

# Observations of out of plane arrivals for long range low frequency transmission in shallow water

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## **Out of (vertical) plane mode arrivals.**

- 3. Large angle Fermat paths from inshore slopes.**
- 4. Small angle discrepancies for mode groupings.**
- 5. Speculate on the influence on temporal and spatial coherence.**

**Unique high s/n data out to 80 km!**

## Florida Straits Propagation Experiments

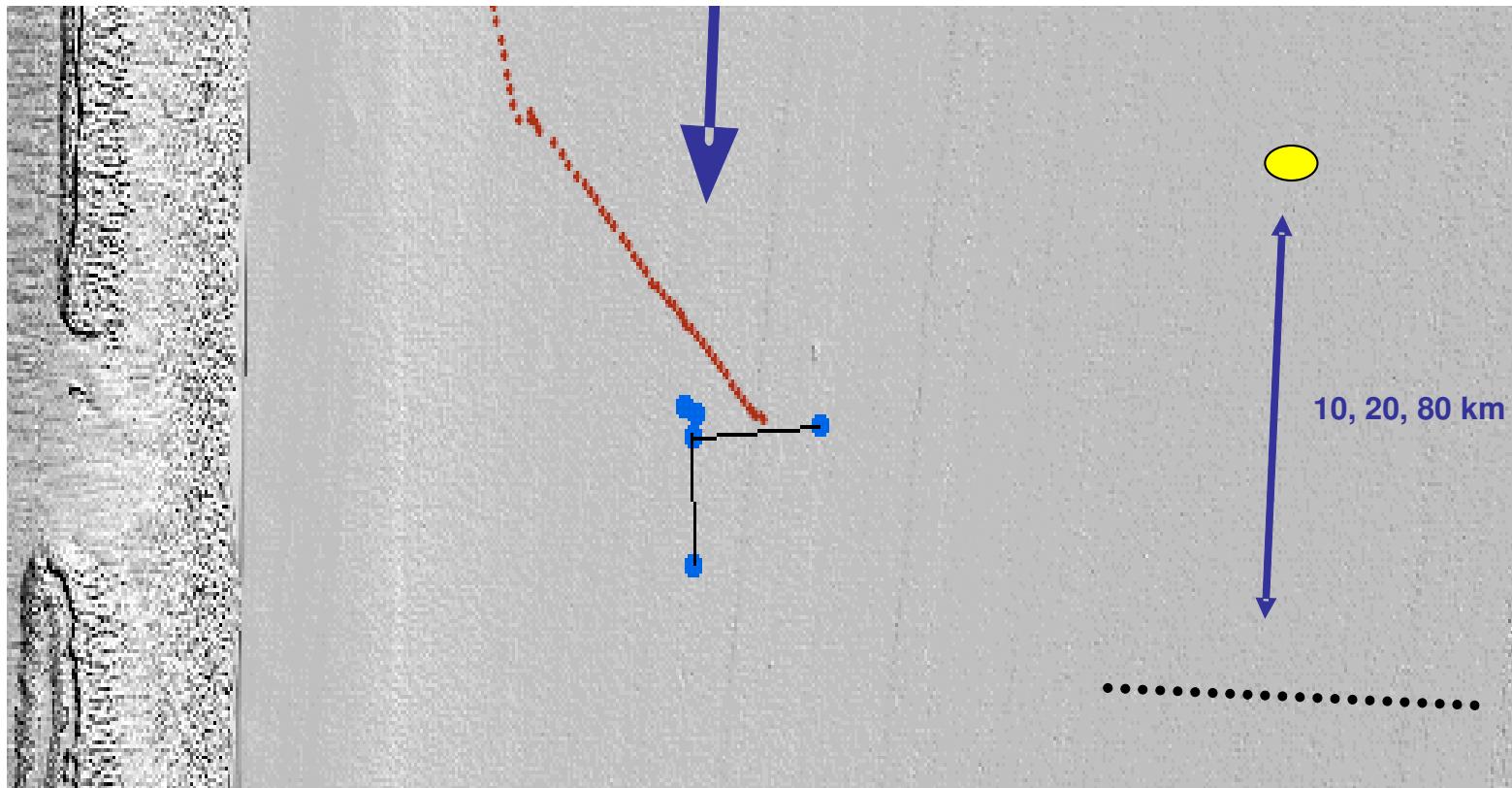
Jan 99, 01 145 m.

Moored Source

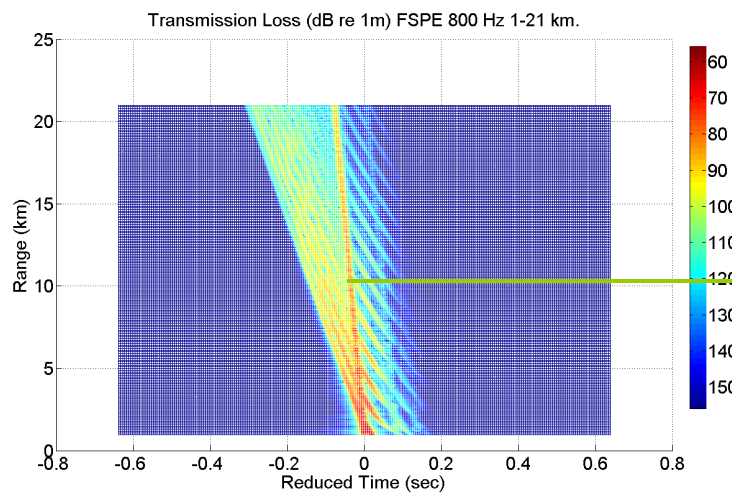
## SWAP CALOPS

Sept 07 230 m.

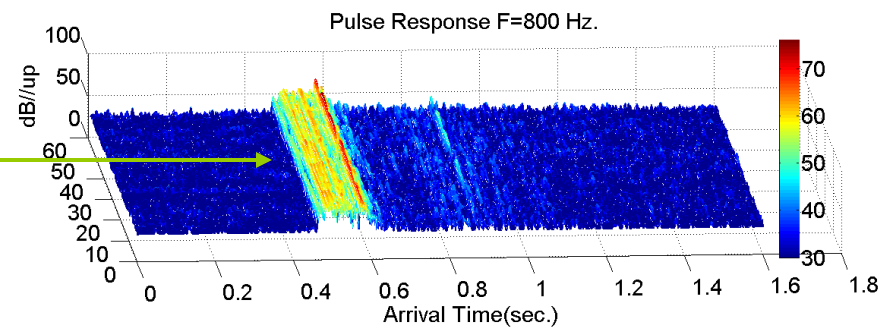
Shipboard Suspended Source



## PE Prediction of 800 Hz. Pulse Response



## Measured - 1 Hour





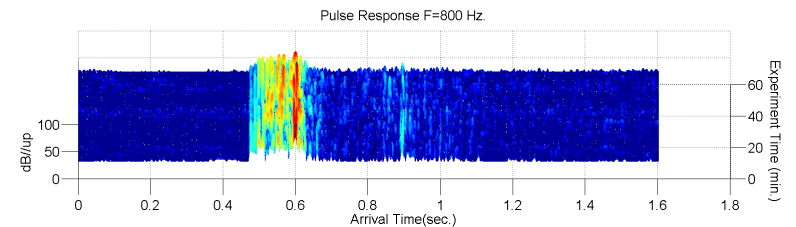
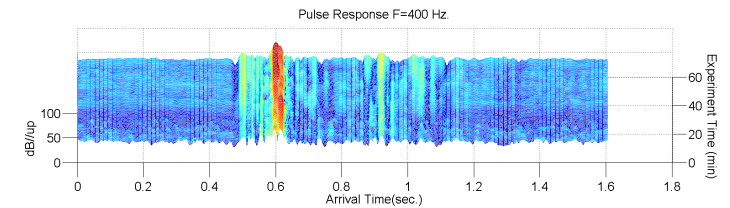
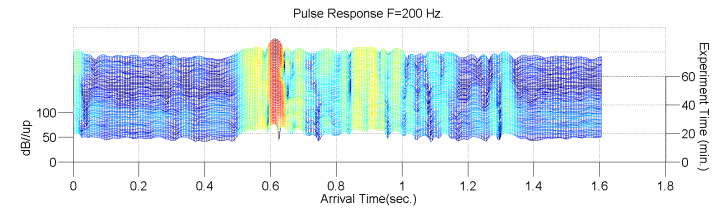
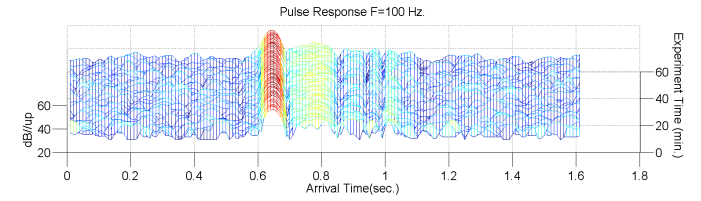
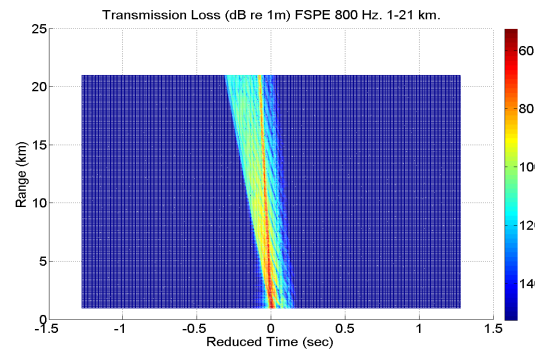
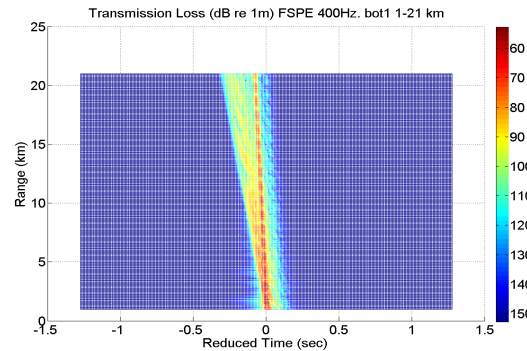
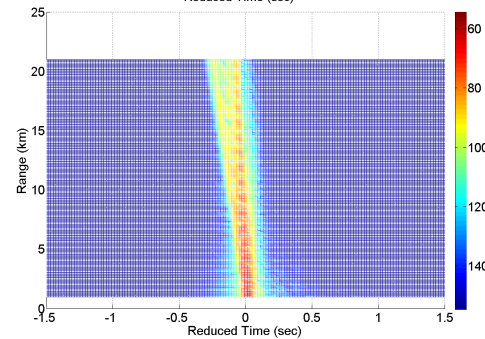
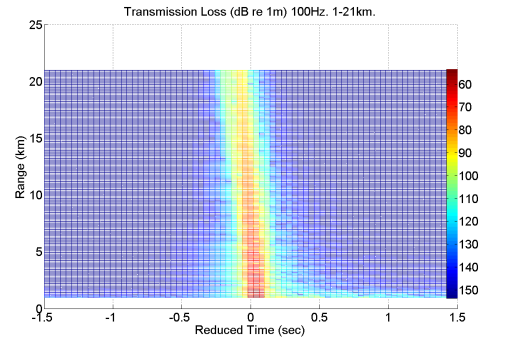
# Florida Straits Propagation Experiments

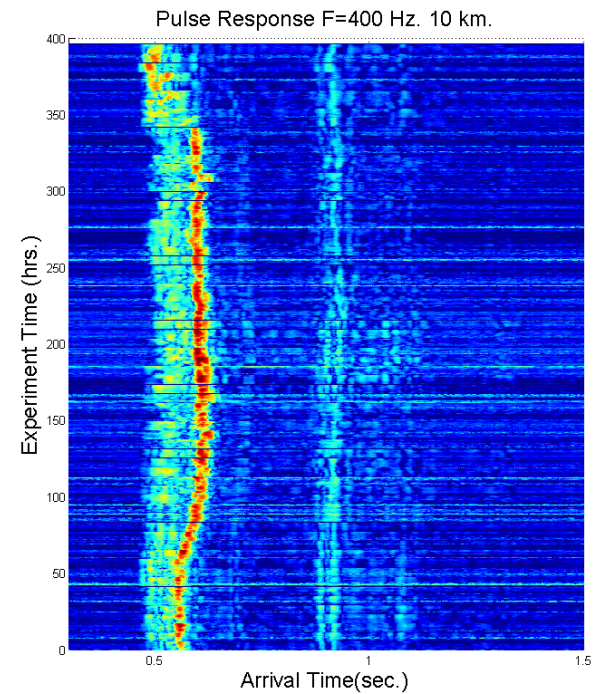
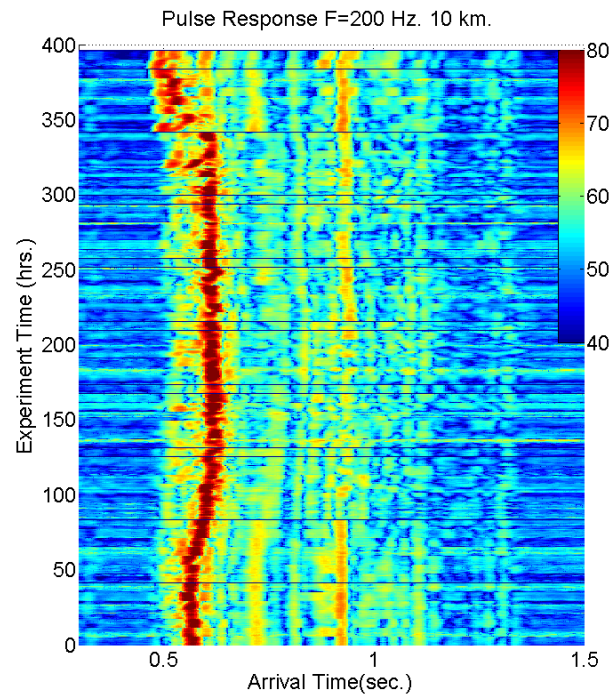
## Frequency Dependence Model < > Measurements

### FSPE

10 km range - f/100 RBR/SRBR modes

- 8 RBR and 8 SRBR @800Hz.
- 4 RBR and 4 SRBR @400 Hz.
- >
- 1 total @50 Hz.



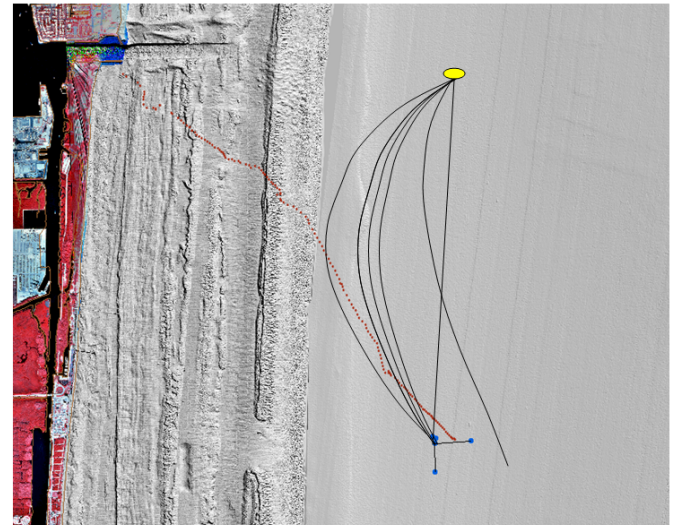


## Out of Plane Arrivals

Harry DeFerrari – San Diego ASA tried layer bottom and shear.

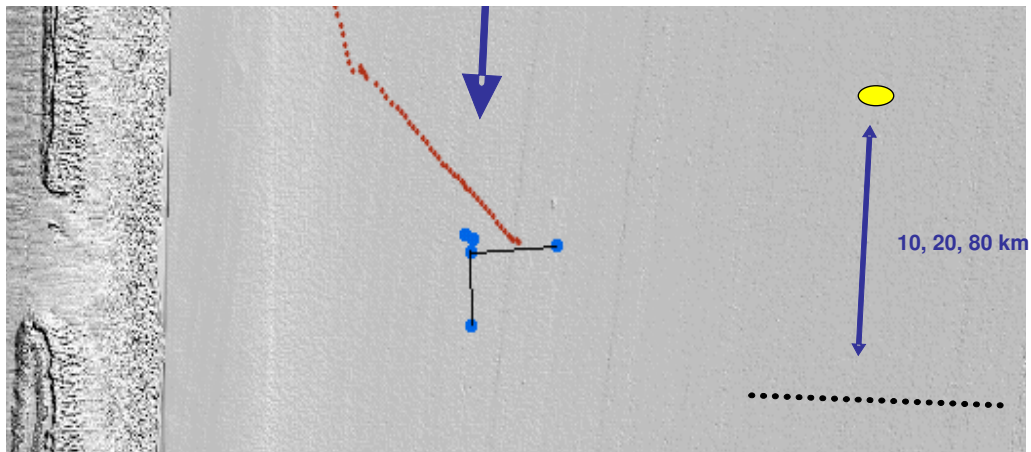
Ross Chapman - Multiple reflections from a sloping bottom turns a ray back to the receiver.

