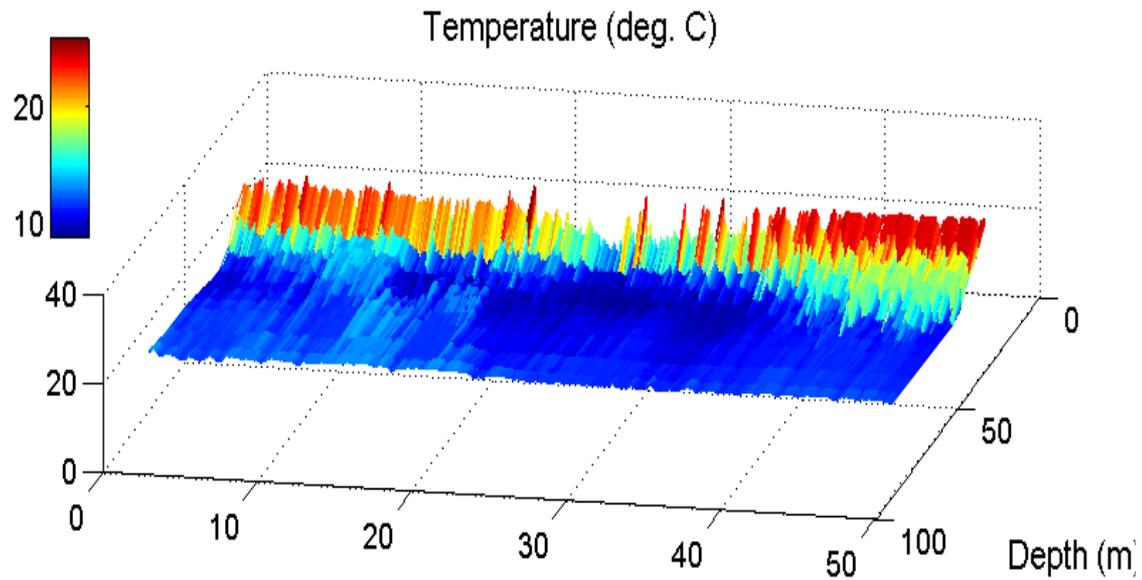
	BRB Group		SBRB arrival	
800Hz.	mean → 2.1	max → 6.5 minutes	800Hz. mean → 2.8	max → 6.5 minutes
400Hz.	3.4	12.0	400Hz. 4.2	>30
200	8.3	> 30	200	15.0 >> 30

Temperature (lowpass)(deg.C)

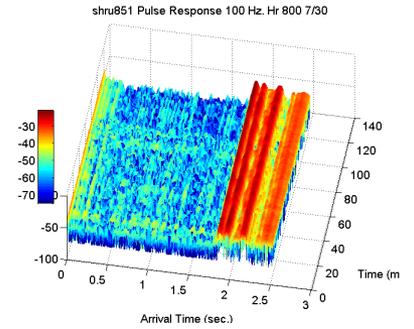
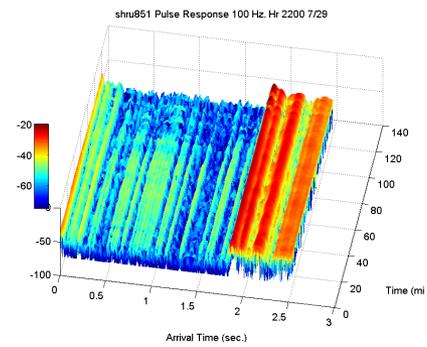
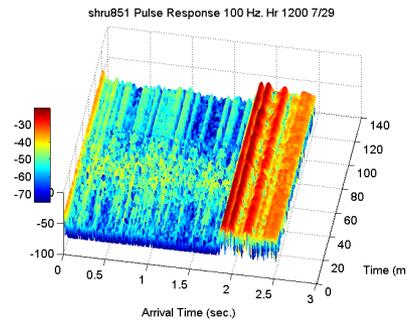
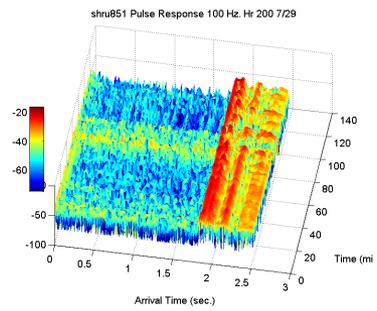
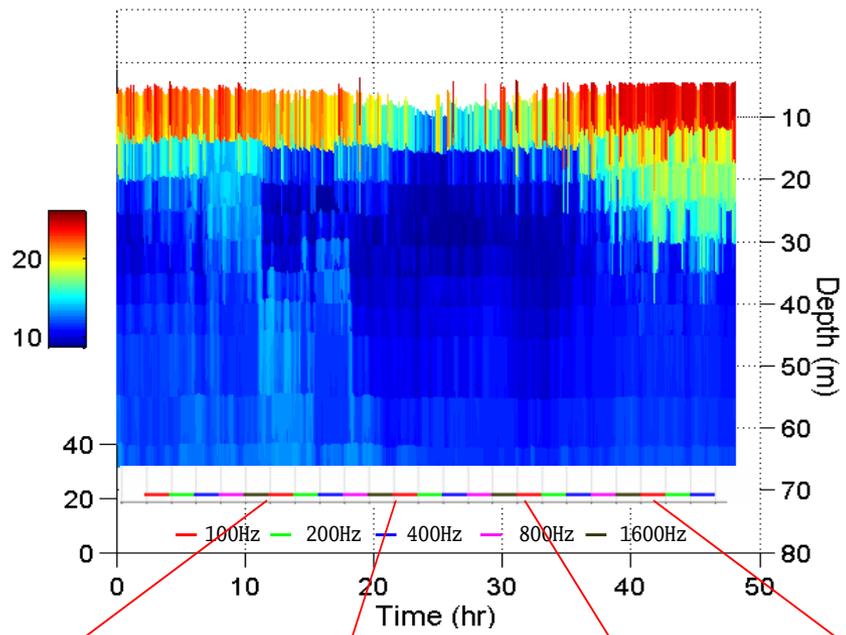


T-Tmean (deg. C)

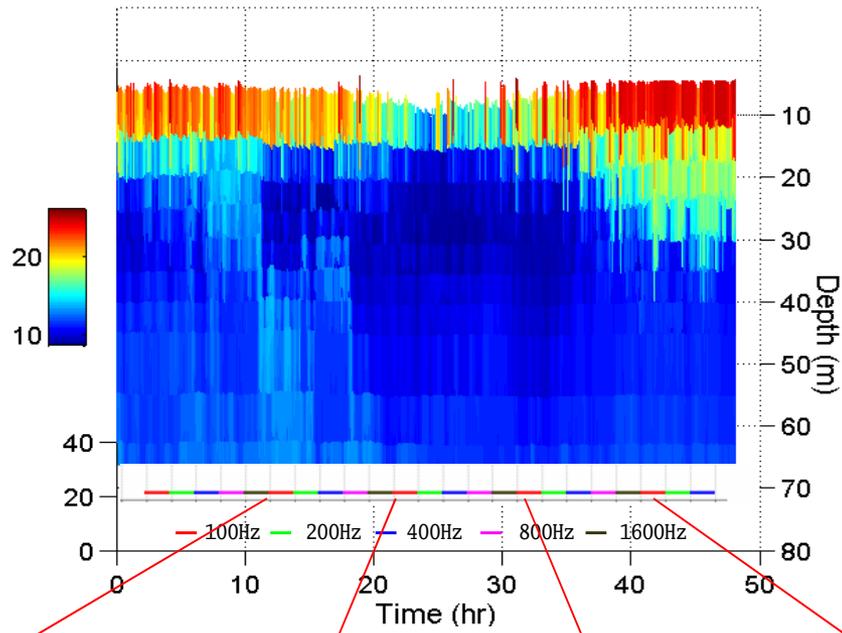
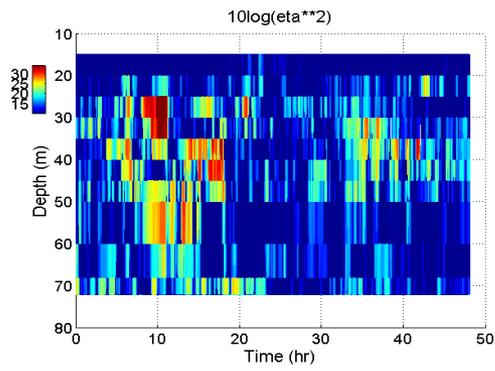




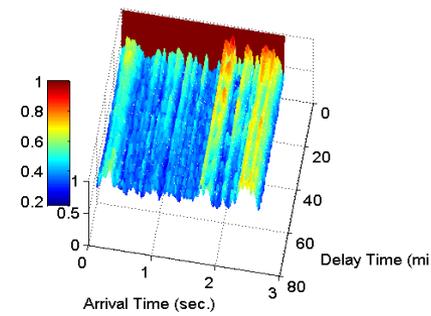
# Temperature (deg. C)



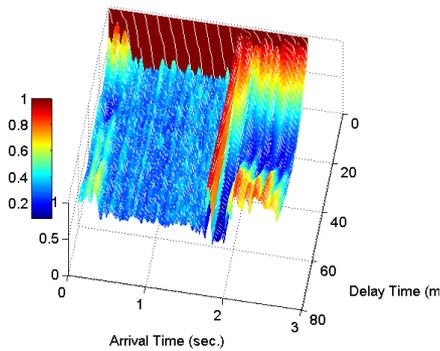
# Temperature (deg. C)



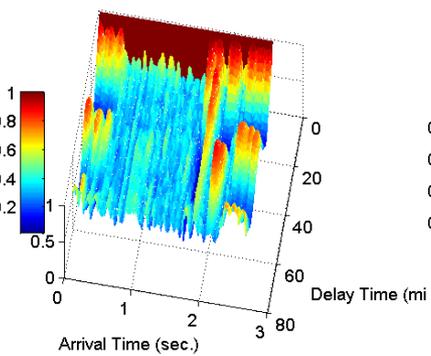
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



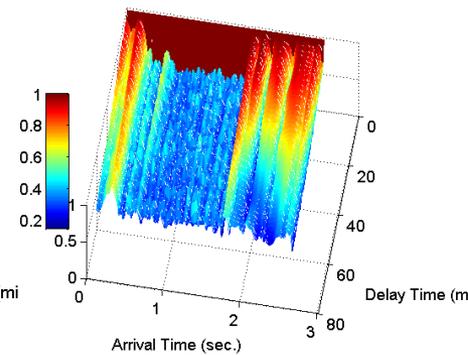
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



shru2252 Temporal Coherence 100 Hz.Hr 2200 7/29



shru852 Temporal Coherence 100 Hz.Hr0800 7/30



## Removing Phase Wrapping

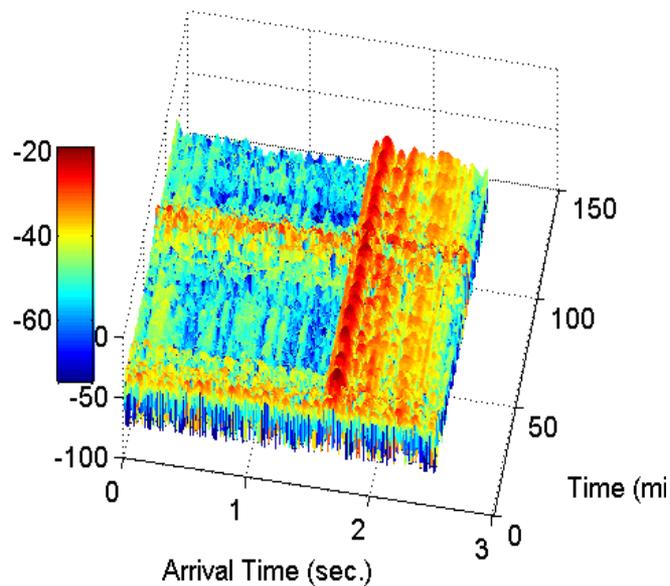
Approach:

- Back out dT/dt
- Loop through small increments of linear time shifts and re-compute COH
- Look for maximum.