Kevin Smith - 3-D Eigenray problem model



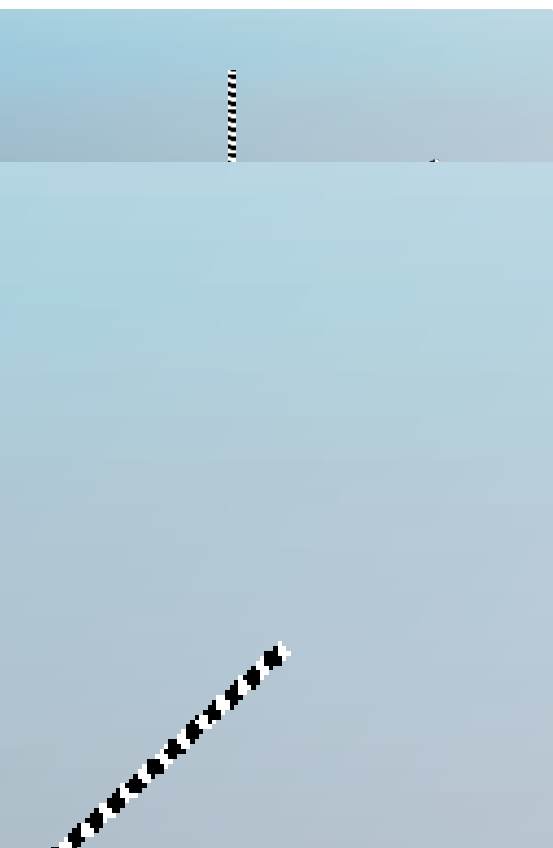




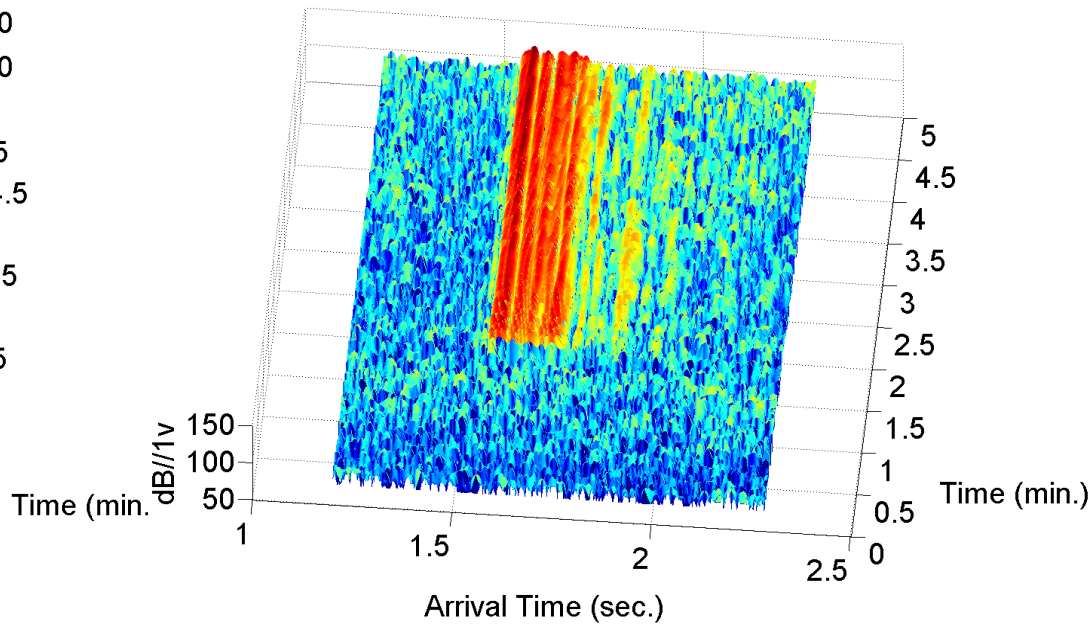
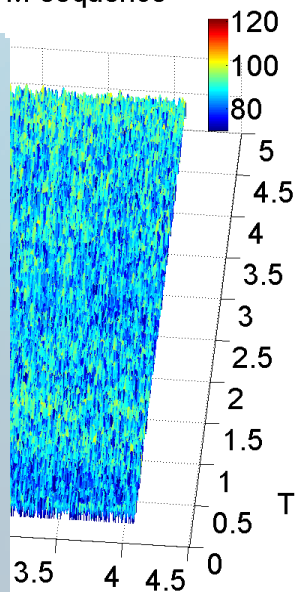


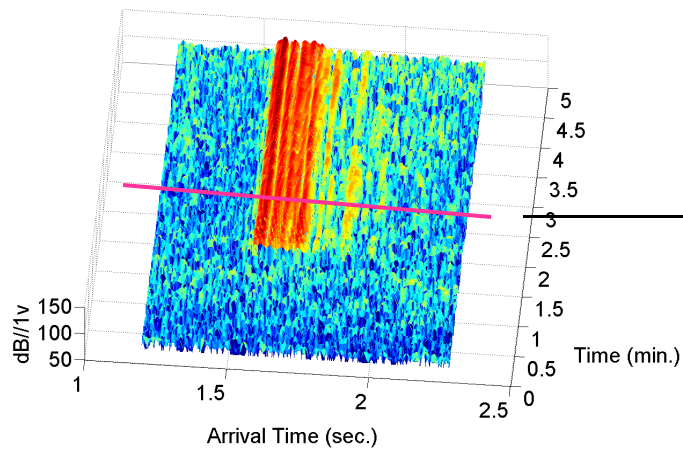
# Acoustic Observatory Receiving Arrays CALOPS Sept 07 Shipboard Suspended and Towed Transmissions

## 10 km data



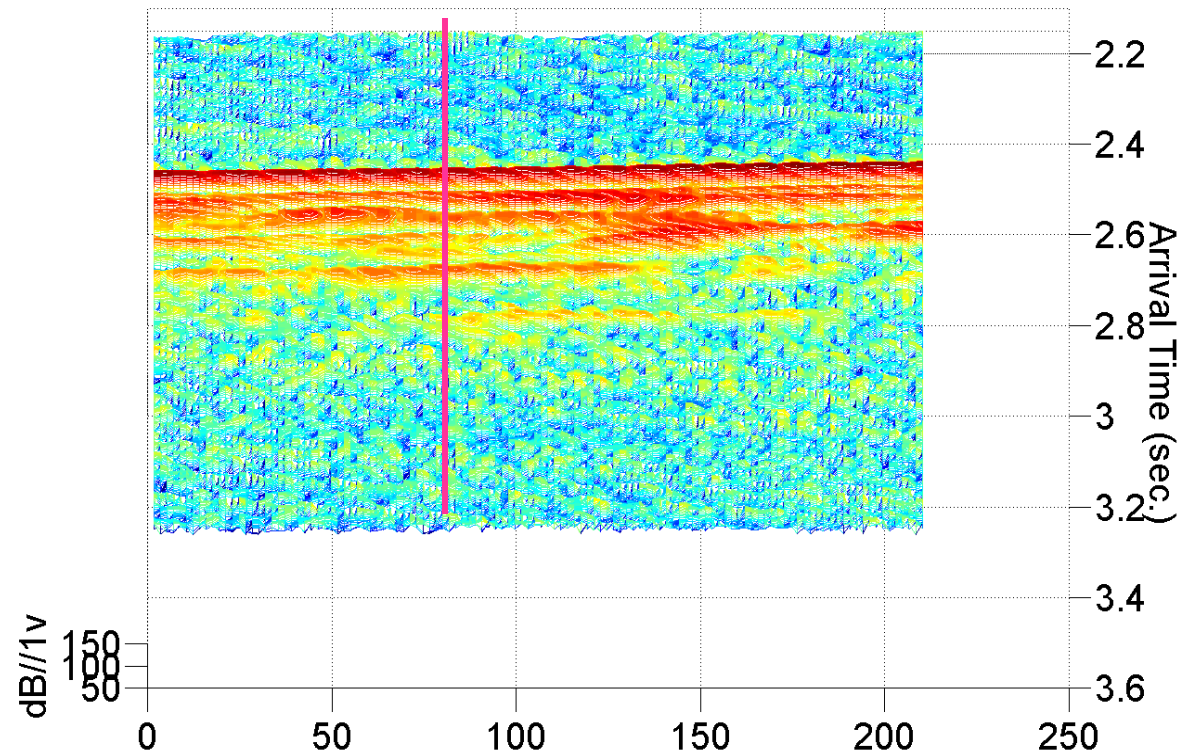
M-sequence



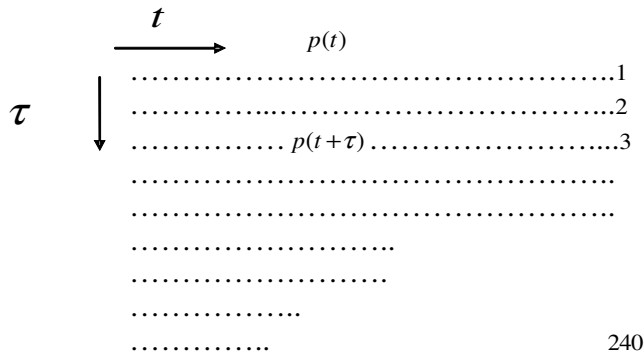


Time slice

Pulse response from 118 phones along the array

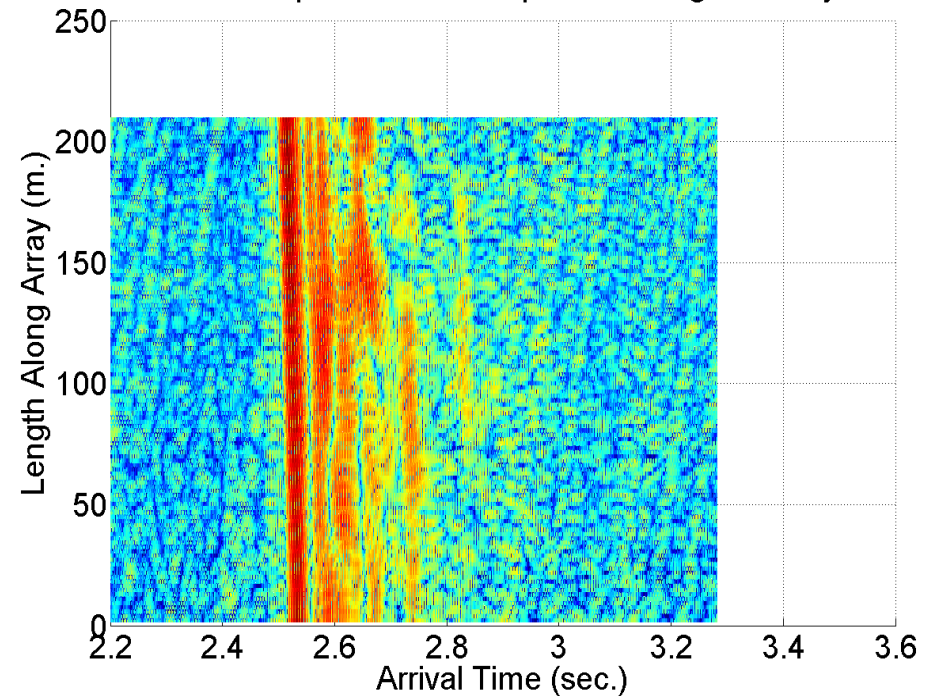


Signal Amplitude Data



$$COH(t, \tau) = \frac{\langle (p(t) * p(t + \tau))^2 \rangle_{\Delta t, \Delta T}}{\langle p(t)^2 \rangle_{\Delta t, \Delta T} \langle p(t + \tau)^2 \rangle_{\Delta t, \Delta T}}$$

Pulse response from 118 phones along the array



**Change tau to dx - distance along the array**

Same calculation yields spatial coherence for every arrival of the pulse response!

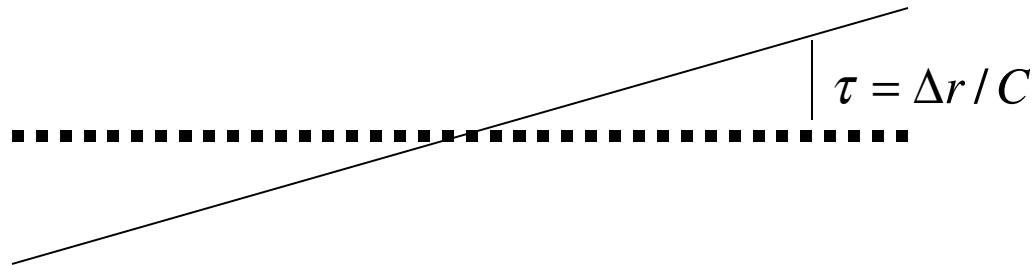
# Steering the Array

Small shifts in travel time without distortion of the waveform

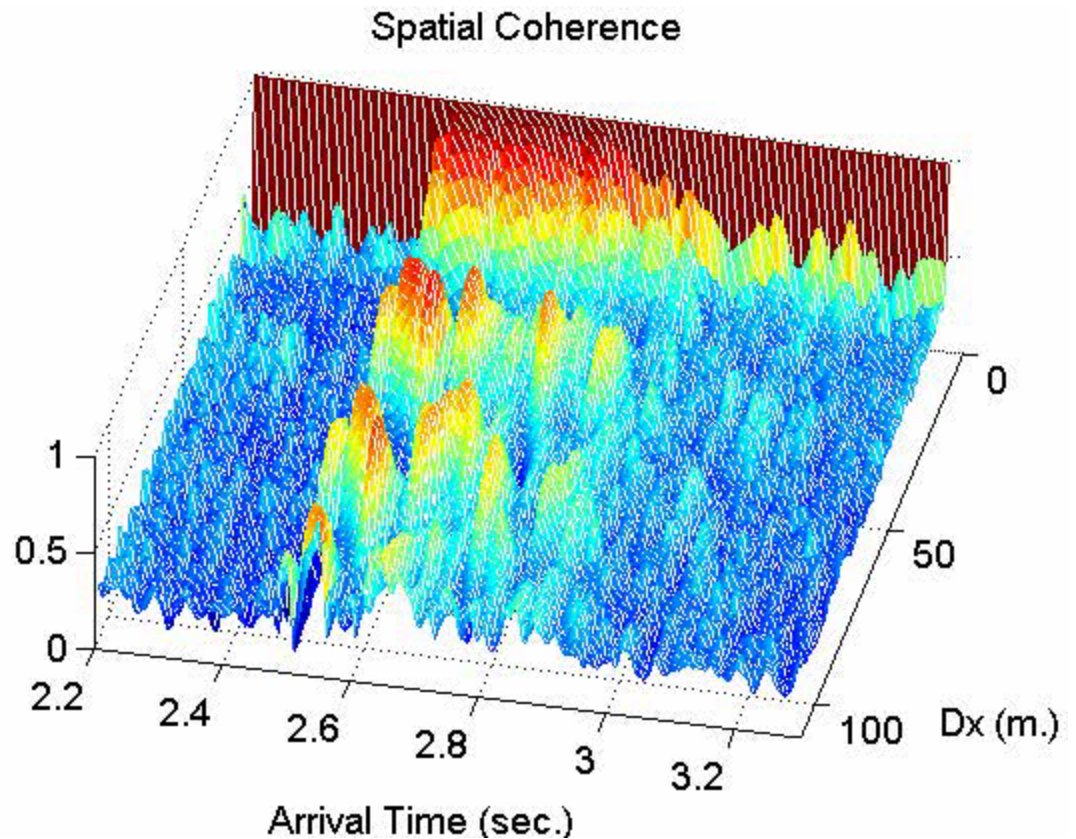
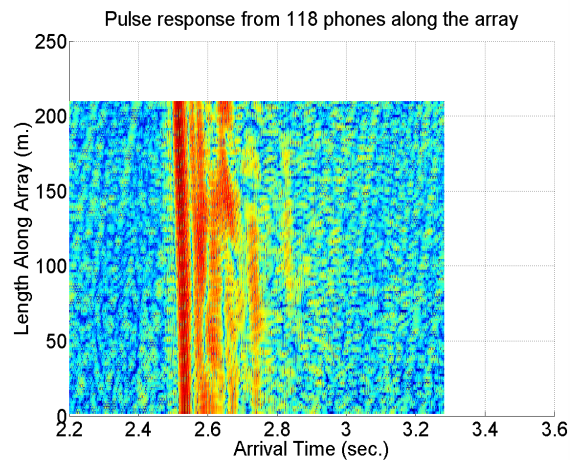
→ Fourier Time Shifting Theorem ←