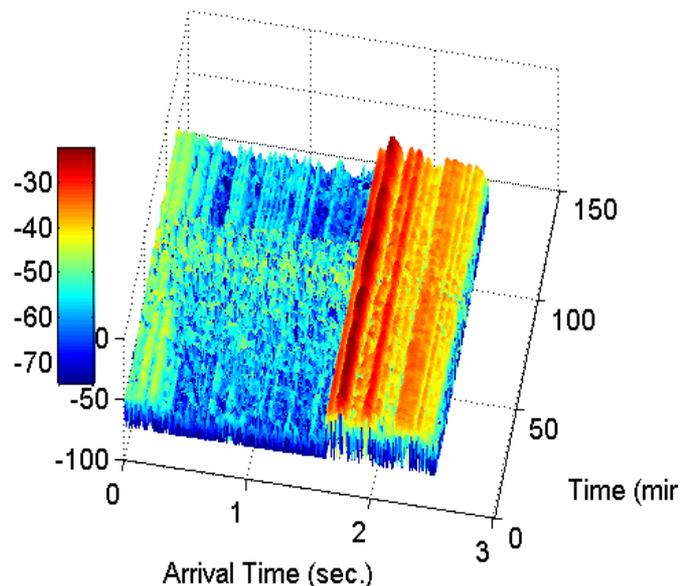
Each pulse  $p(t)$  is time shifted by  $\tau$  using the shifting theorem.

$$F^{-1}\left(F(p(t))e^{i\omega\tau}\right)$$

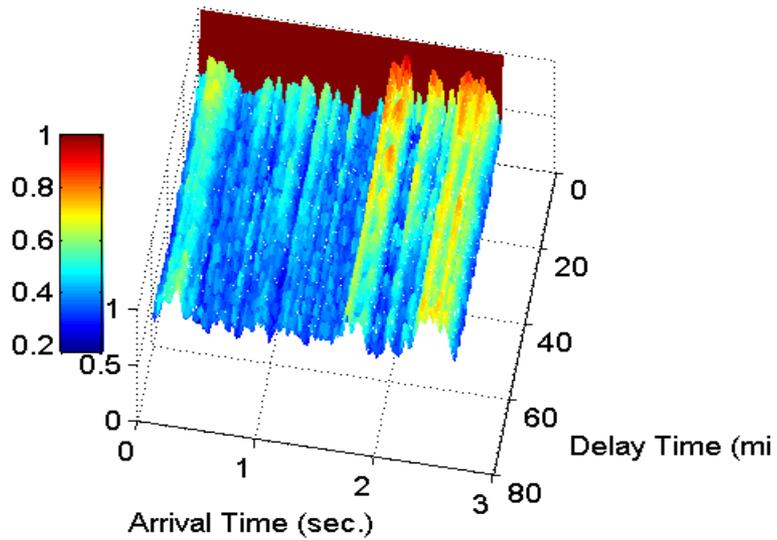
shru852 Pulse Response 100 Hz. Hr 200 7/29



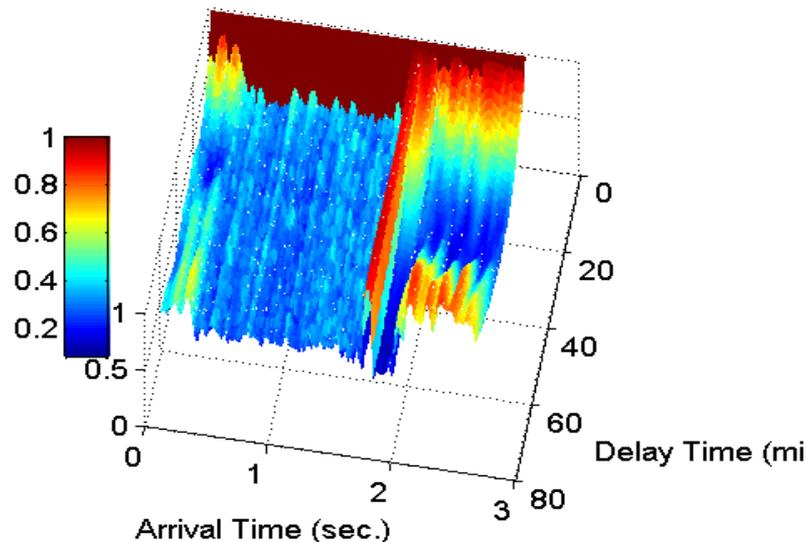
shru852 Pulse Response 100 Hz. Hr 1200 7/29



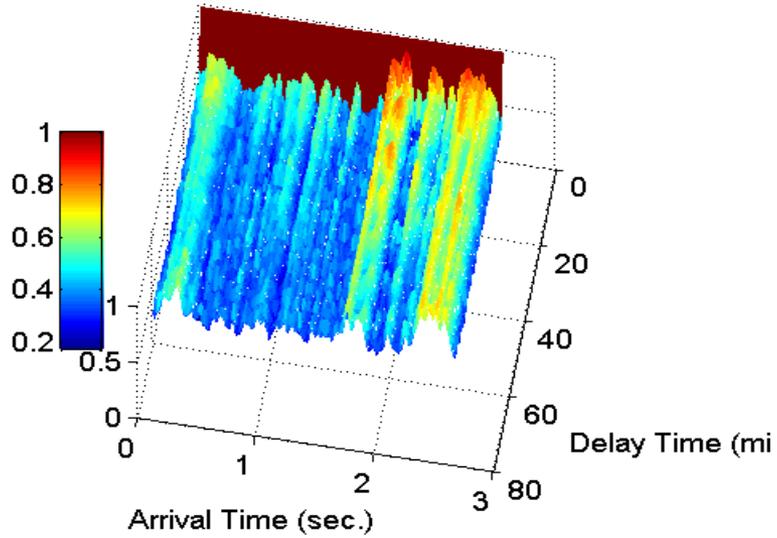
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



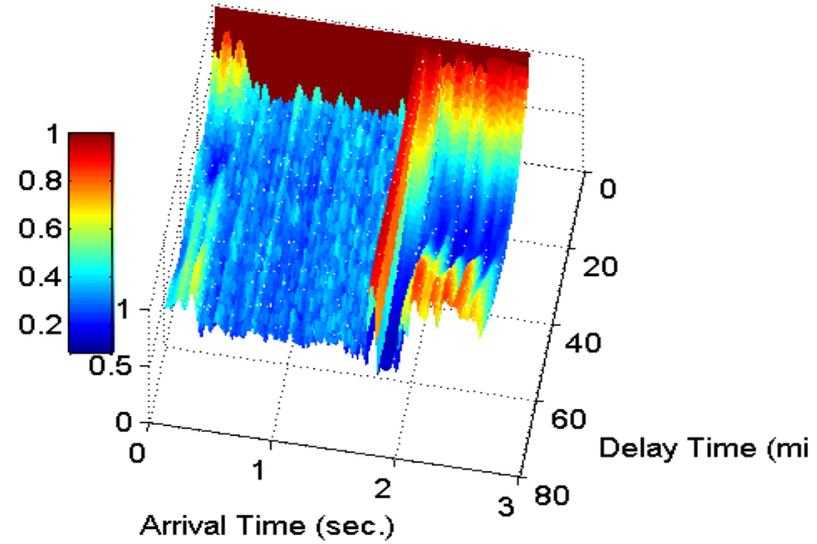
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



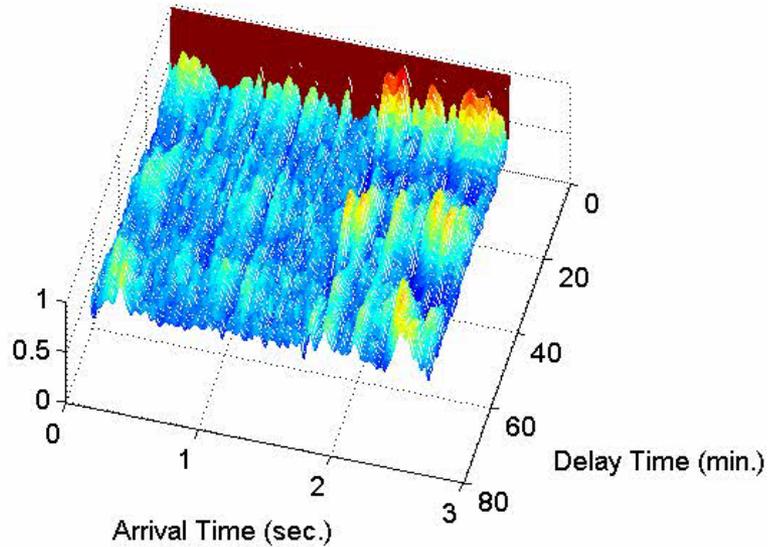
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