$$p(t) \quad \Rightarrow FT \Rightarrow F(\omega)$$

$$F(\omega)e^{i\omega\tau} \quad \Rightarrow IFT \Rightarrow p(t-\tau)$$





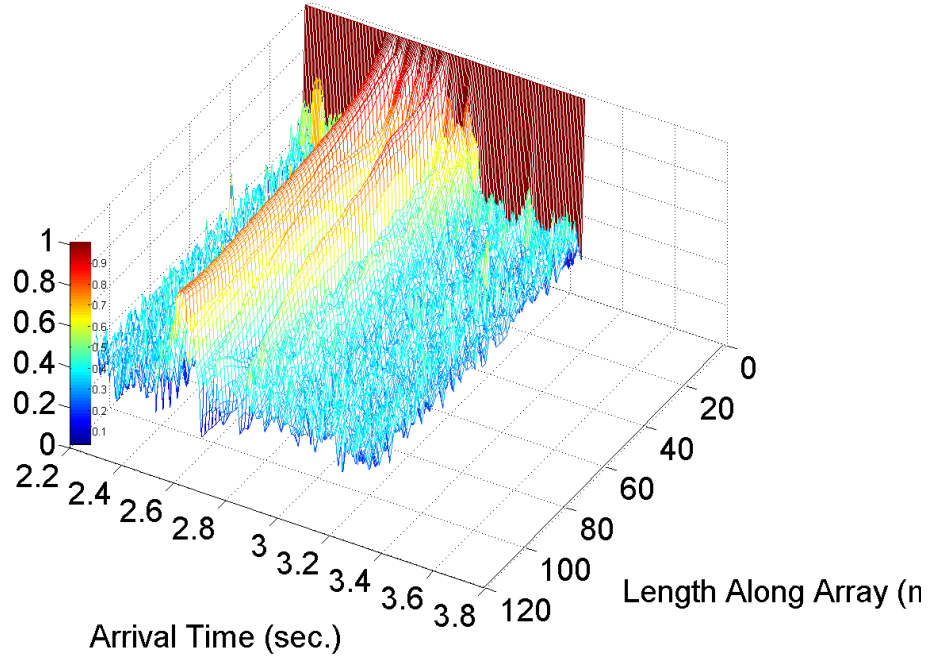


Not aligned with wavefront

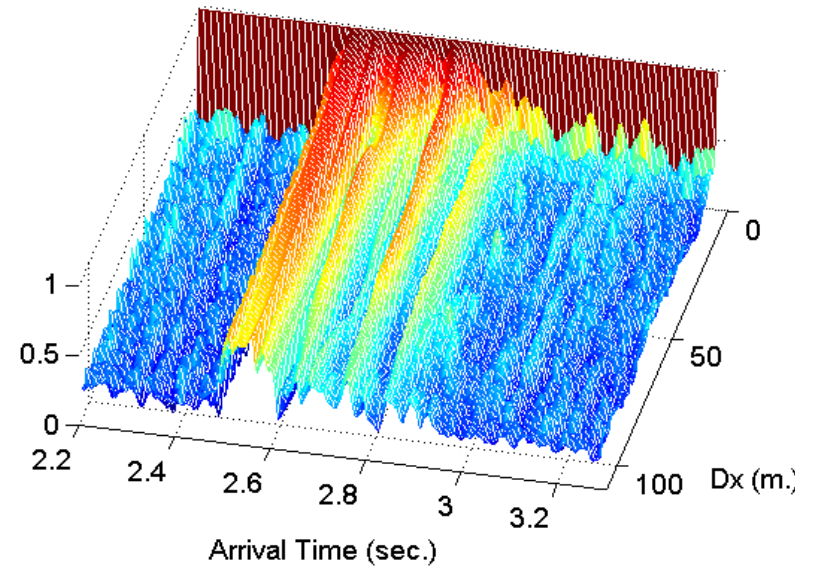
Phase changing along the array causing the coherence calculation to cycle.



Spatial Coherence AO 10 km 250 Hz.

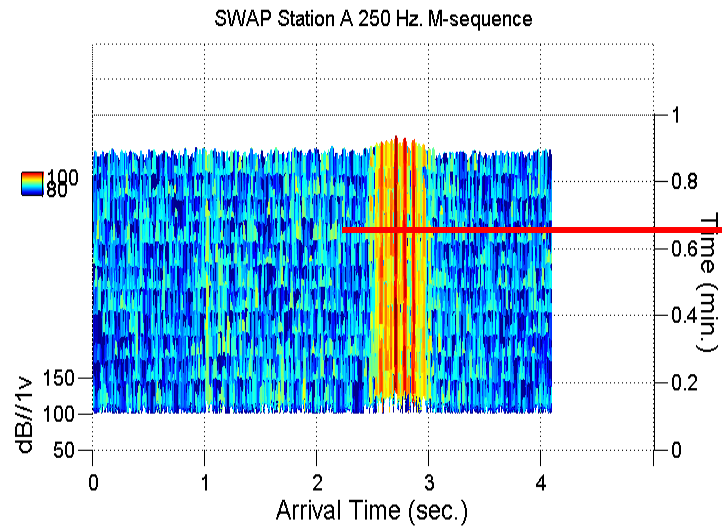


Spatial Coherence

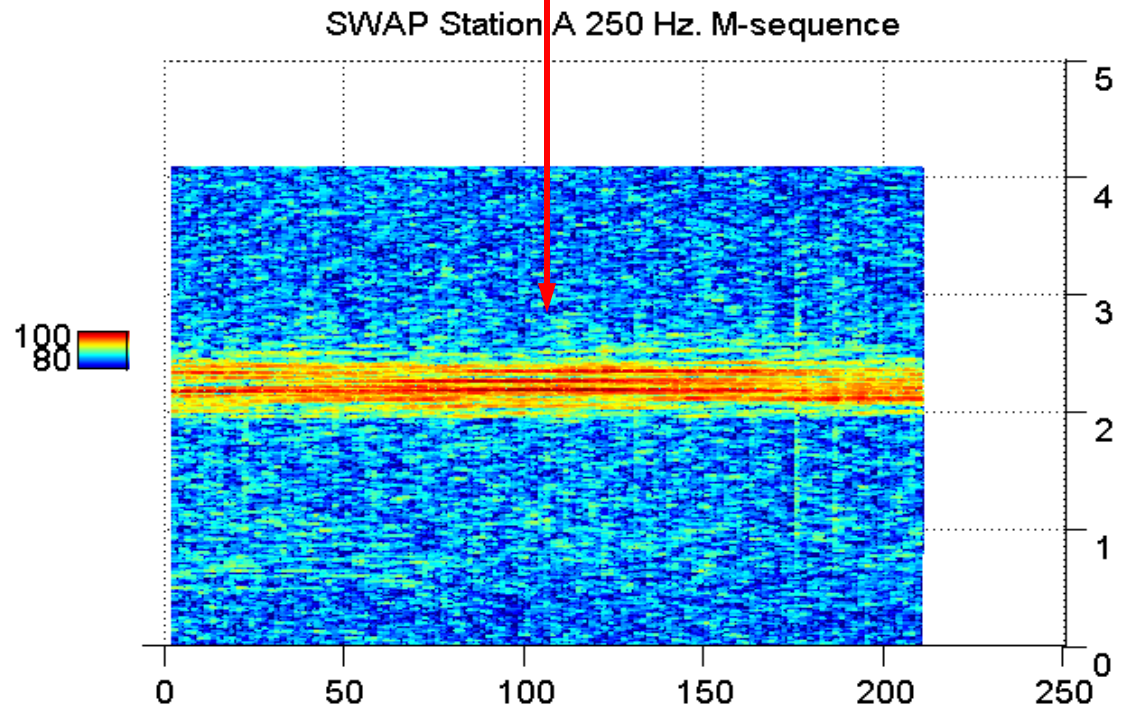


1. Lower order modes are more spatially coherent than higher order modes
2. All modes have **same** angle of arrival

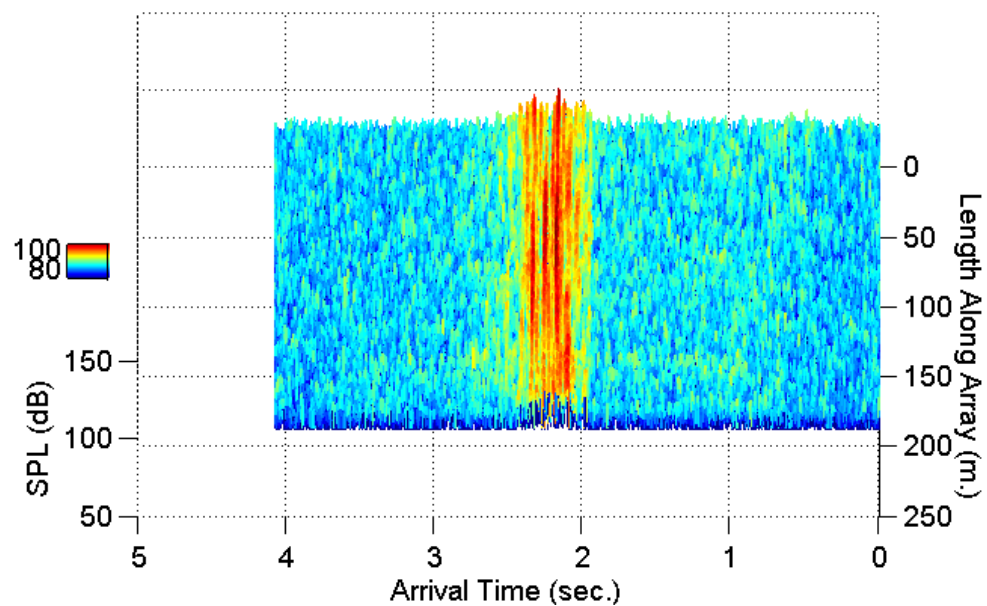
# 80 km m-sequence reception



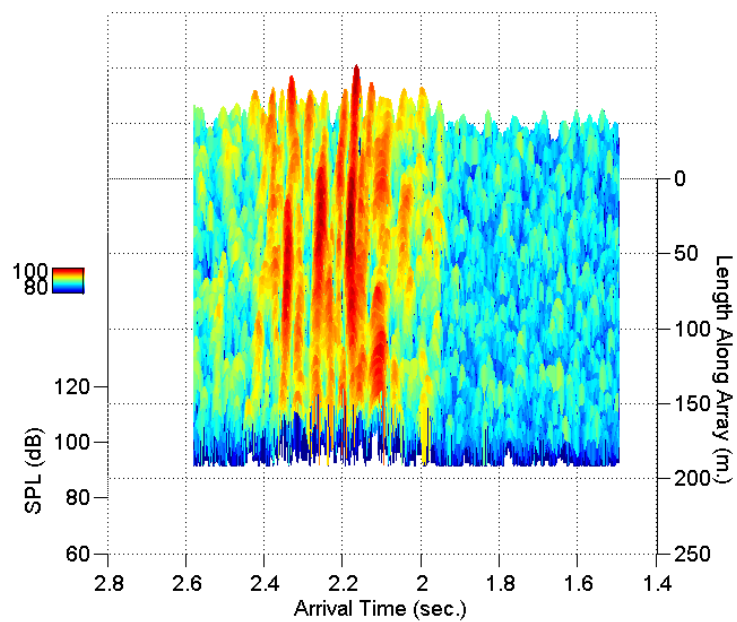
Time slice



SWAP Station A 250 Hz. M-sequence

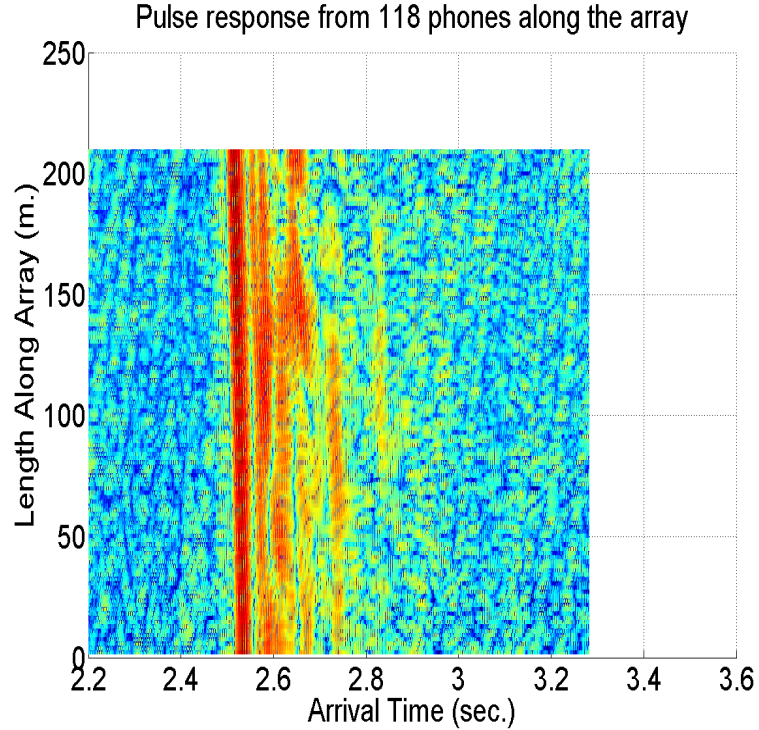


SWAP Station B 80 km 250 Hz. M-sequence

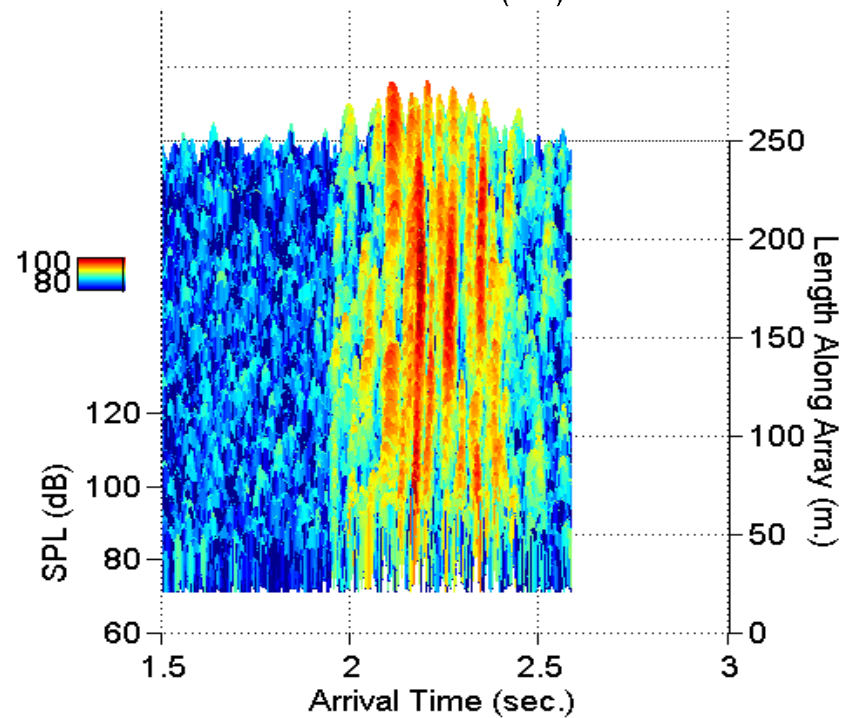


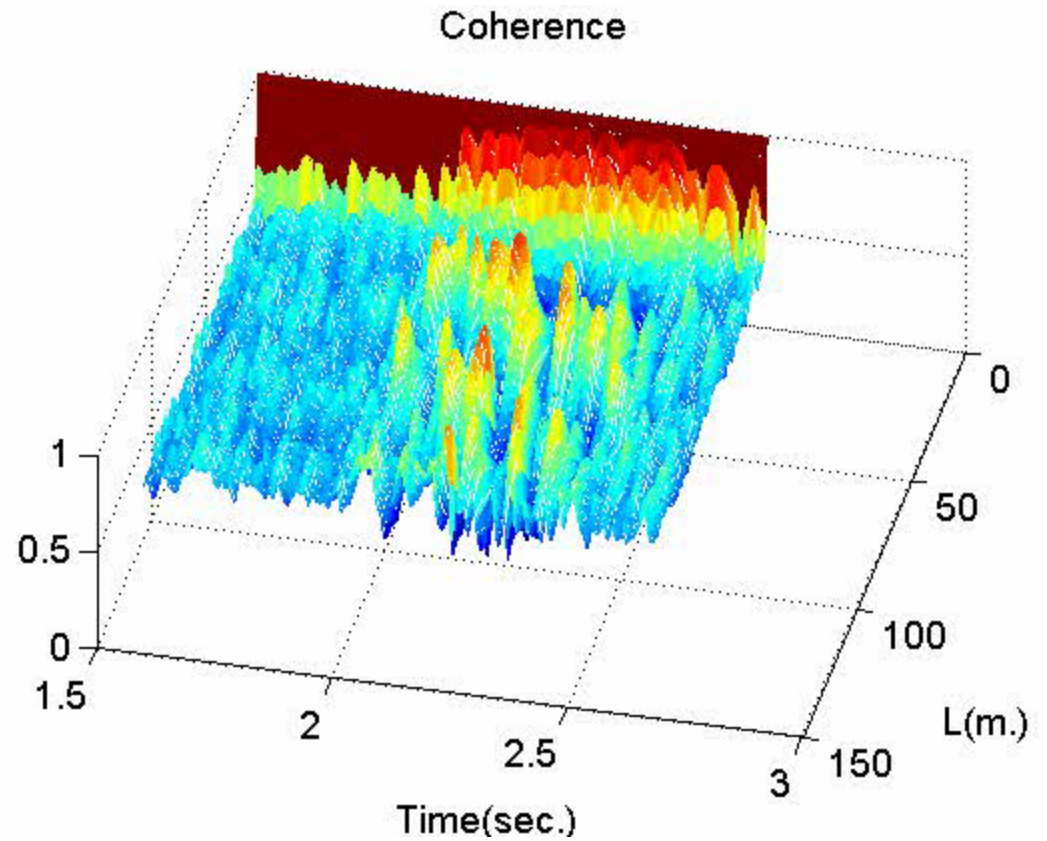
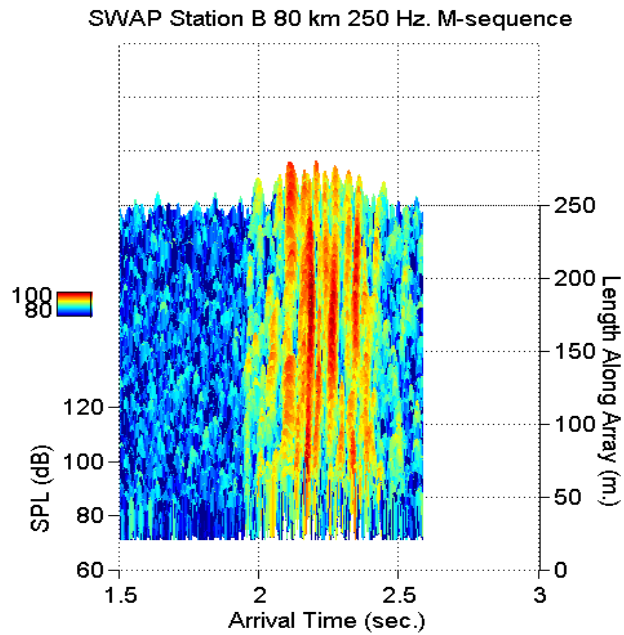


10 km



80 km



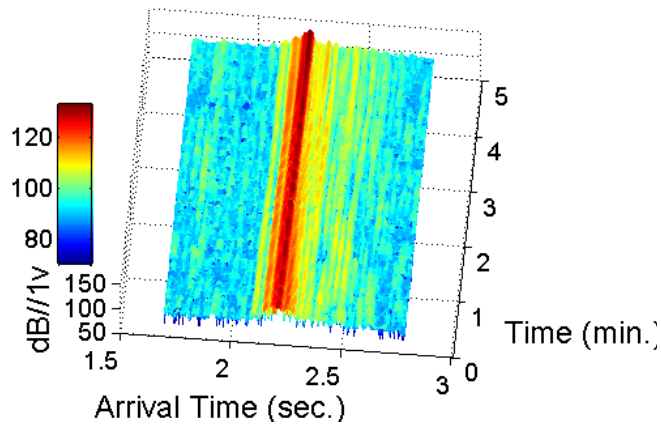


1. No recognizable modal structure
2. Burst of micro-paths
3. Different angles of arrival

## Winter CALOPS 20 km 300 m Source Depth

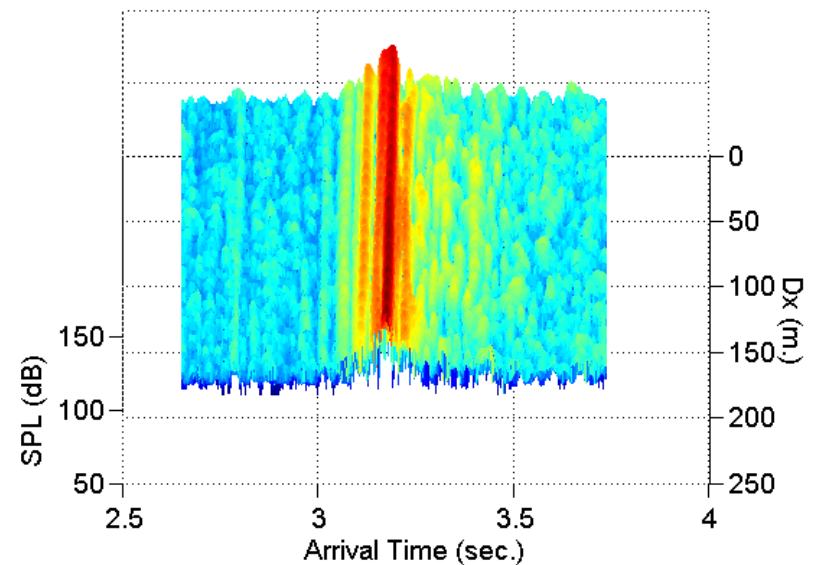
Time

VC St A 20km 250 Hz. M-seq Pluse Arrival vs. Time



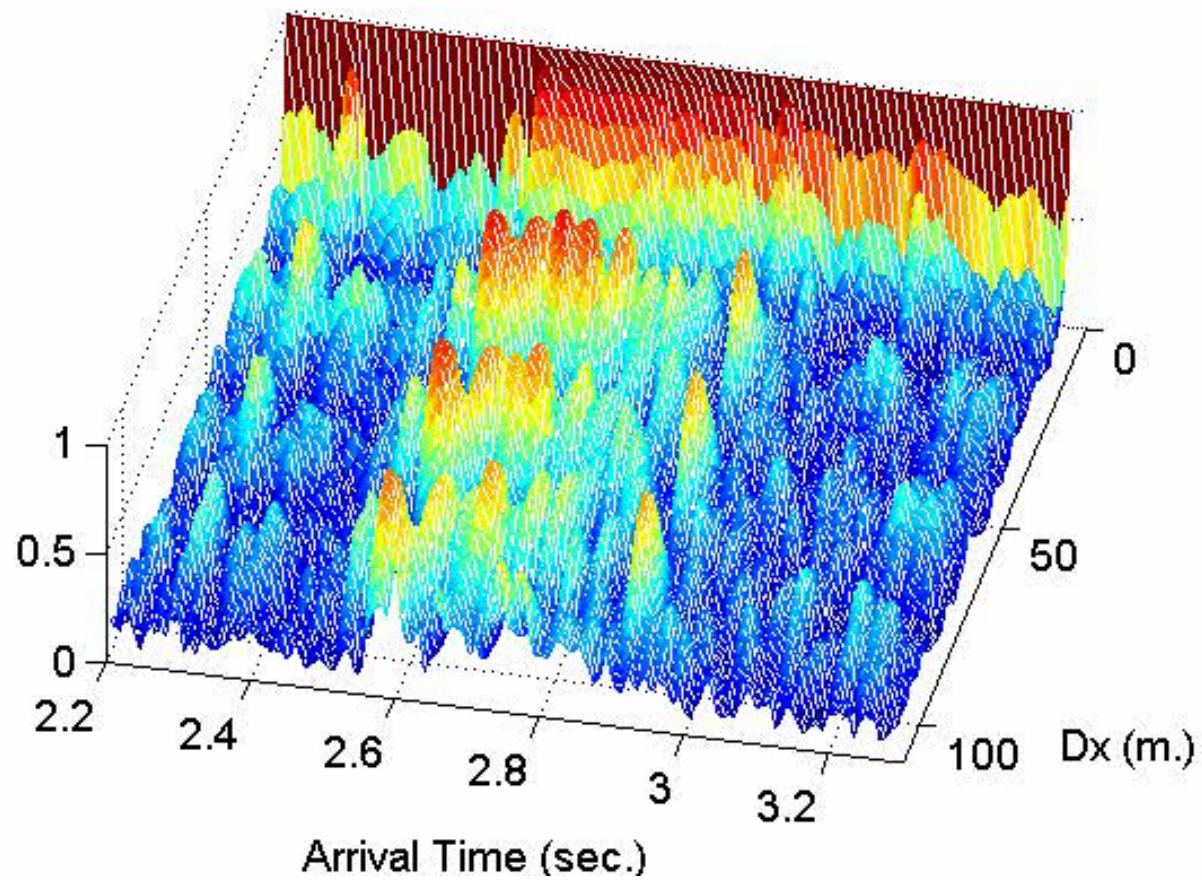
Dx Along array

Pulse Response Along Array A1 203m 20 km. 250 Hz

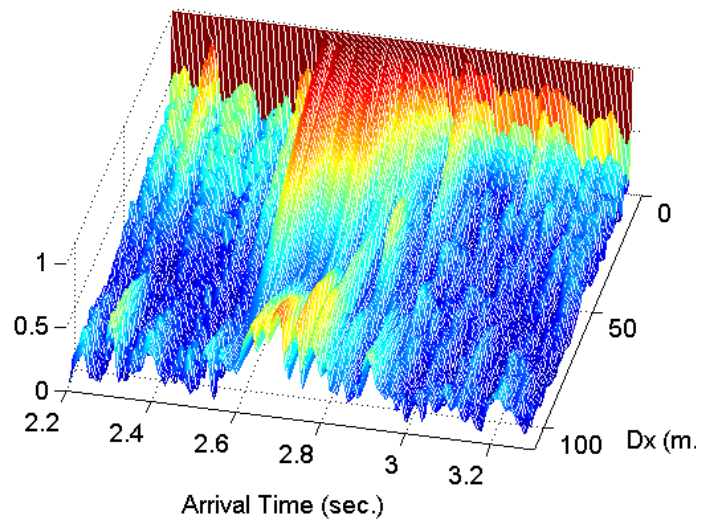




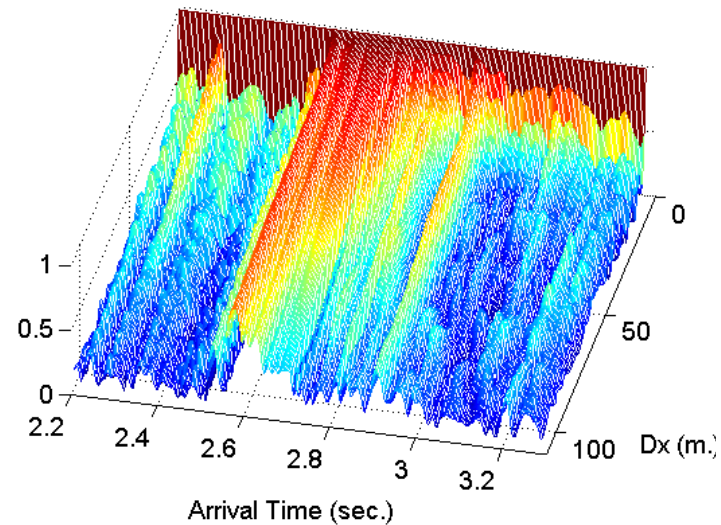
Spatial Coherence A1 203m 20 km 250 Hz



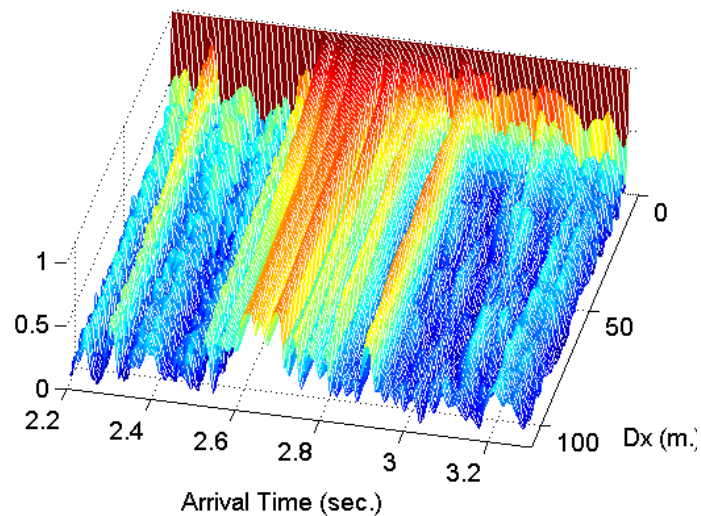
Spatial Coherence A1 203m 20 km 250 Hz



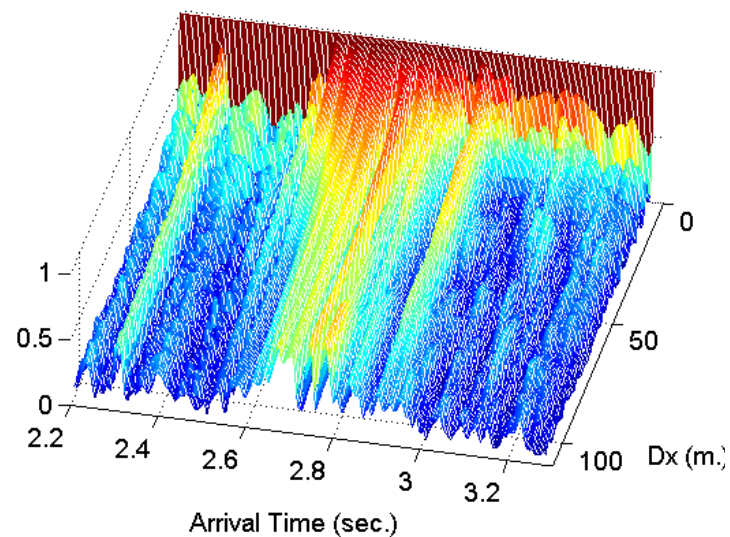
Spatial Coherence A1 203m 20 km 250 Hz



Spatial Coherence A1 203m 20 km 250 Hz



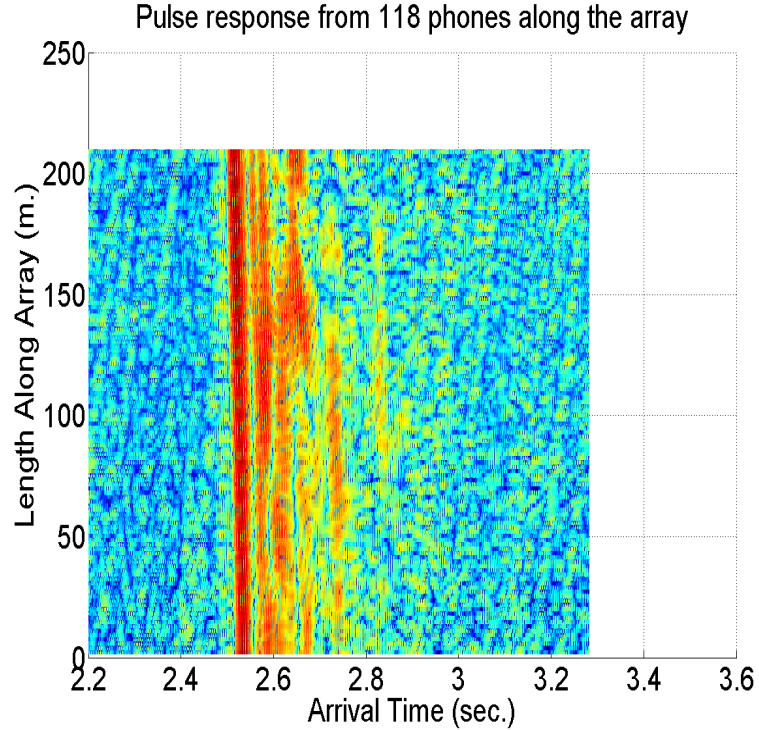
Spatial Coherence A1 203m 20 km 250 Hz



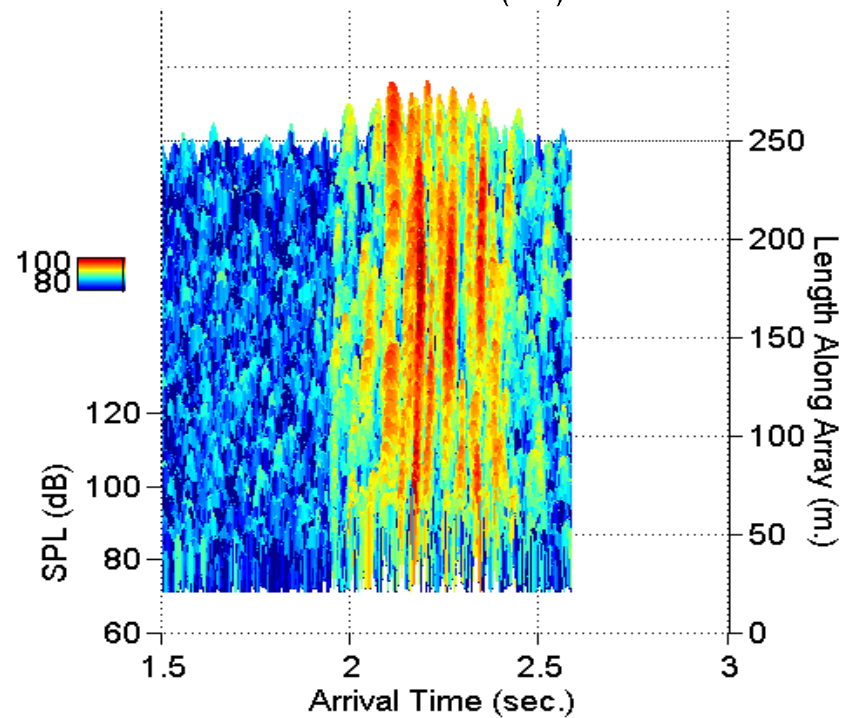




10 km



80 km



## 800 Hz. data time history 20 km

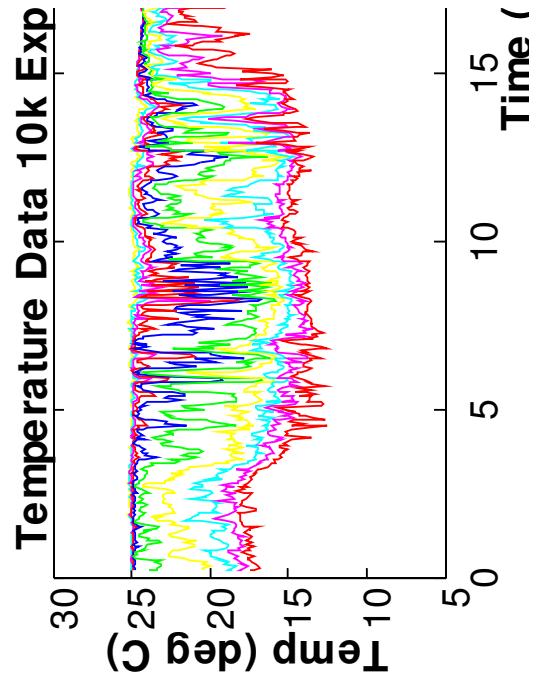
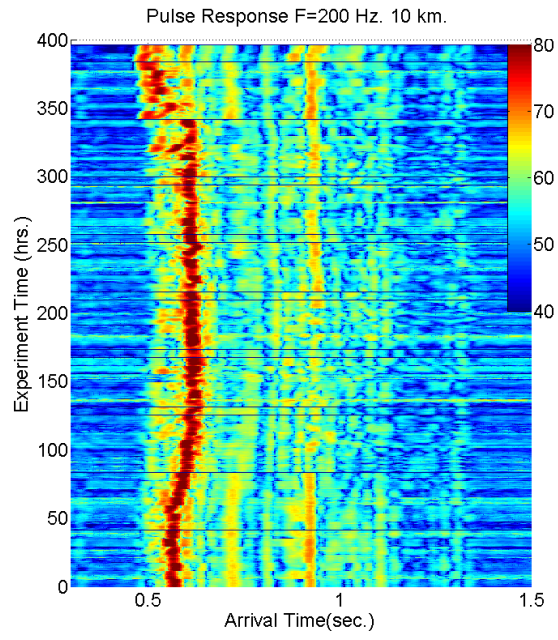
No internal waves(1800)

With internal waves(2230)

cir\_800hz

## Spatial Coherence

- Higher order modes less coherent than lower order
- Modes have varying arrival angles (horizontal)
- Angular spread (horizontal) depends on range
  - <1 deg. @ 10 km