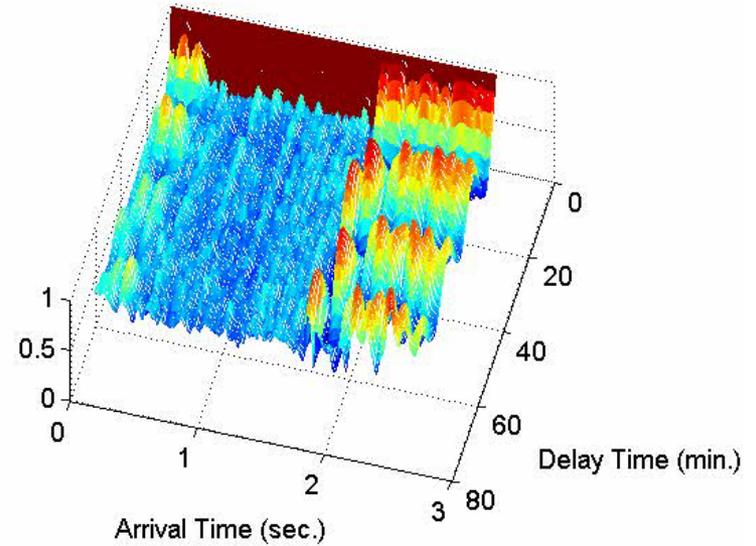
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29

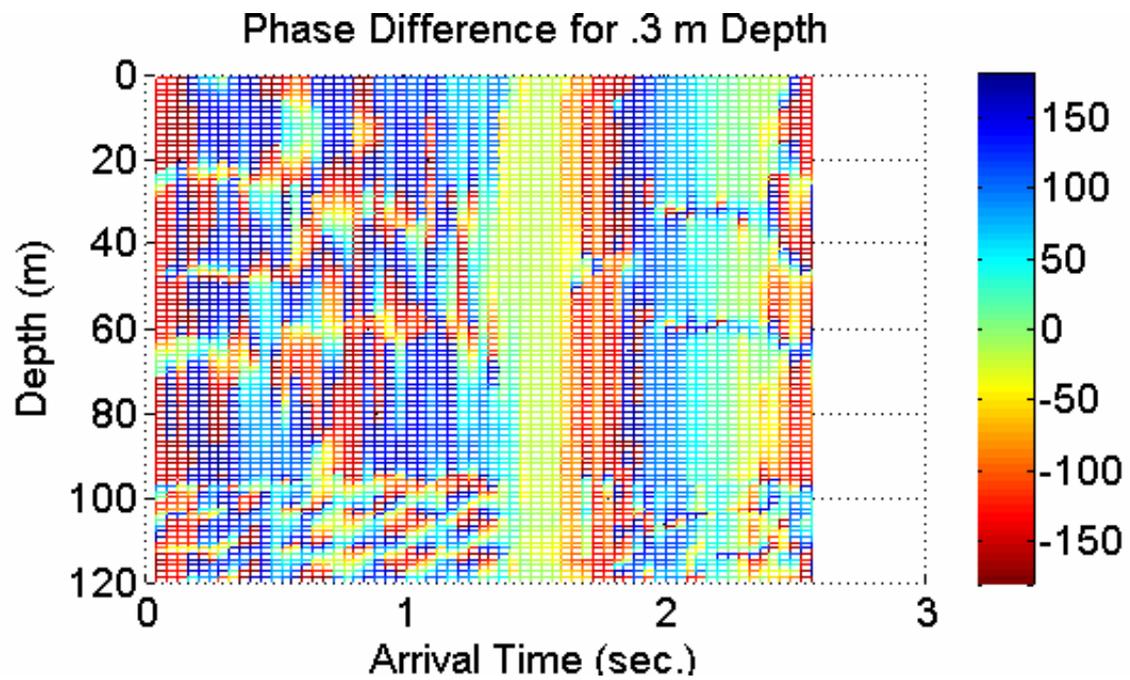


shru252 Temporal Coherence 100 Hz.

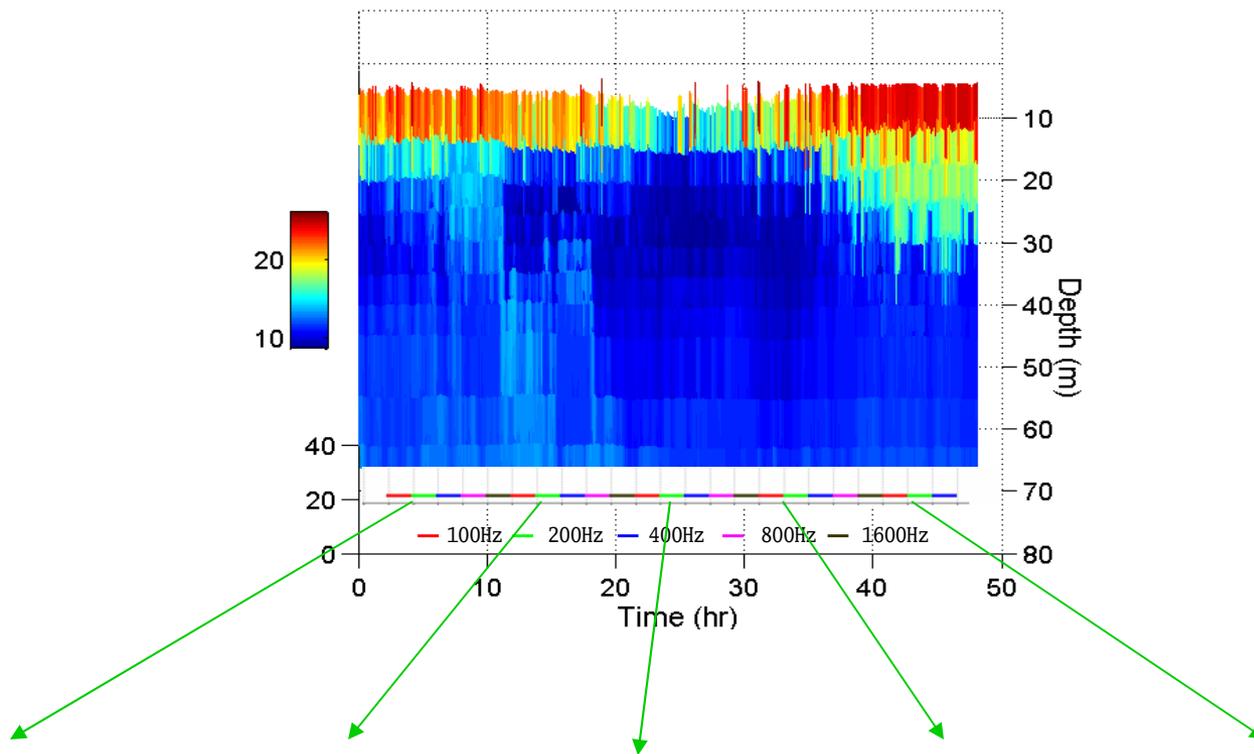


shru853 Temporal Coherence 100 Hz.

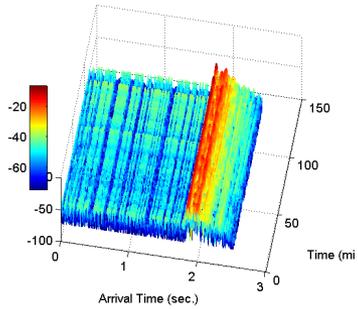




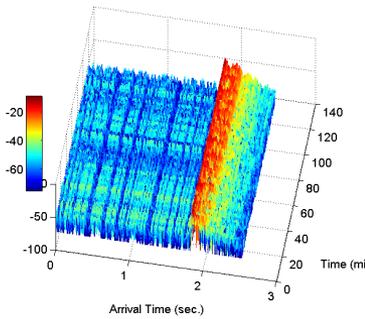
# Temperature (deg. C)



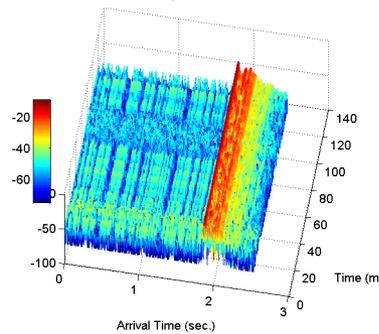
shru1851 Pulse Response 200 Hz. Hr 1800 7/28



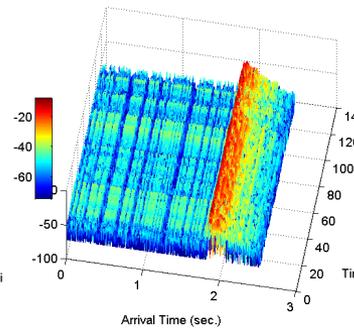
shru451 Pulse Response 200 Hz. Hr 400 7/29



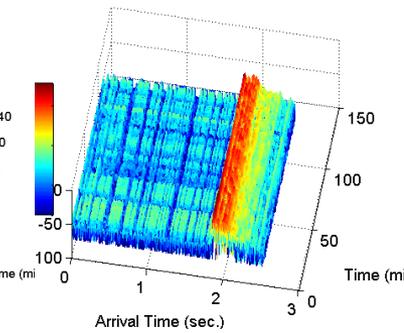
shru051 Pulse Response 200 Hz. Hr 1400 7/29



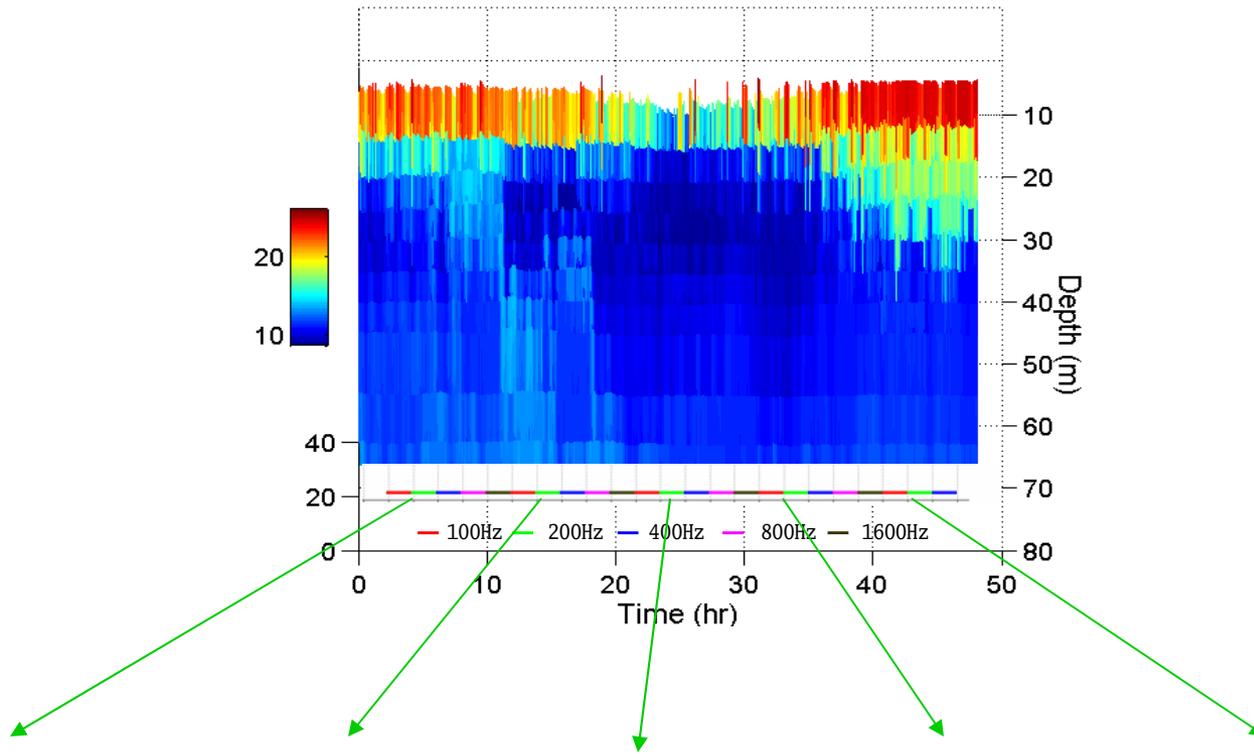
shru051 Pulse Response 200 Hz. Hr 2400 7/29