  - < 3-4 deg. 20 km
  - < 4-6 deg. 80 km
- \* Mode burst in space like those observed in time
- Speculation - does not appear to be the principle cause of decorrelation in time or space.

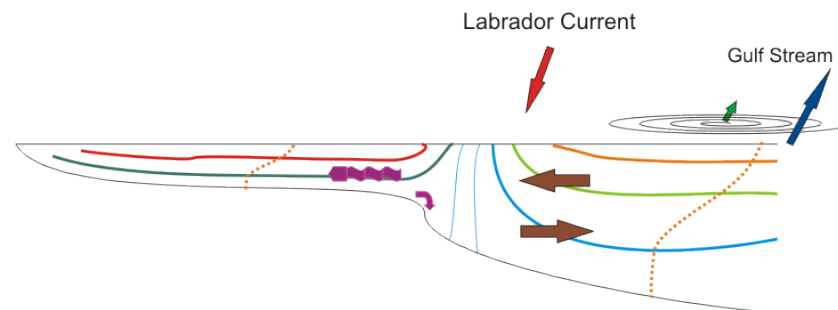
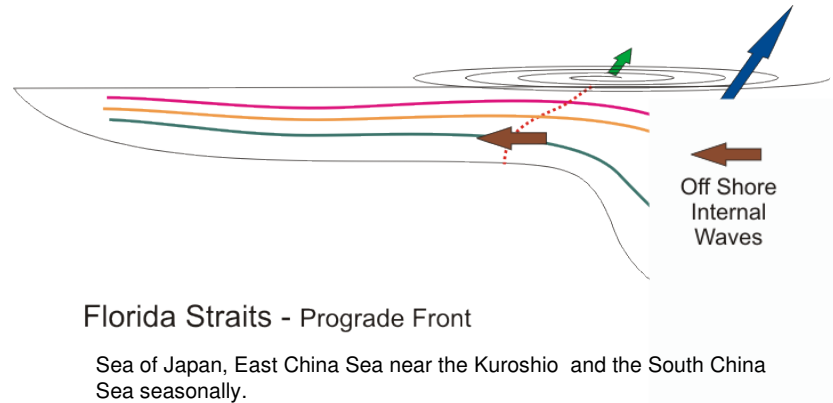


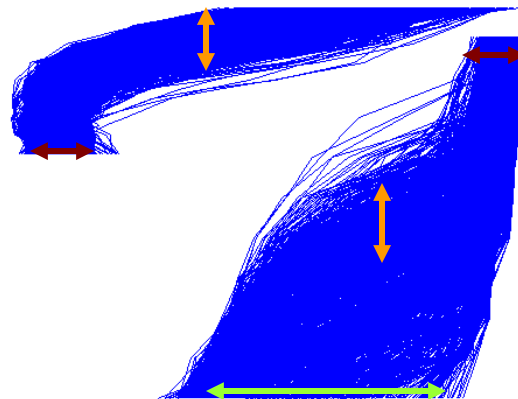
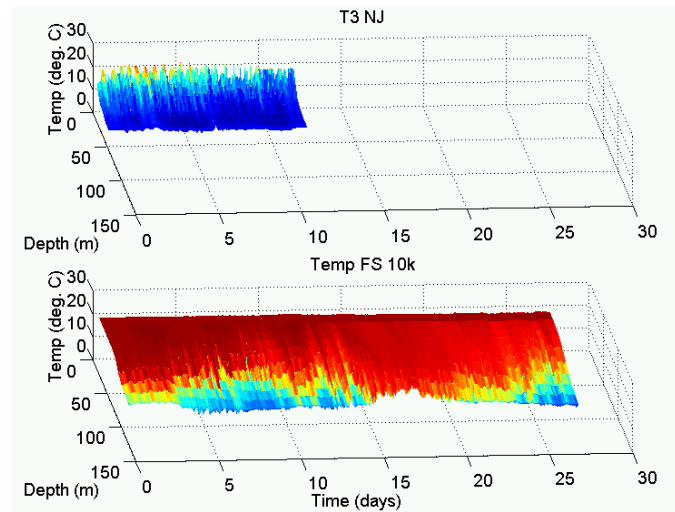
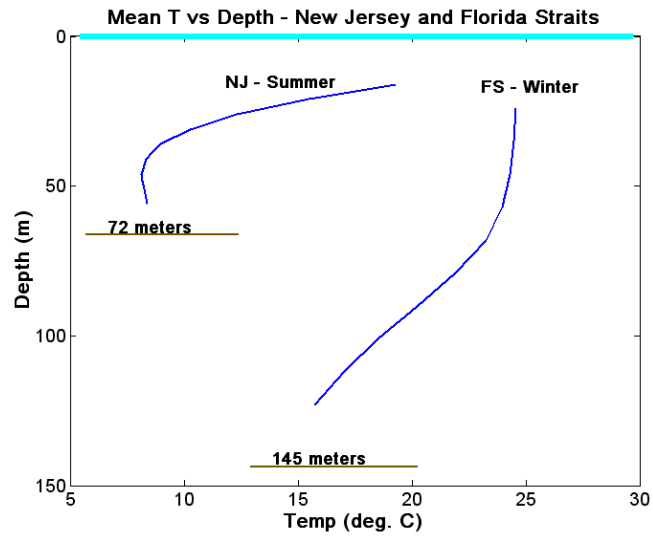
# Publications

1. Observations of Low-Frequency Temporal and Spatial Coherence in Shallow water. DeFerrari.  
Topic -- FSPE and AO data analysis of spatial and temporal coherence  
Status – Submitted
5. Temporal Coherence of Mode Arrivals. DeFerrari, Lynch, Newhall.  
Topic -- MSM to SHRU's transmission data analysis - temporal coherence  
Status – Submitted
9. Spatial Coherence of Mode arrivals. DeFerrari, Colis, Duda, Newhall  
Topic -- MSM to Shark - Coherence of mode arrivals.  
Status – Early draft.
13. Acoustic Propagation on Shallow Shelves Inside of Retrograde and Progade Fronts.  
Topic -- Comparison of internal wave fields and effects of propagation for two types of environments.
5. Limitations of Horizontal Coherence in Shallow Water.

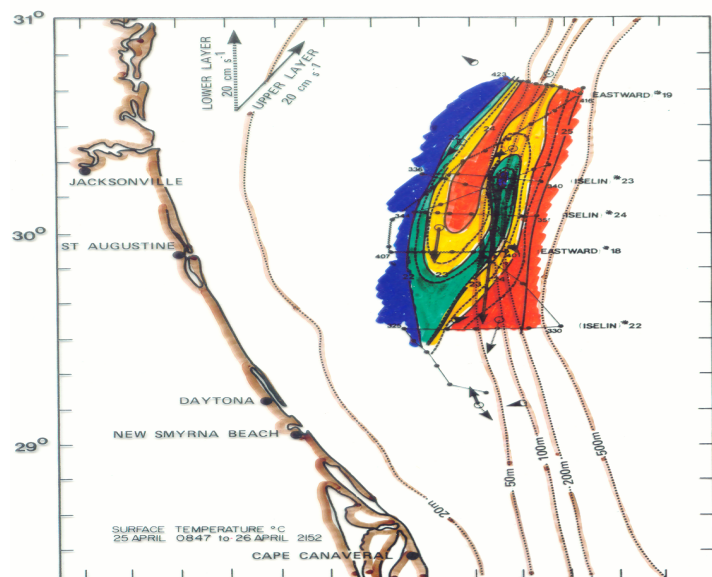
# Acoustic propagation shallow shelves inside of western boundary currents

## Prograde vs Retrograde fronts

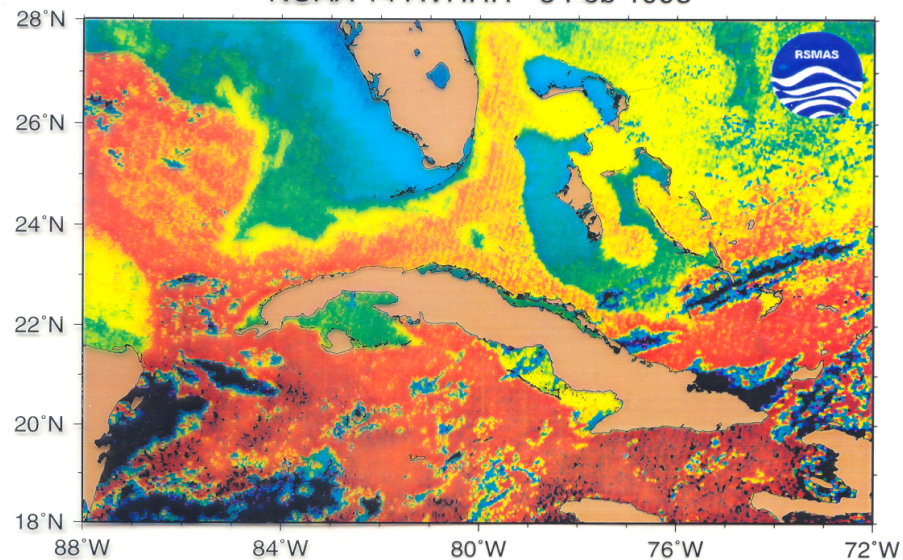




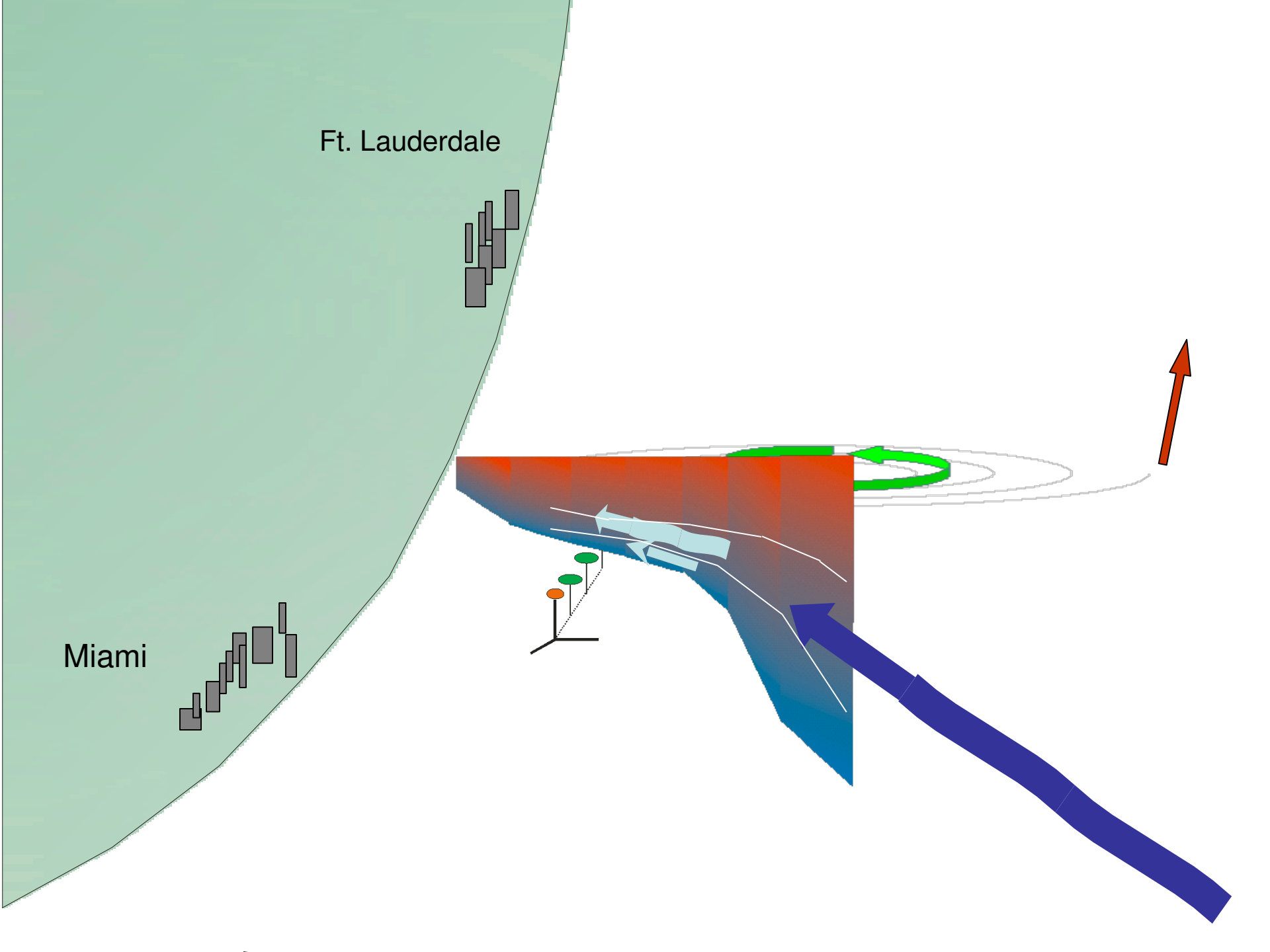
Seasonal  
Internal Wave  
Sub-inertial

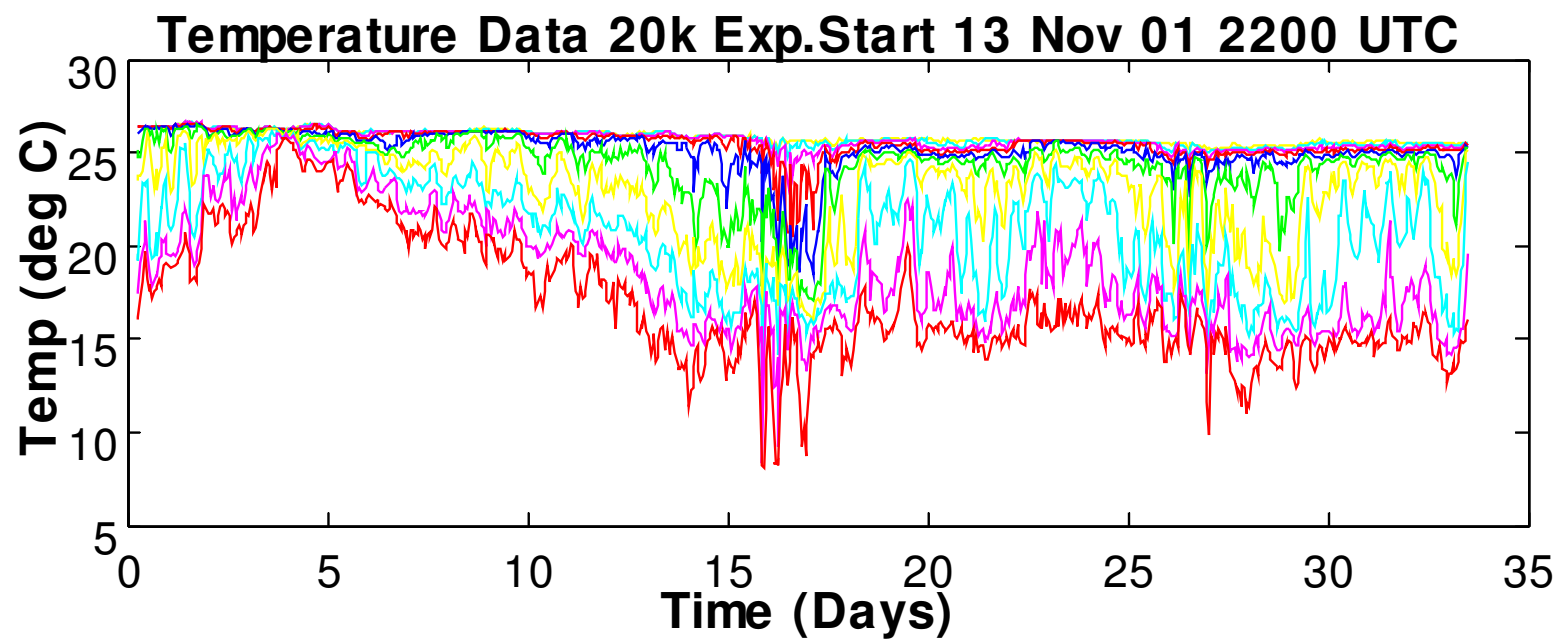
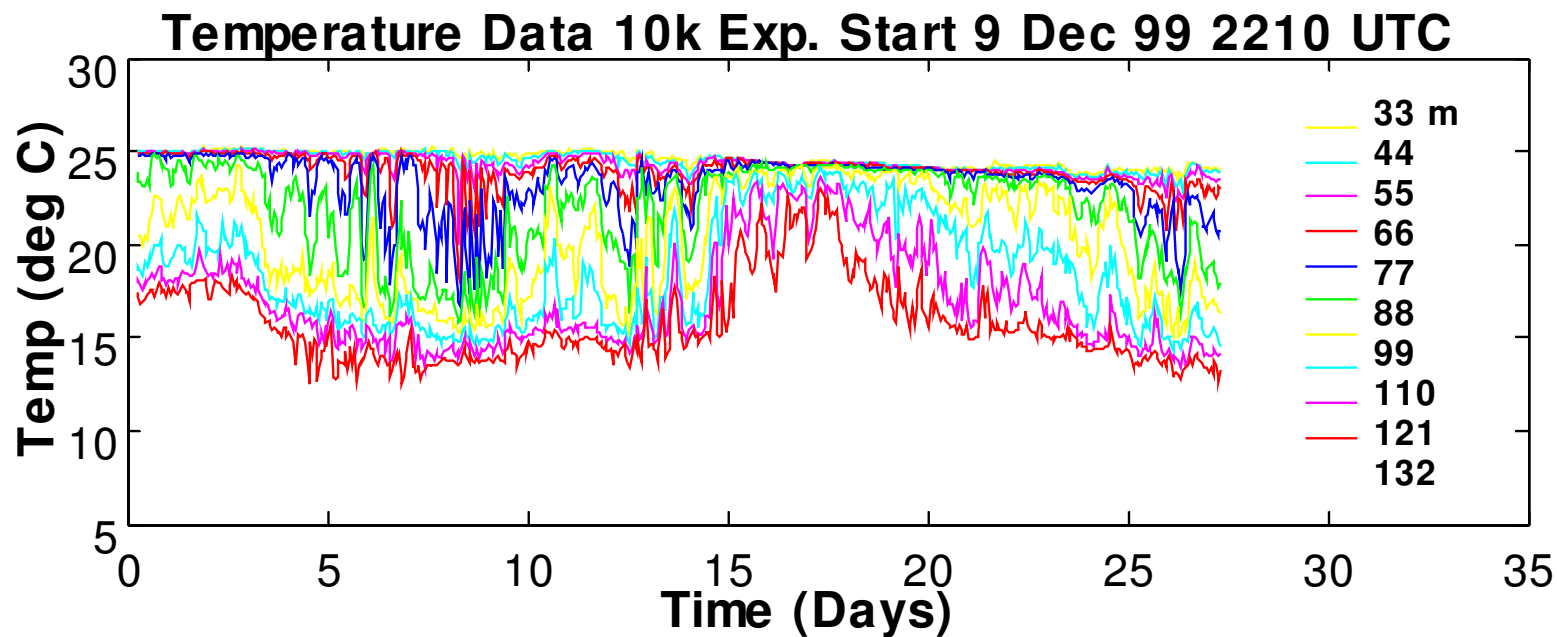


NOAA 14 AVHRR - 3 Feb 1995

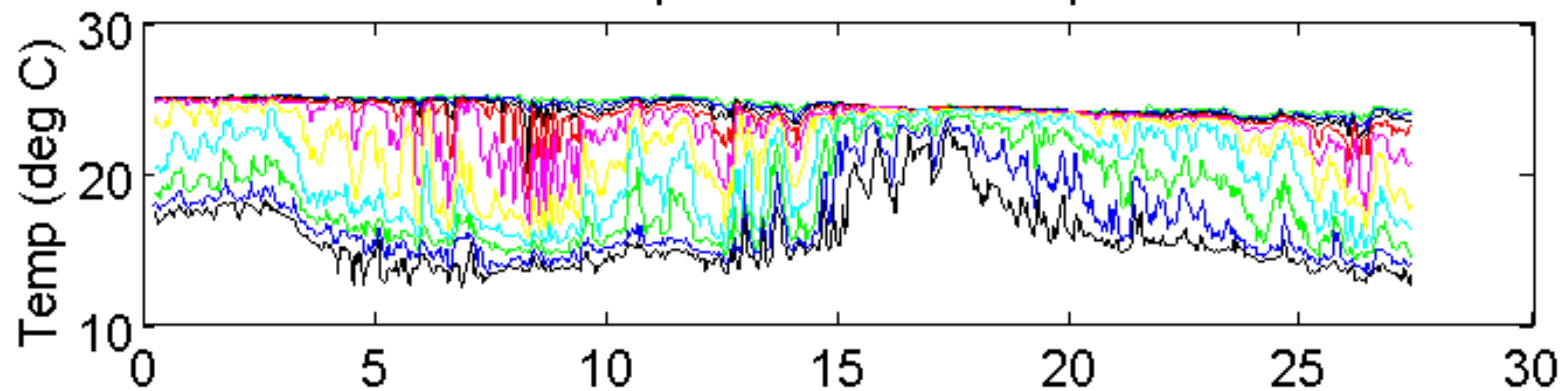




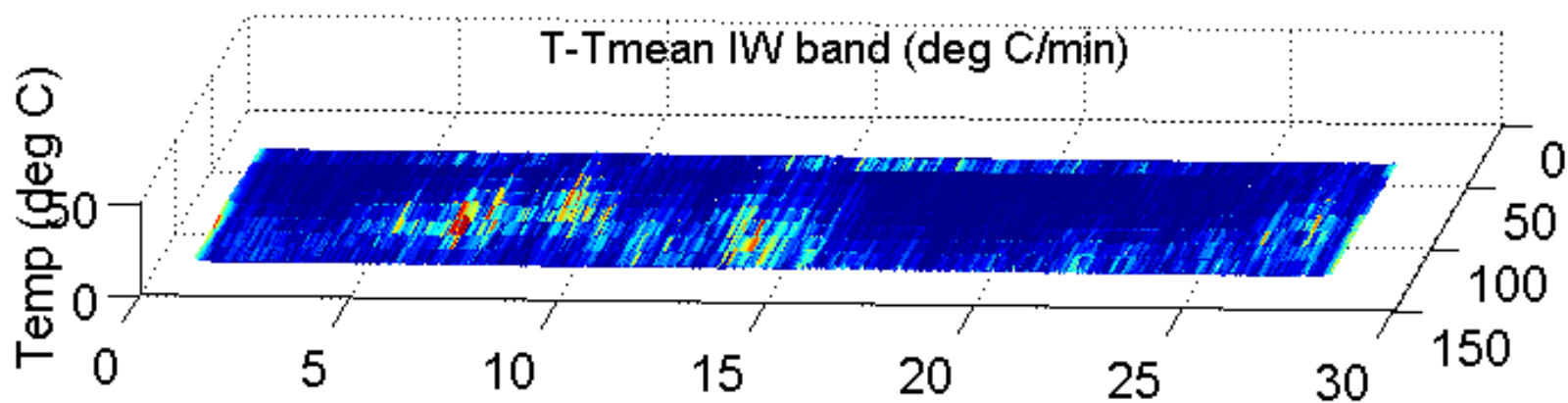




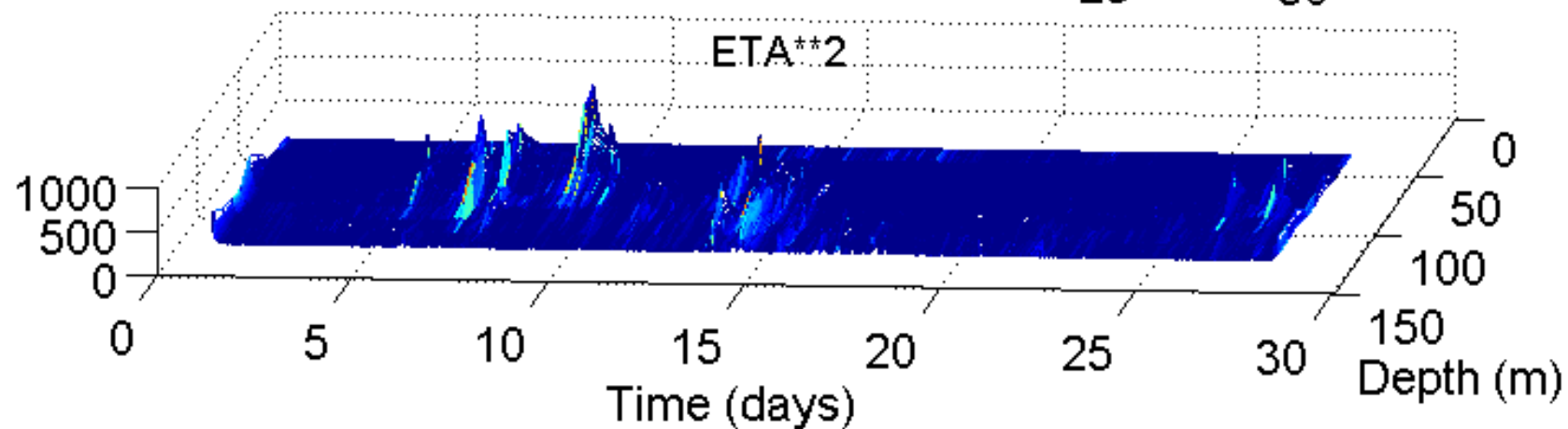
Temperature Data 10k Exp.



T-Tmean IW band (deg C/min)



ETA\*\*2



# Effects of an eddy

## **3. Produces a focusing sound speed profile for RBR Modes**

- Deep source is amplified relative to shallow source
- Near perfect multipath recombination

## **4. Forms a duct for internal waves to propagate onto the shelf**

- Orders of magnitude increase in IW energy
- Corresponding increase in sound speed variability –degrades signal coherence

**Mesoscale modulation of cross shelf exchange in the Straits of Florida**  
**D. Olson, H. DeFerrari, N. Shay and W. Johns**  
**Progress in Oceanography**

**Focused arrivals in shallow water propagation in the Straits of Florida**  
**H. DeFerrari, N. Williams and H. Nguyen**  
**ARLO 4, 106 (2003)**

# Data Sets

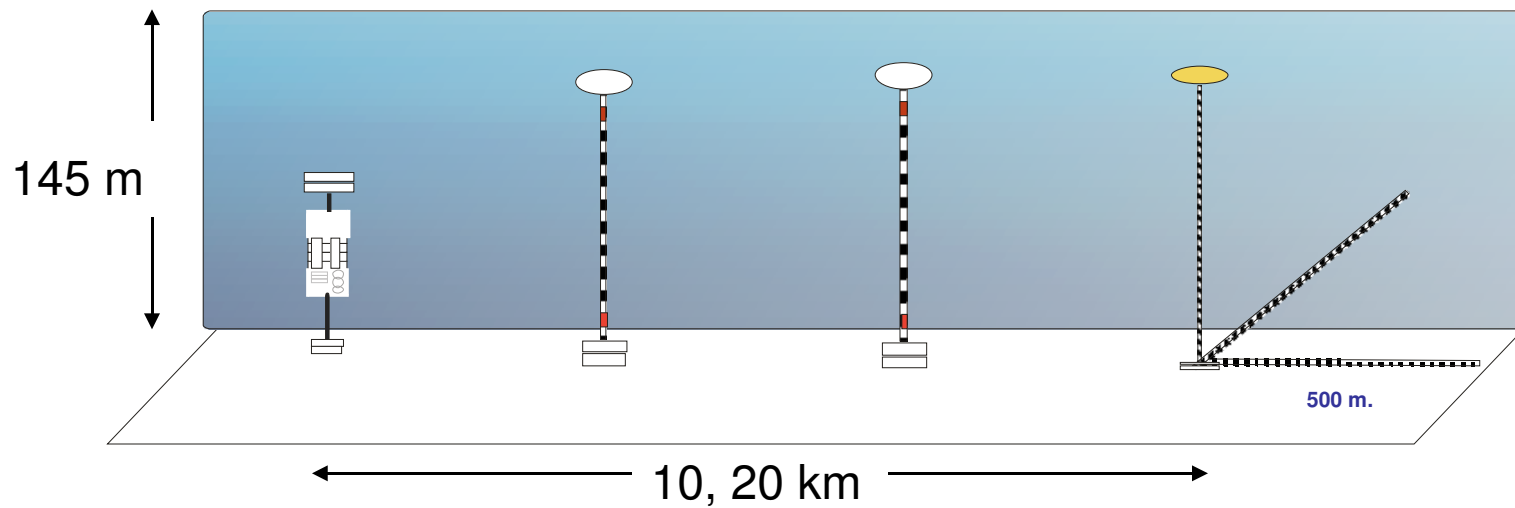
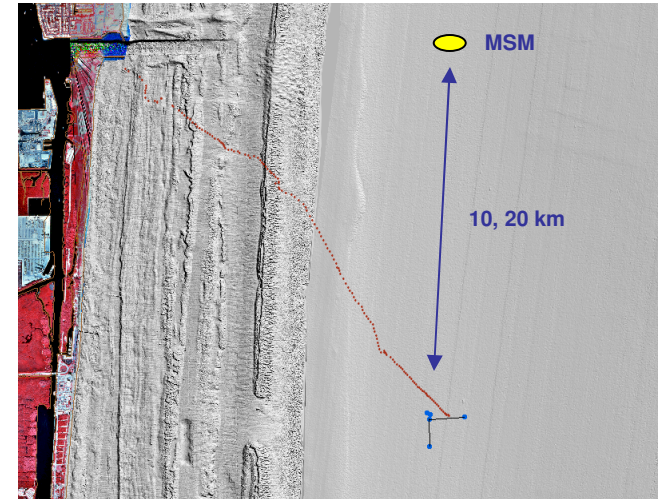
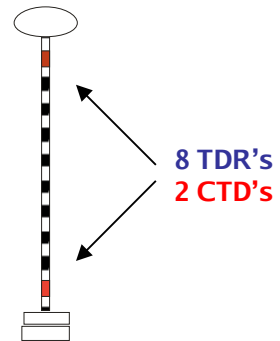
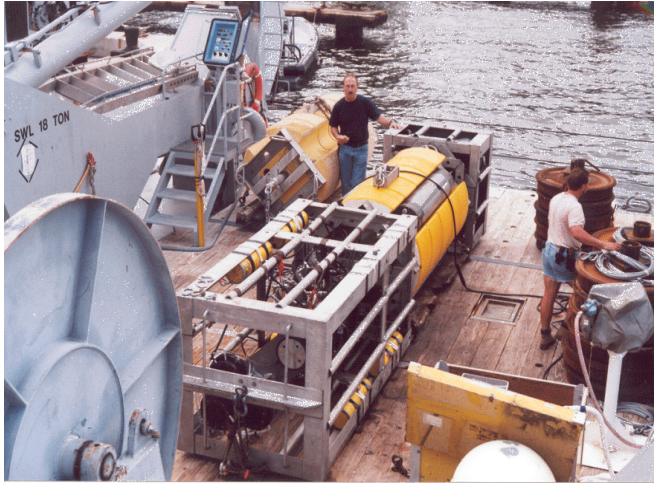
(M-sequence  $q=4$ )

- **SW06**
  - Continuous transmission to SHRU receivers. 50 hours  
→ temporal properties – fluctuations, coherence in time
  - Periodic transmission to SHARK VLA and HLA  
→ spatial properties
- **FSPE** - Florida Straits Propagation Experiment
  - Continuous Transmission 2 -30 day periods.  
→ temporal properties
- **AO** - Acoustic Observatory
  - Short 20 min Transmission 500 element - HLA  
→ spatial properties 20 to 80 km.