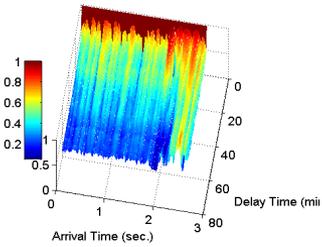
shru1051 Pulse Response 200 Hz. Hr 1000 7/30



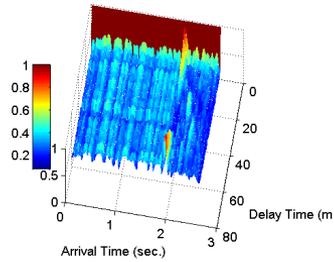
# Temperature (deg. C)



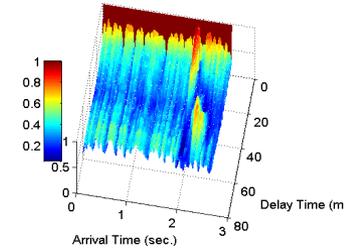
shru1851 Temporal Coherence 200 Hz. Hr 1800 7/28



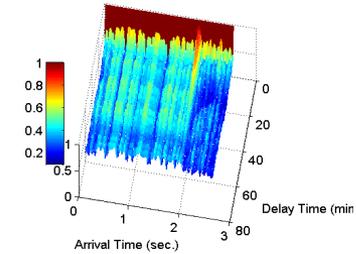
shru451 Temporal Coherence 200 Hz. Hr 400 7/29



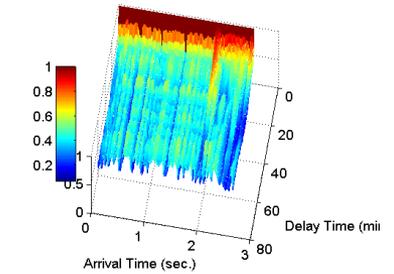
shru051 Temporal Coherence 200 Hz. Hr 1400 7/29

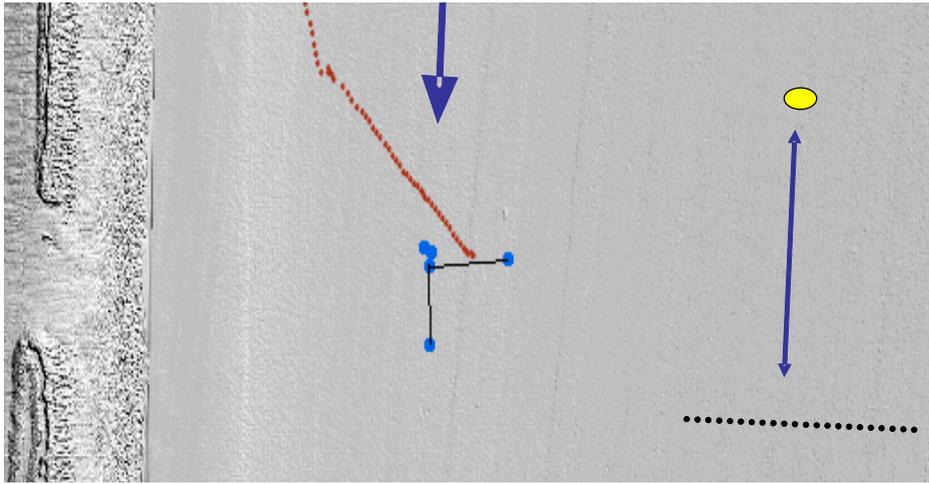


shru051 Temporal Coherence 200 Hz. Hr 2400 7/29



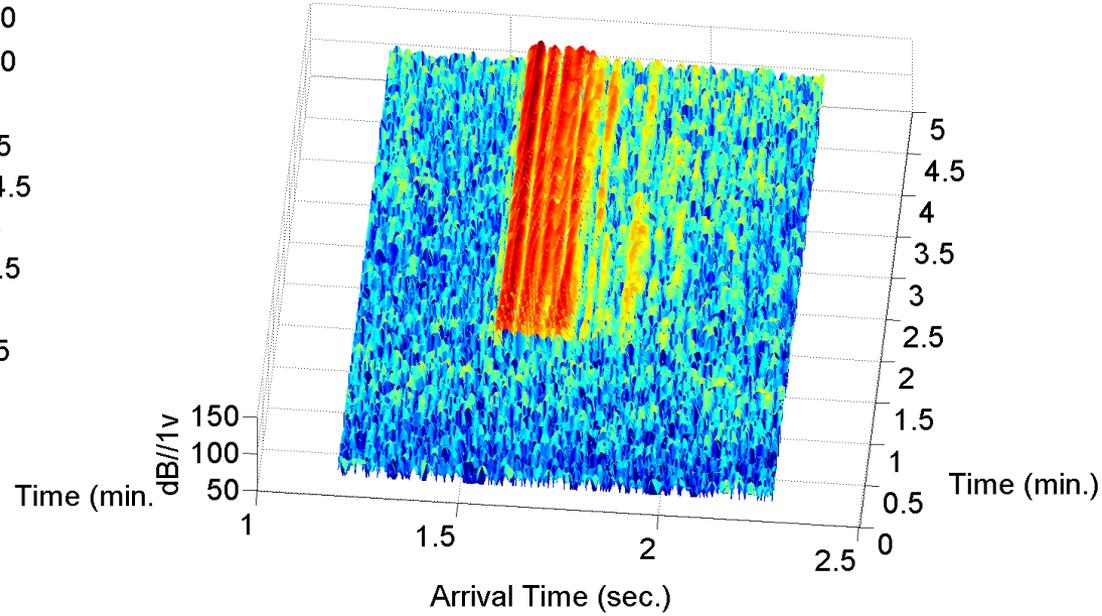
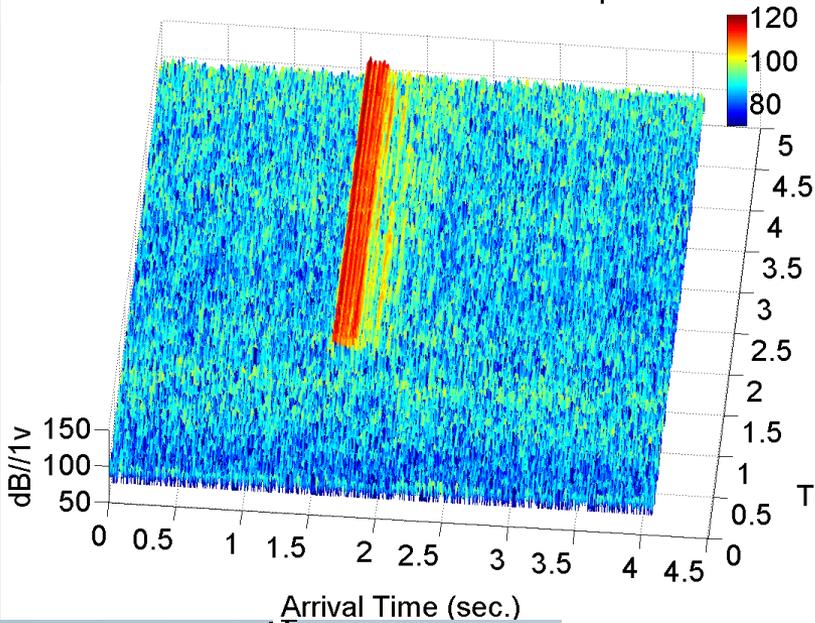
shru1051 Temporal Coherence 200 Hz. Hr 1000 7/30

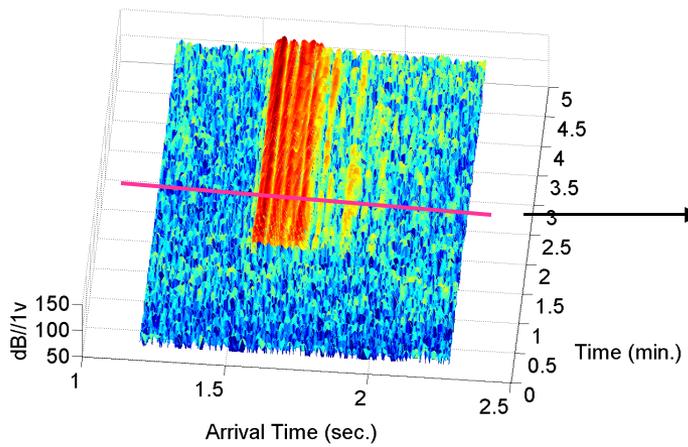




Acoustic Observatory Receiving Arrays  
 CALOPS Sept 07  
 Shipboard Suspended and Towed  
 Transmissions

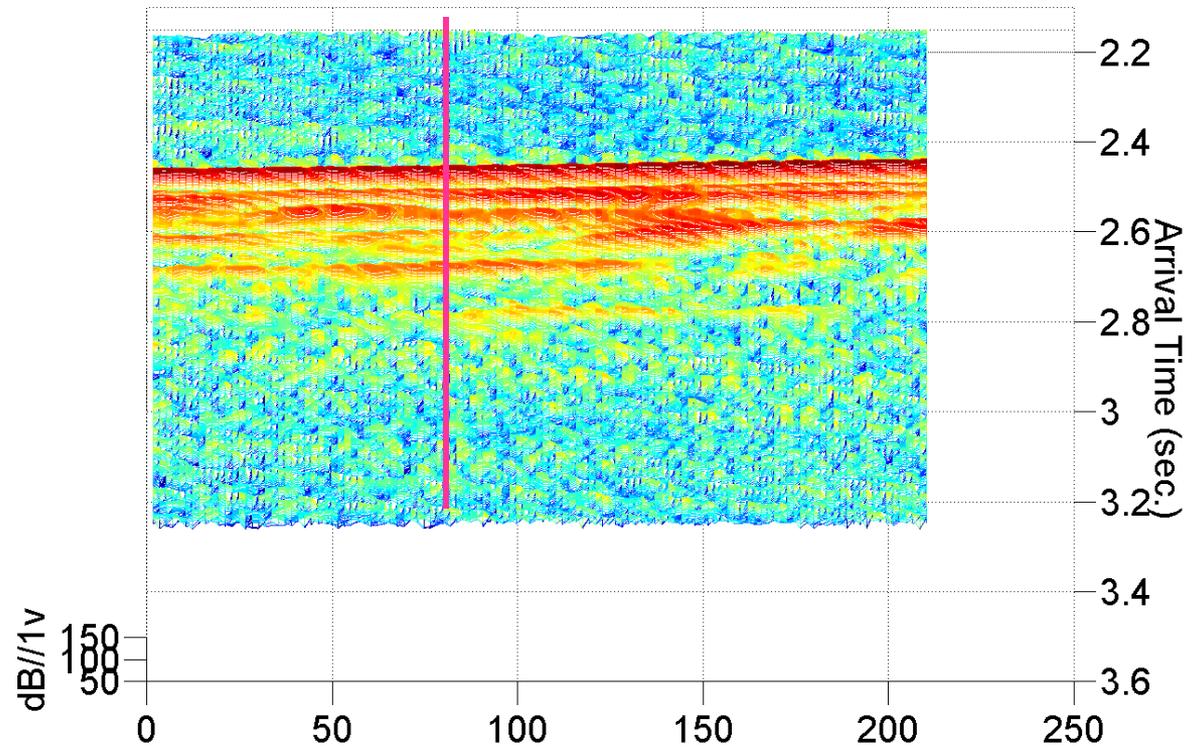
SWAP Station A 250 Hz. M-sequence



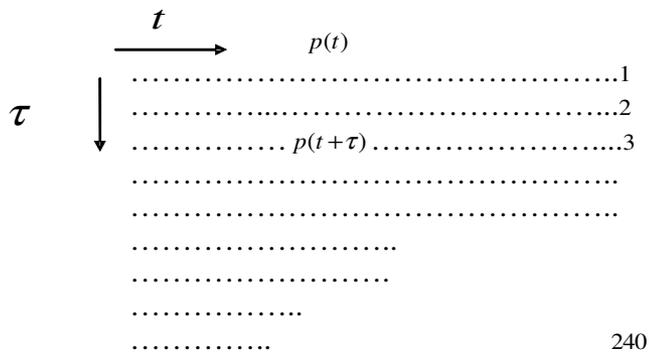


Time slice

Pulse response from 118 phones along the array

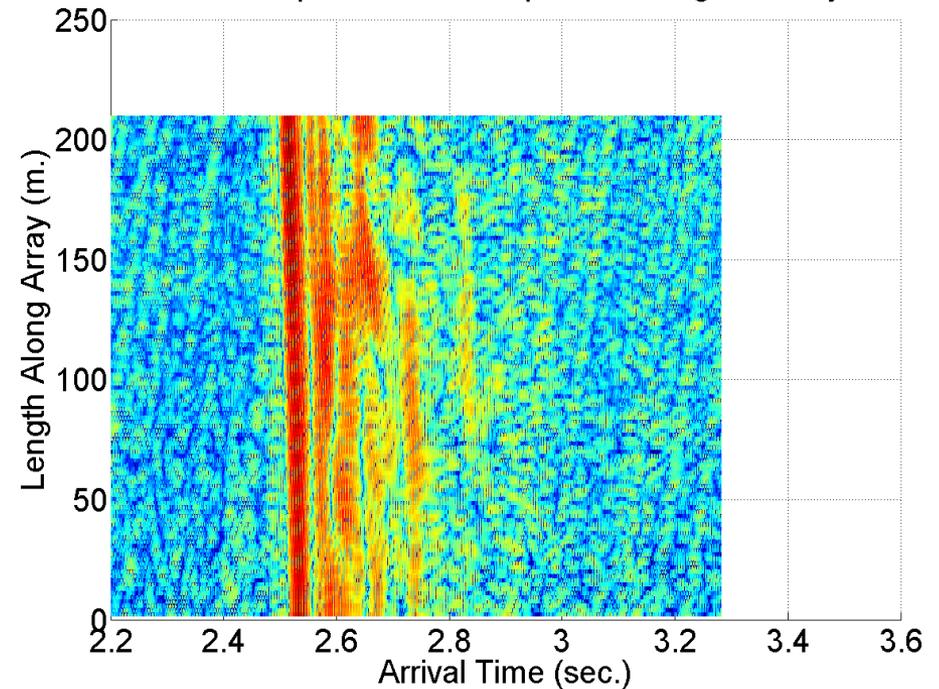


### Signal Amplitude Data



$$COH(t, \tau) = \frac{\langle (p(t) * p(t + \tau))^2 \rangle_{\Delta t, \Delta T}}{\langle p(t)^2 \rangle_{\Delta t, \Delta T} \langle p(t + \tau)^2 \rangle_{\Delta t, \Delta T}}$$

### Pulse response from 118 phones along the array



**Change tau to dx - distance along the array**

Same calculation yields spatial coherence for every arrival of the pulse response!

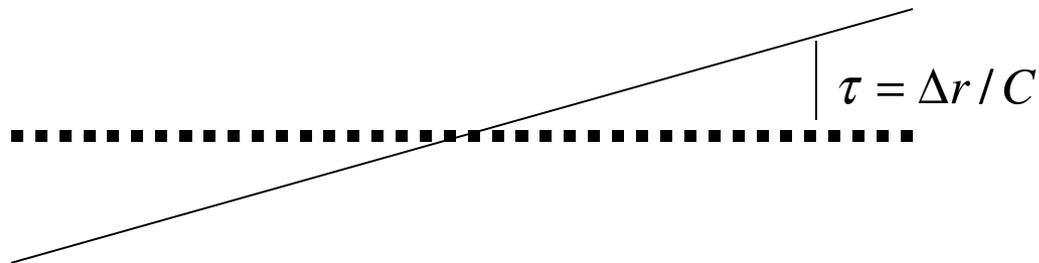
# Steering the Array

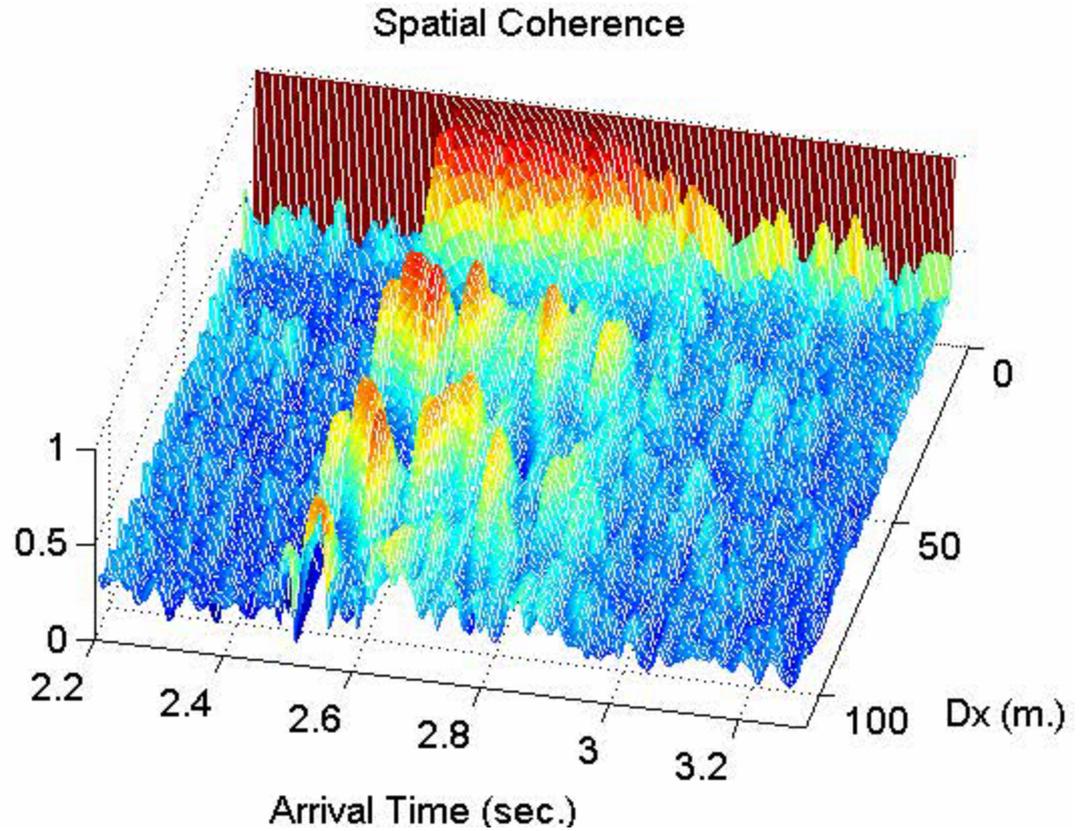
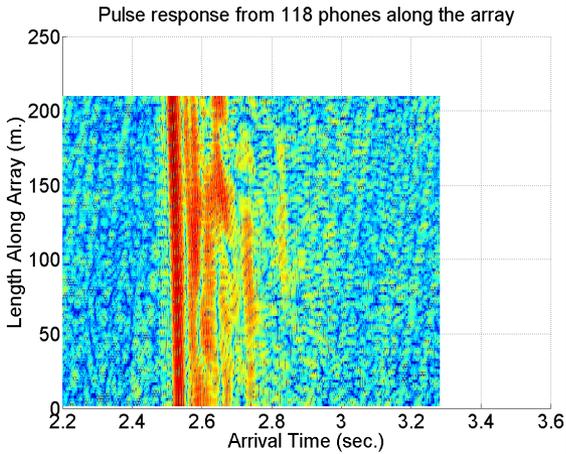
Small shifts in travel time without distortion of the waveform