## Miami Sound Machine

$F_c = 100, 200, 400, 800, 1600, 3200$ . Hz.

$B_w = 25, 50, 100, 200, 400, 800$ .



## Florida Strait Propagation Experiments

### Transmissions

M-Sequences

Hour	Frequency
------	-----------

1	100
---	-----

2	200
---	-----

3	400
---	-----

4	800
---	-----

5	1600
---	------

6	3200
---	------

7	100
---	-----

repeat

\*

\*

28 days



### Reception

VLA

32 – Phones

Coherent Averaging  
(1 min)

SHARP

Pulse compression

**Pulse Responses**

One per minute

## Signal Processing of M-sequences:

- Synchronous sampling  $n \times f$ ,  $n = > 4$ .
- Coherent averaging for 1 minute.
- Sharp Pulse Compression (SPC) - Hadamard Transforms - a matched filter operation that yields the pulse response instead of the correlation of the pulse response.

## Result:

- Gain =  $10 \log(M \times L)$ , =36dB @400 Hz.
- 2x Improvement in time resolution.
- Transparent to end user - no time leakage.
- Robust and well documented.



# SW06 Experiments – Mid-Atlantic Bight

MSM



19.7 km Range

85 m Depth



VLA



HLA

SHARK

MSM

M-Sequences

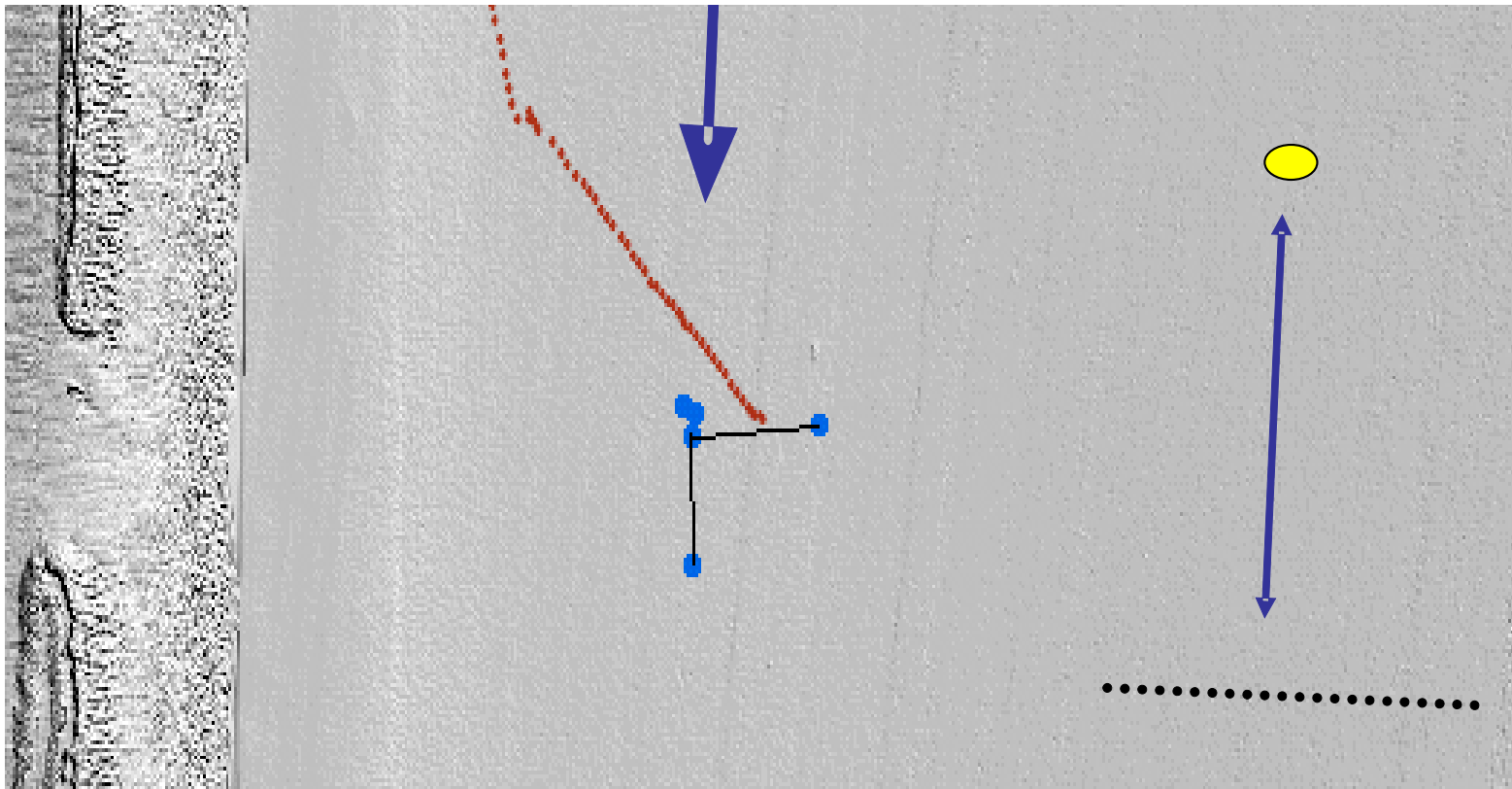
Center freq.		Band
4	Hz.	25
200		50
400		100
800		200
1600		400

VLA 16 phones

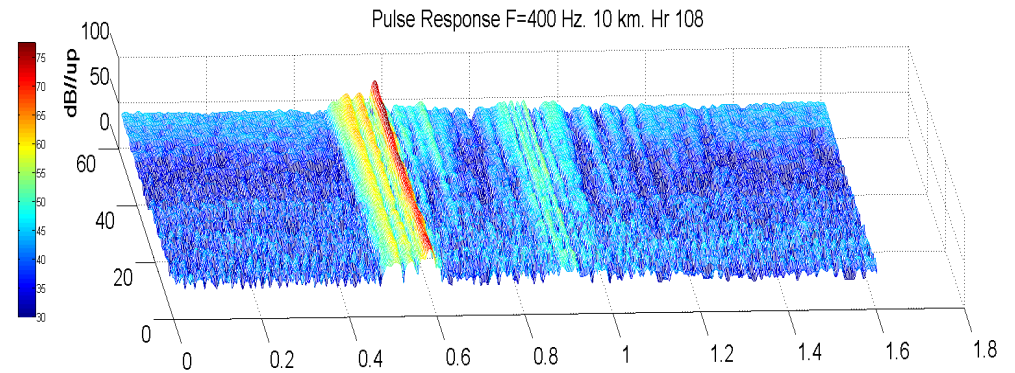
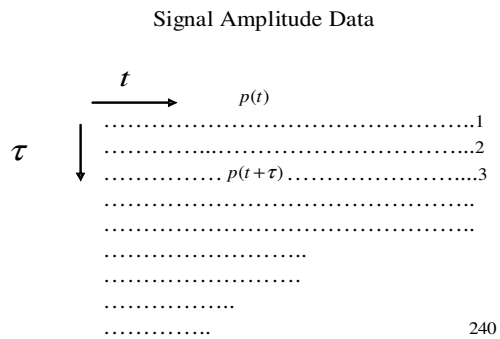
HLA 32 phones 468 m (15 m spacing)

# Acoustic Observatory CALOPS Sept 07

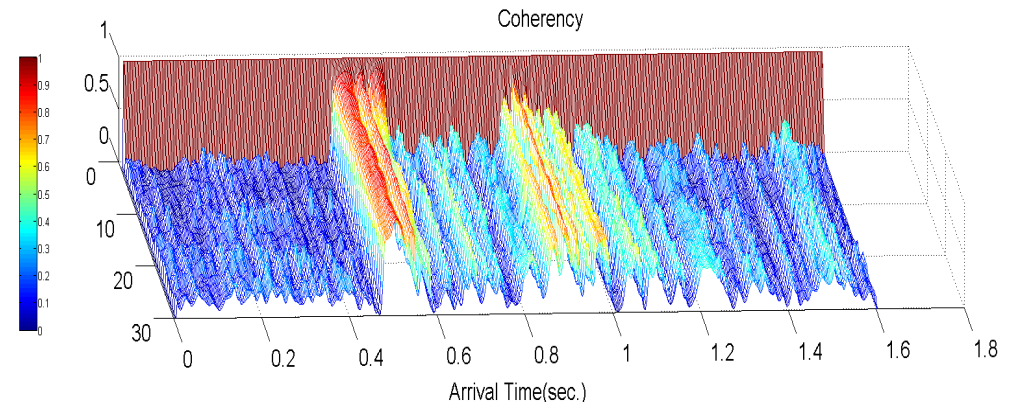
## Shipboard Suspended and Towed Transmissions



# Data Analysis



$$COH(t, \tau) = \frac{\langle (p(t) * p(t + \tau))^2 \rangle_{\Delta t, \Delta T}}{\langle p(t)^2 \rangle_{\Delta t, \Delta T} \langle p(t + \tau)^2 \rangle_{\Delta t, \Delta T}}$$



# Propagation Modeling

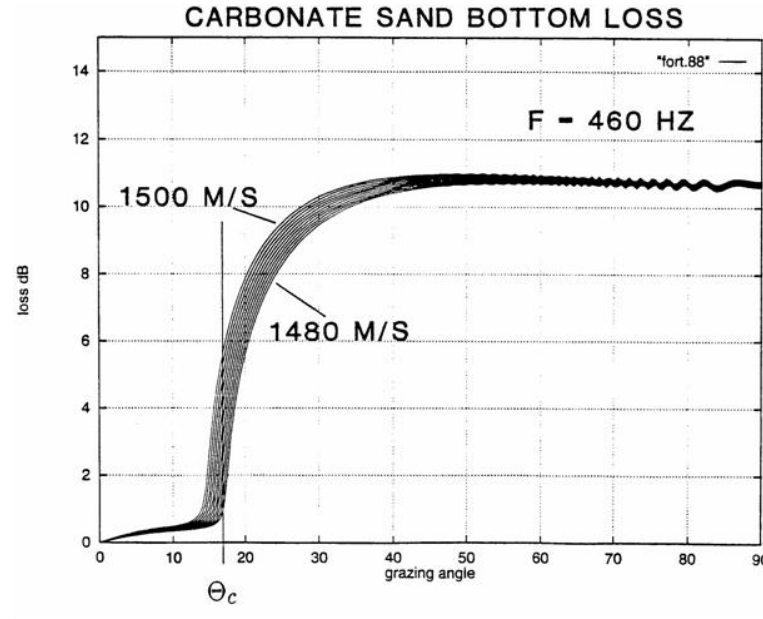
## Identifying modes and arrivals

# Propagation Modeling

## Propagation Models

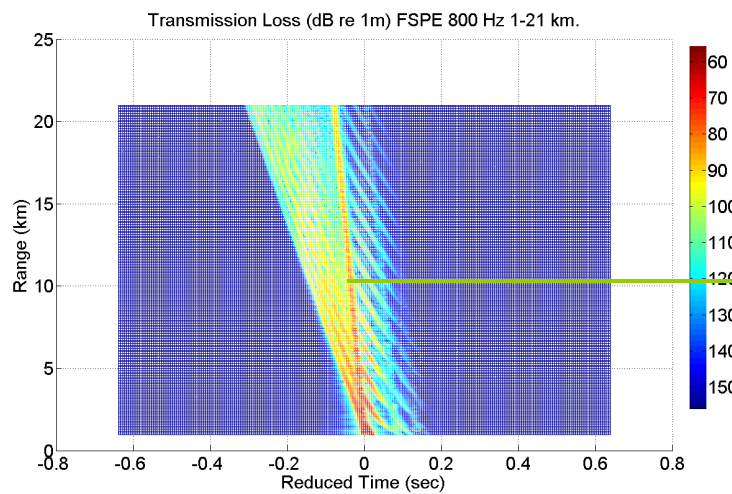
- PE
  - MMPE
- Normal Mode
  - PROSIM
  - SNAP
- SAFARI

## Bottom Models

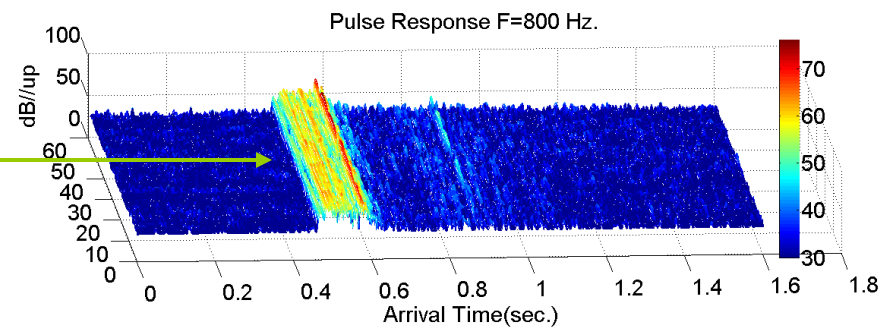


	Velocity (m/s)	Gradient (1/s)	Density (dB/km/Hz)	Loss (dB/km/Hz)	Shear (m/s)	Shear Loss (dB/km/Hz)
MONJO	1585	1.4	1.85	.30	300	3.3
MEASURED (cores)	1640	1.4	1.95	.30	300	6.3
CHAPMAN (inv)	1720	1.4	2.06	.60	300	6.3

## PE Prediction of 800 Hz. Pulse Response

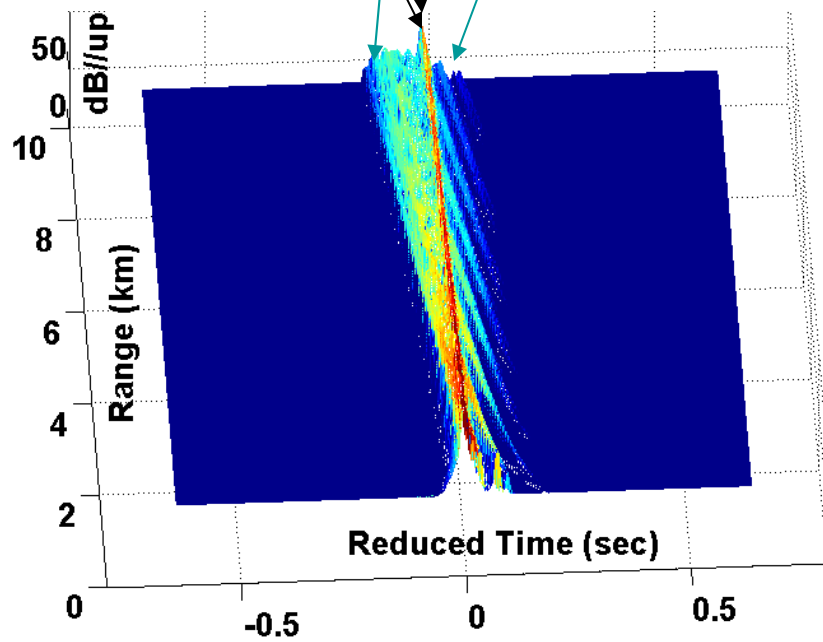
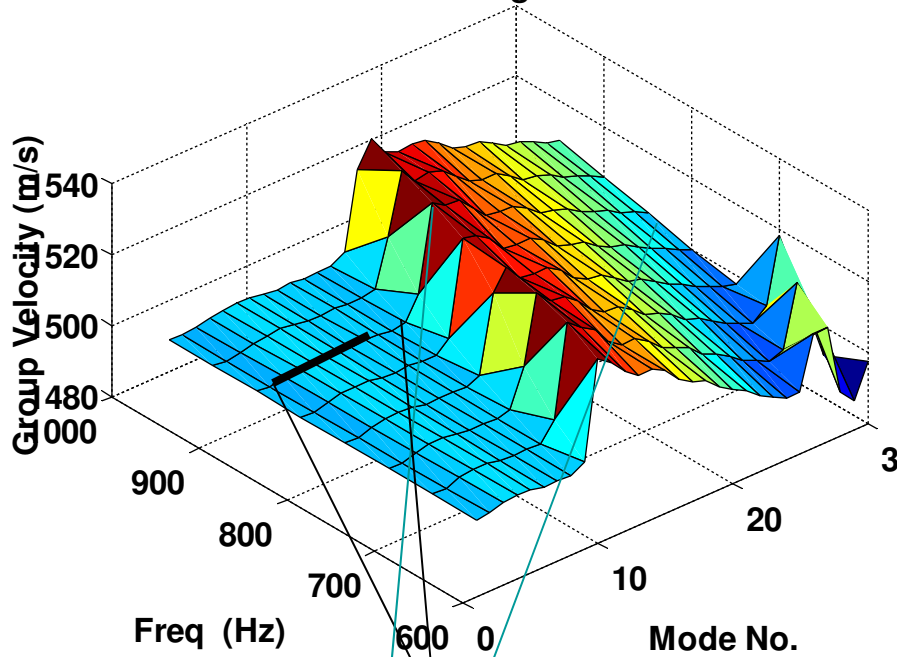