→ Fourier Time Shifting Theorem ←

$$p(t) \quad \Rightarrow FT \Rightarrow \quad F(\omega)$$

$$F(\omega)e^{i\omega\tau} \quad \Rightarrow IFT \Rightarrow \quad p(t-\tau)$$

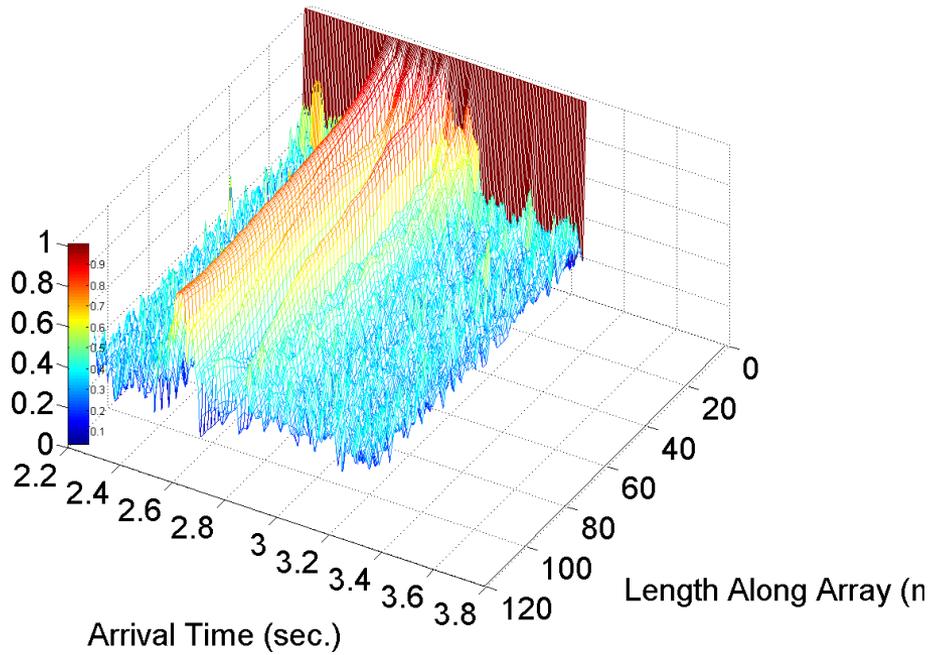




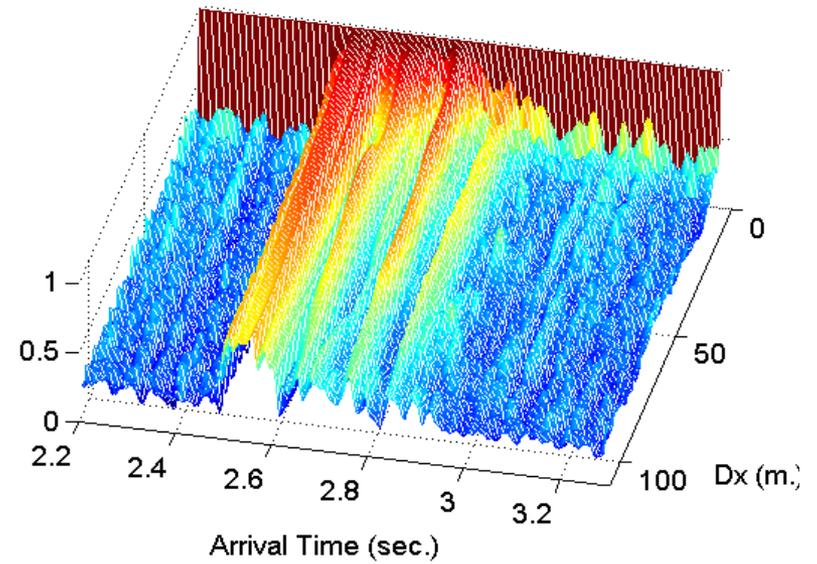
Not aligned with wavefront

Phase changing along the array causing the coherence calculation to cycle.

Spatial Coherence AO 10 km 250 Hz.



Spatial Coherence

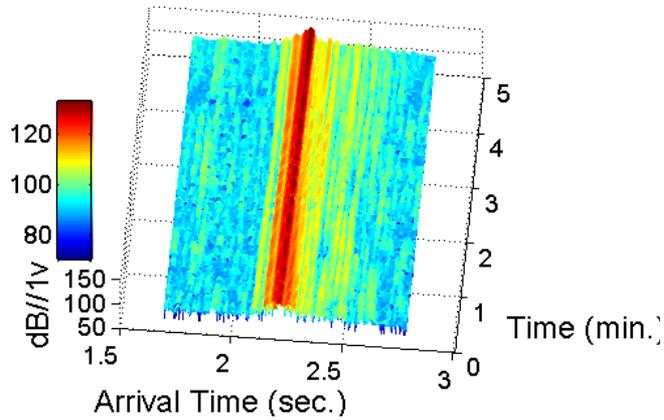


1. Lower order modes are more spatially coherent than higher order modes
2. All modes have *same* angle of arrival

# Winter CALOPS 20 km 302 m Source Depth

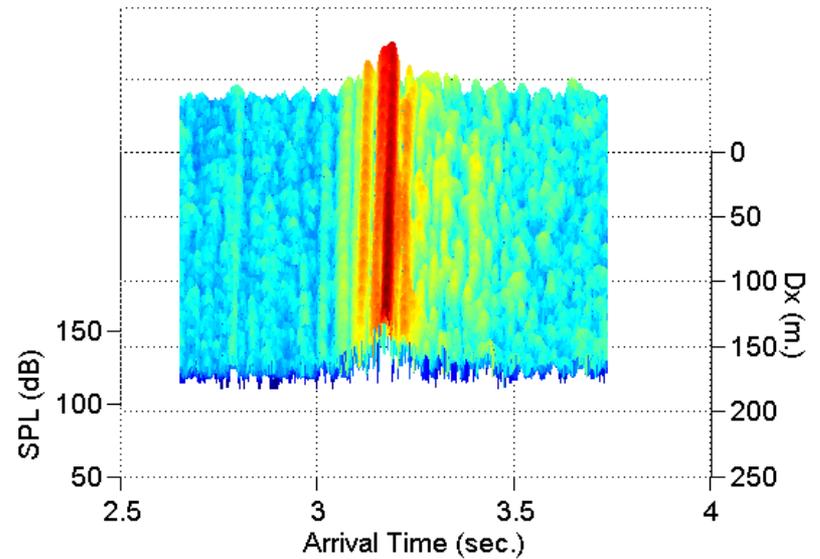
Time

VC St A 20km 250 Hz. M-seq Pluse Arrival vs.Time

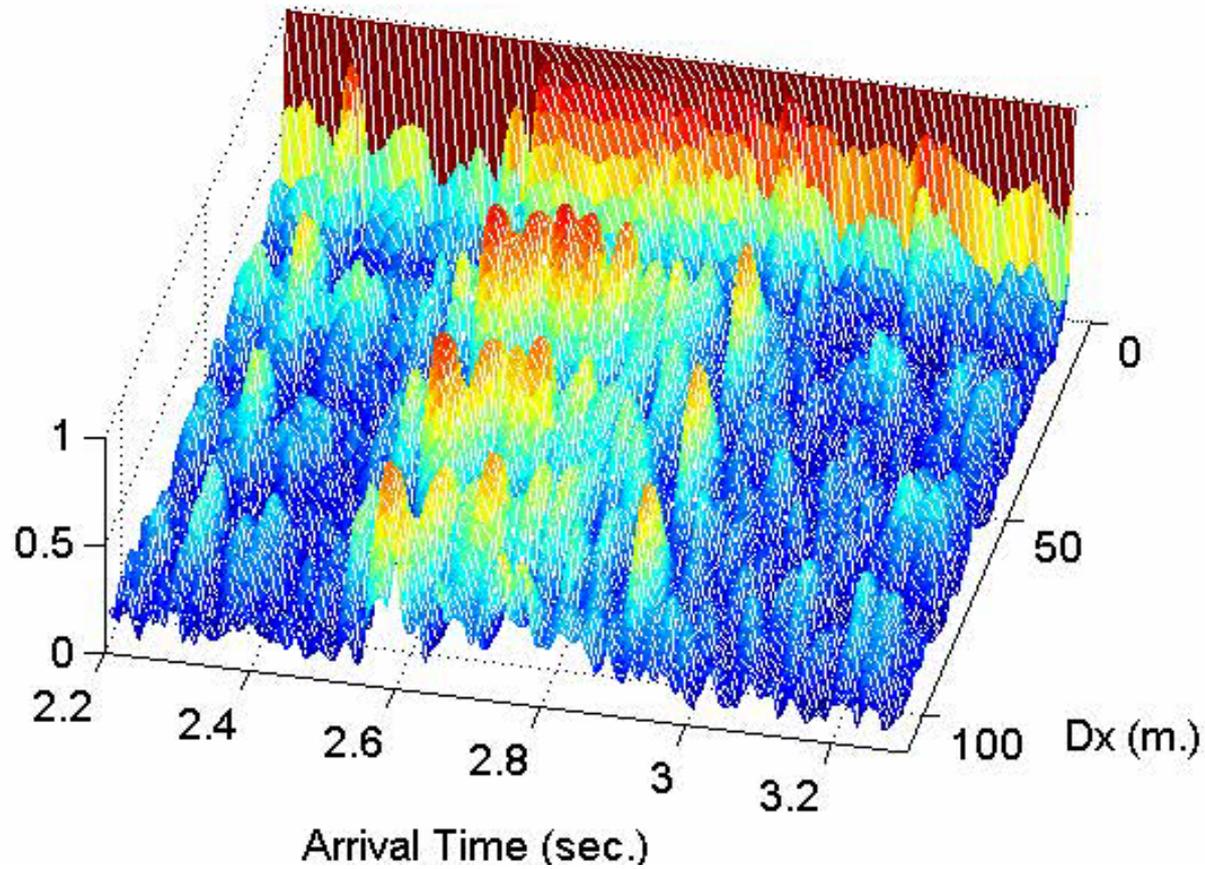


Dx Along array

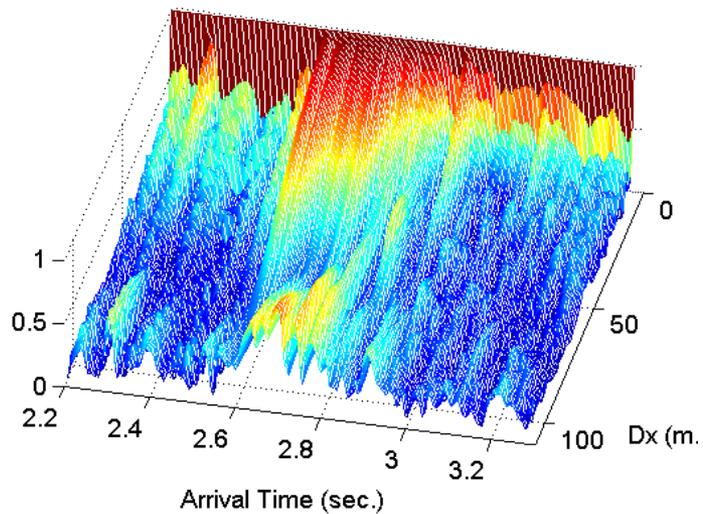
Pulse Response Along Array A1 203m 20 km. 250 Hz



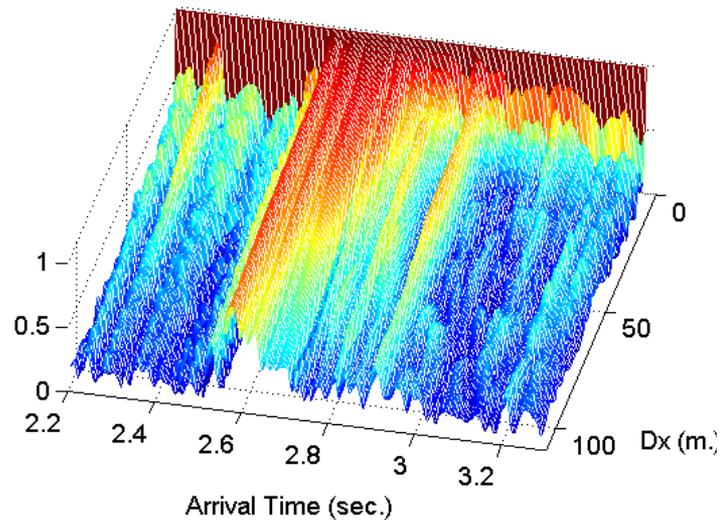
Spatial Coherence A1 203m 20 km 250 Hz



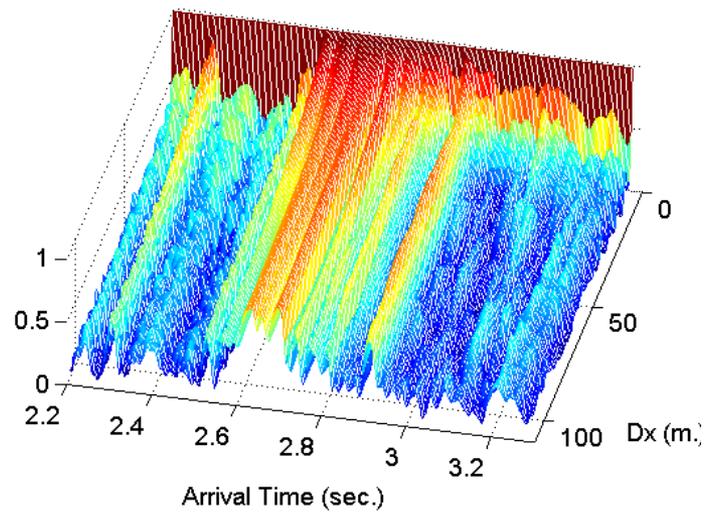
Spatial Coherence A1 203m 20 km 250 Hz



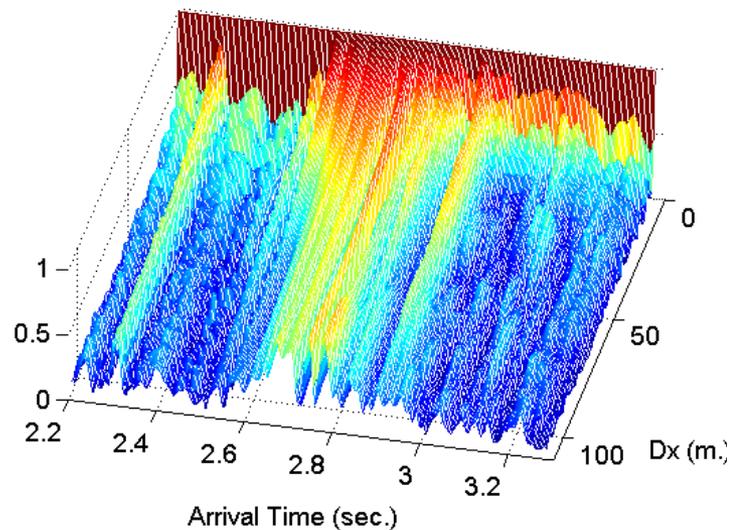
Spatial Coherence A1 203m 20 km 250 Hz



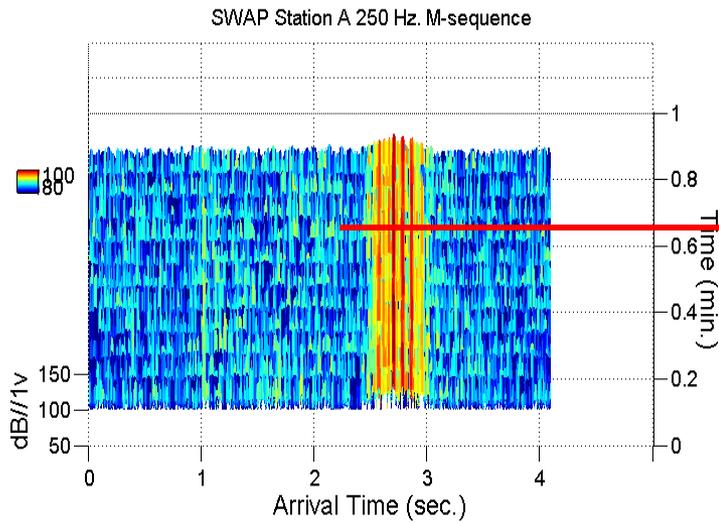
Spatial Coherence A1 203m 20 km 250 Hz



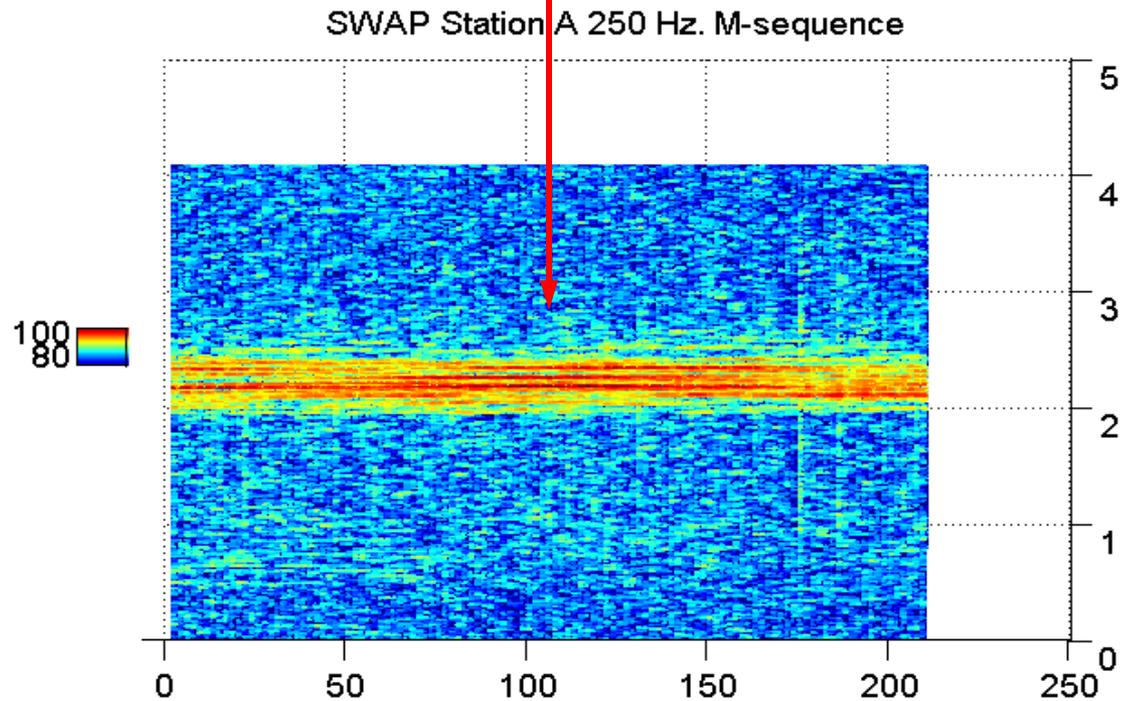
Spatial Coherence A1 203m 20 km 250 Hz



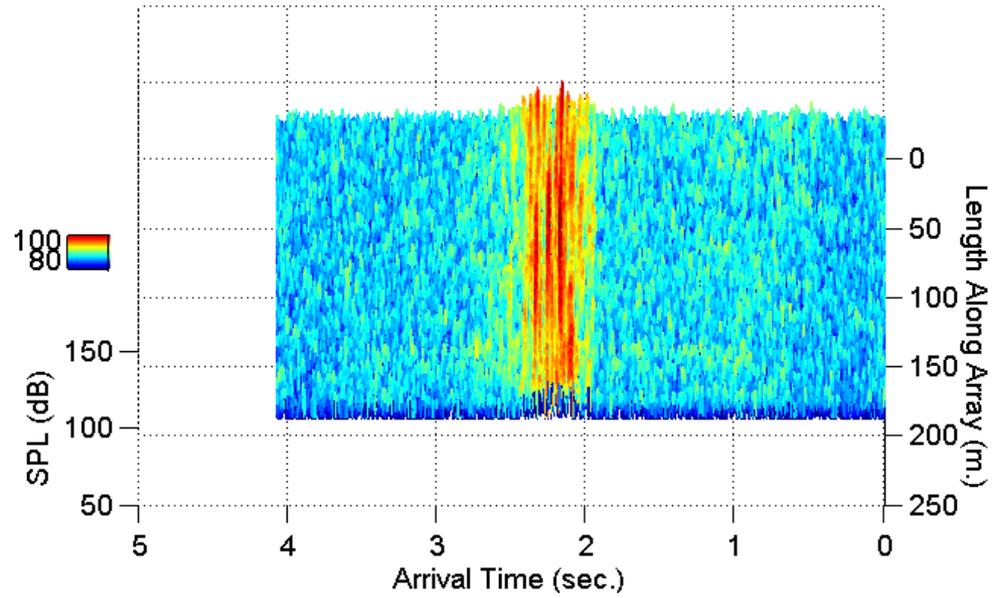
# 80 km m-sequence reception



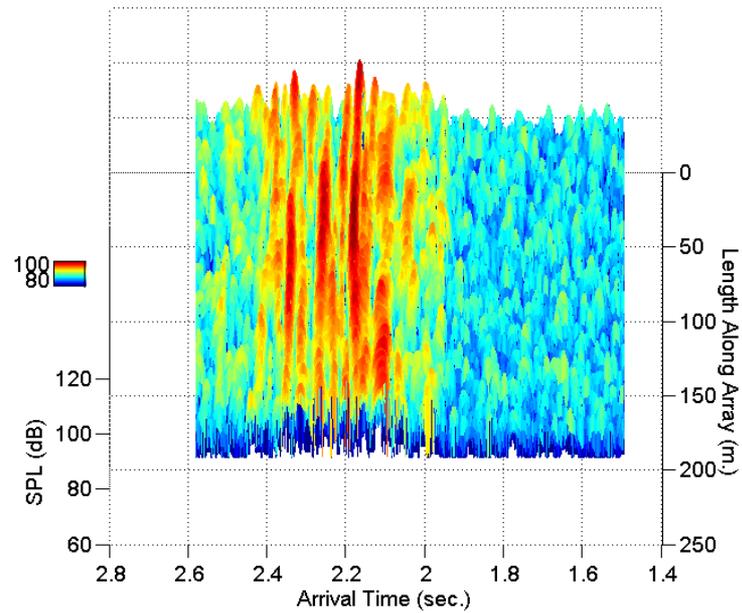
Time slice



SWAP Station A 250 Hz. M-sequence

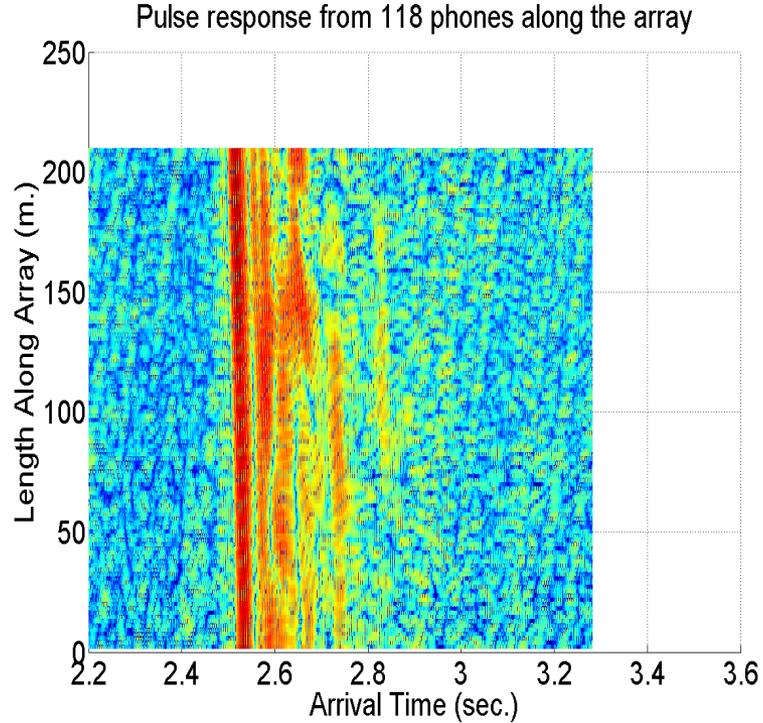


SWAP Station B 80 km 250 Hz. M-sequence

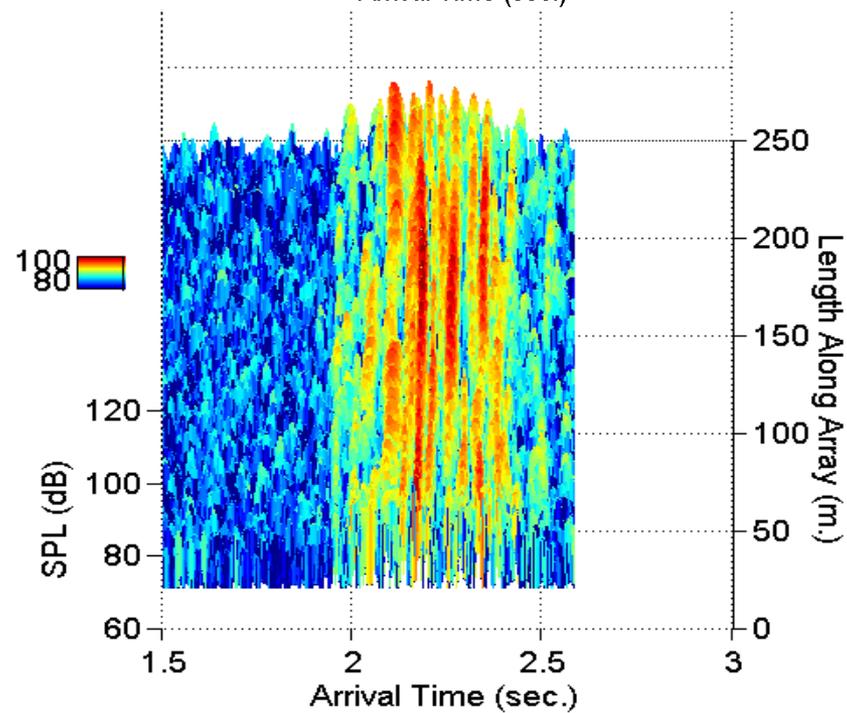




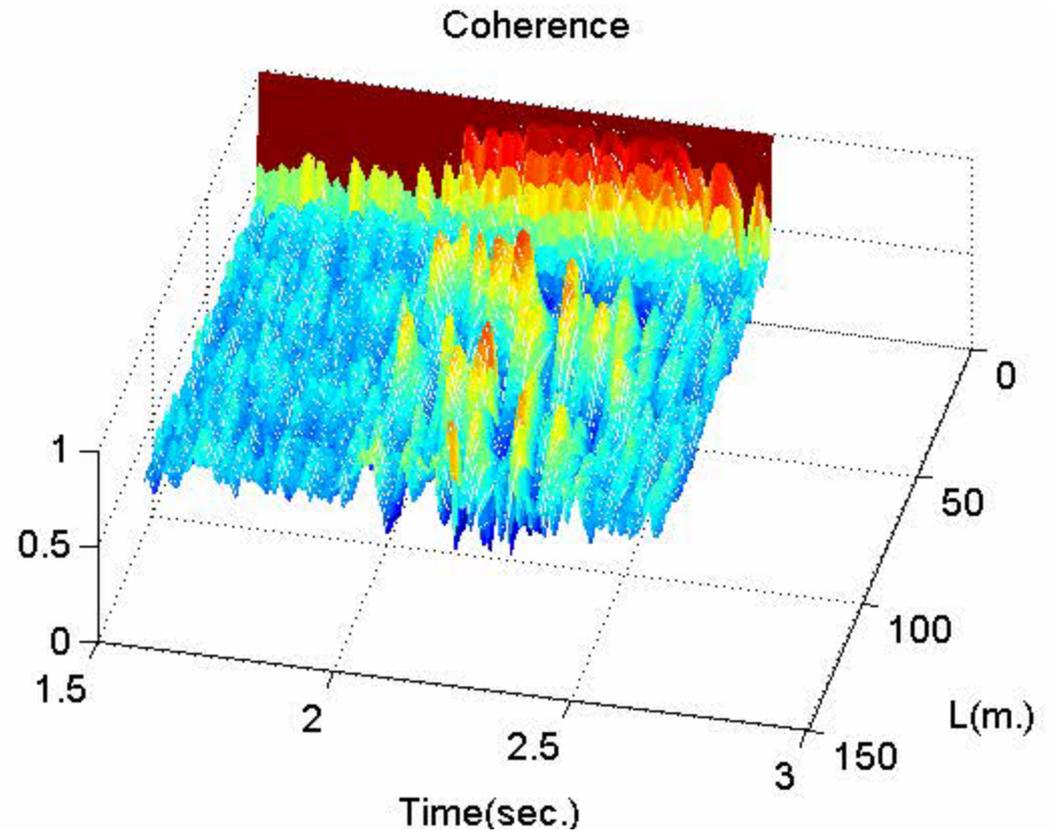
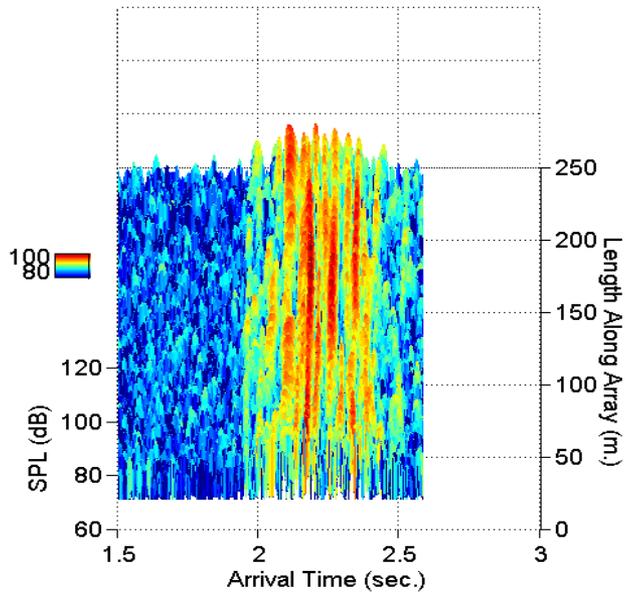
10 km



80 km



SWAP Station B 80 km 250 Hz. M-sequence



1. No recognizable modal structure
2. Burst of micro-paths
3. Different angles of arrival

# Spatial Coherence

Higher order modes less coherent than lower order

Modes have varying arrival angles (horizontal)

Angular spread (horizontal) depends on range

<1 deg. @ 10 km

< 2 deg. 20 km

< 4-6 deg. 80 km

# Publications

1. Observations of Low-Frequency Temporal and Spatial Coherence in Shallow water. DeFerrari.  
Topic -- FSPE and AO data analysis of spatial and temporal coherence  
Status – Submitted
  
5. Temporal Coherence of Mode Arrivals. DeFerrari, Lynch, Newhall.  
Topic -- MSM to SHRU's transmission data analysis - temporal coherence  
Status – Submitted
  
9. Spatial Coherence of Mode arrivals. DeFerrari, Colis, Duda, Newhall  
Topic -- MSM to Shark - Coherence of mode arrivals.  
Status – Early draft.
  
13. Acoustic Propagation on Shallow Shelves Inside of Retrograde and Progade Fronts.  
Topic -- Comparison of internal wave fields and effects of propagation for two types of environments.
  
5. Limitations of Horizontal Coherence in Shallow Water.