## Measured - 1 Hour

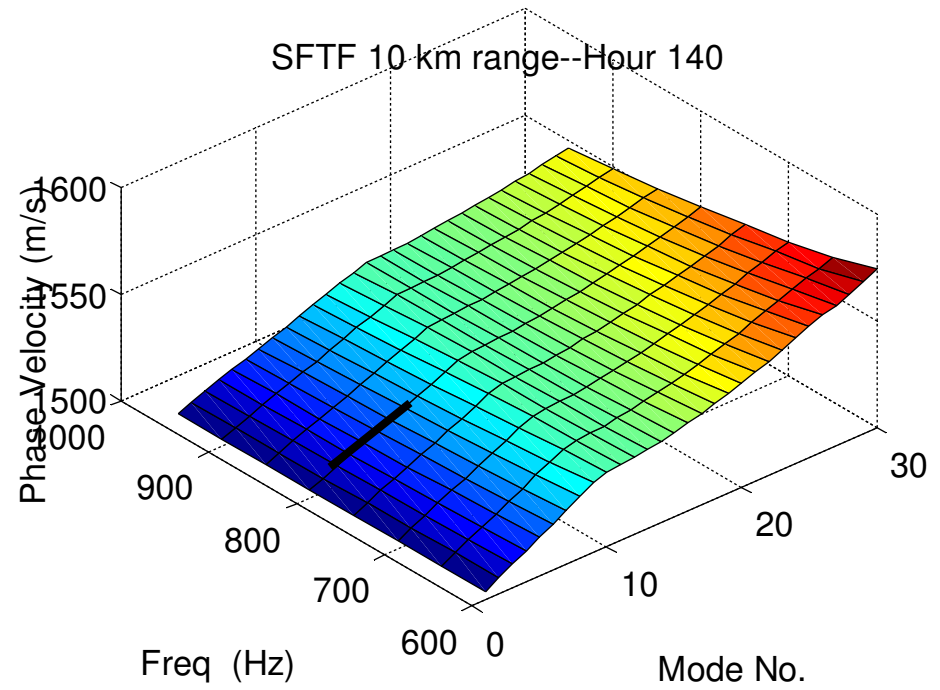




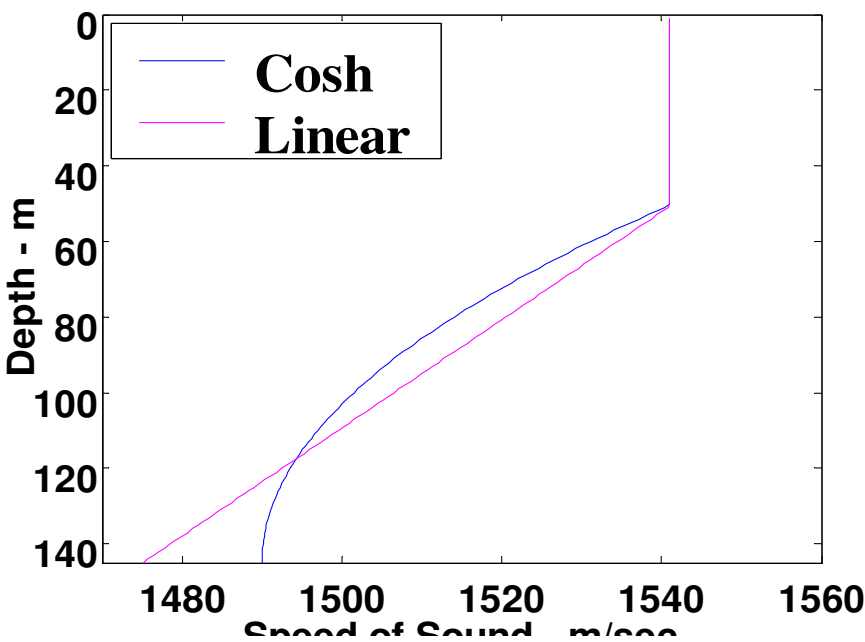
SFTF 10 km range--Hour 140



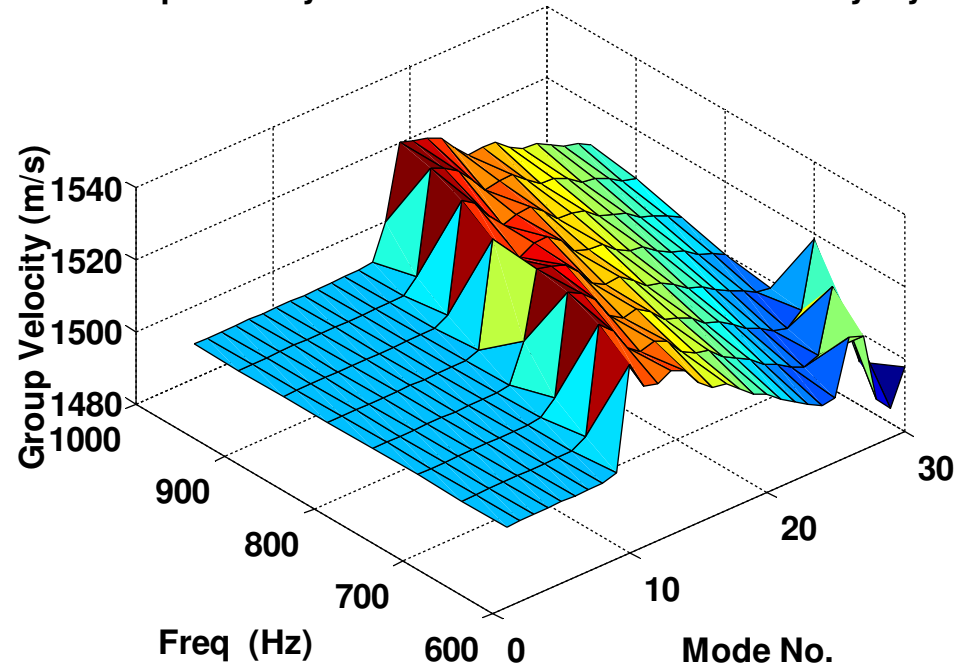
SFTF 10 km range--Hour 140



$$\beta^{-1} = -\frac{\Delta s_{g,mn}}{\Delta s_{p,mn}}$$



Group Velocity COSH Profile w/ 75 m isovelocity layer



$$\beta^{-1}$$

SRBR      BRB

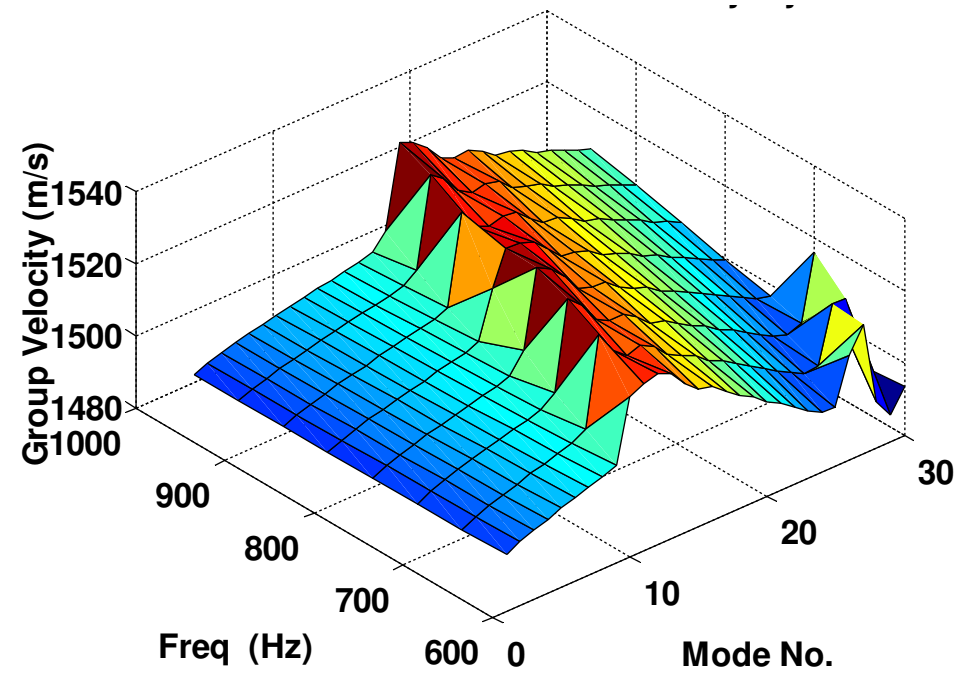
Linear

1.0      -0.5

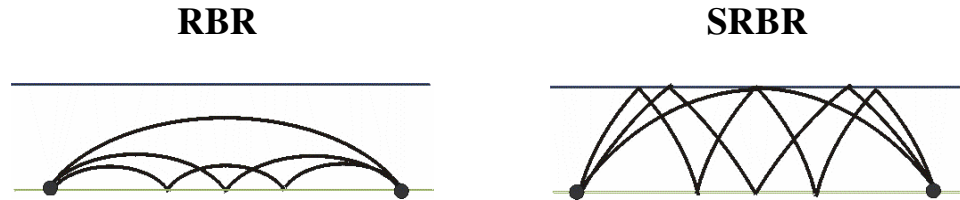
Cosh

1.2      0.0

$$c_o \cosh(g(1-z/D))$$



## Ray/Mode Equivalence for $\beta^{-1}$



$$\text{Travel Time} = \int \frac{ds}{c(s)} \propto \frac{PL}{\langle c \rangle}$$

### Travel Time dependence on Launch Angle:

Linear Profile  $\langle c \rangle > \text{PL}$ ,  $\beta^{-1} = -.5$

$\text{PL} > \langle c \rangle$ ,  $\beta^{-1} = 1.0$

Cosh Profile  $\langle c \rangle = \text{PL}$ ,  $\beta^{-1} = 0.0$

$\text{PL} > \langle c \rangle$ ,  $\beta^{-1} = 1.2$

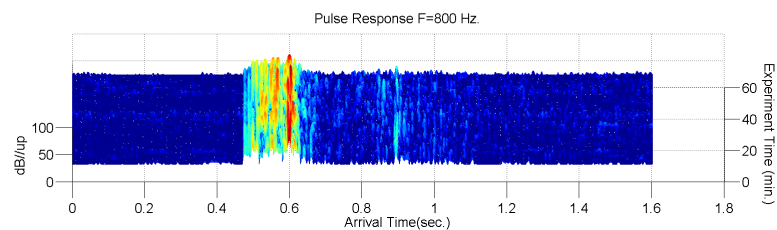
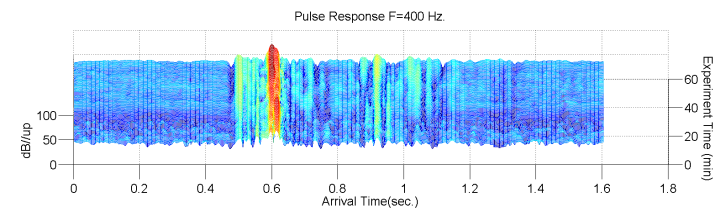
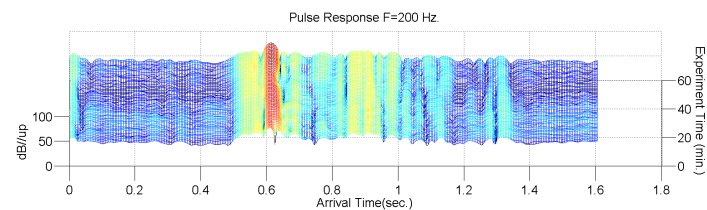
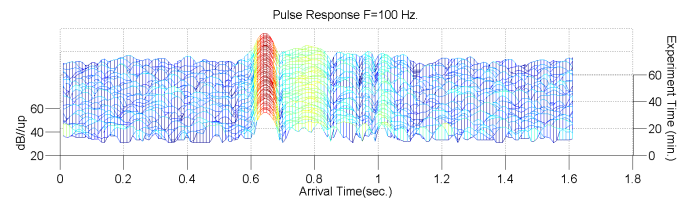
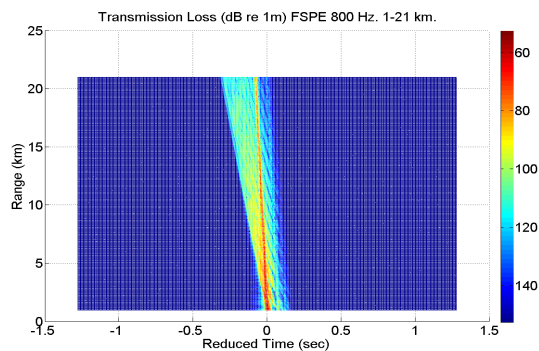
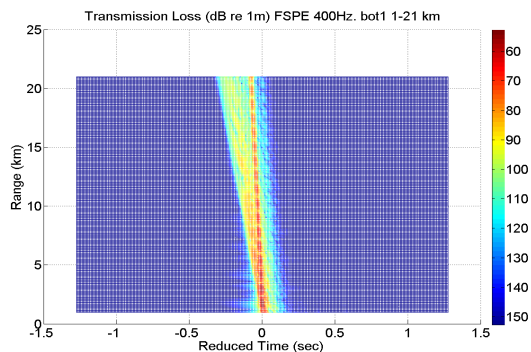
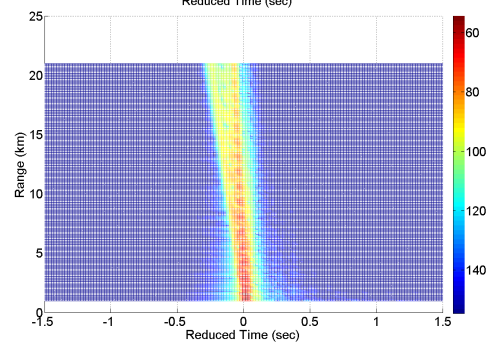
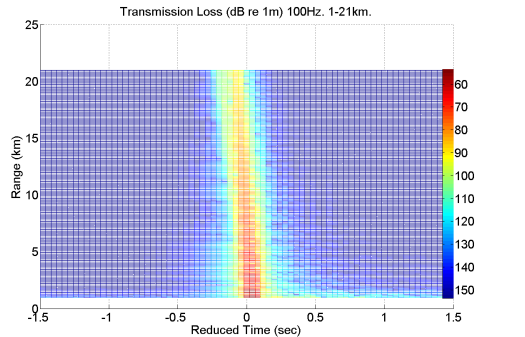
**Conclusion: All BRB eigenrays have exact same travel time at each range.**

# Frequency Dependence Model < > Measurements

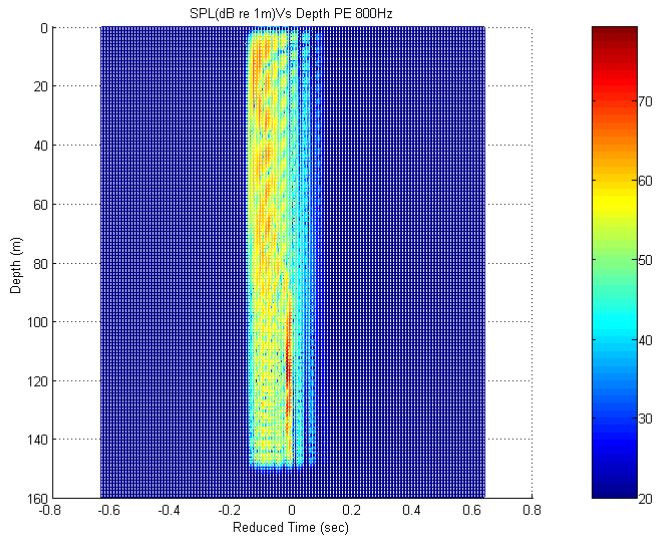
## FSPE

10 km range - f/100 RBR/SRBR modes

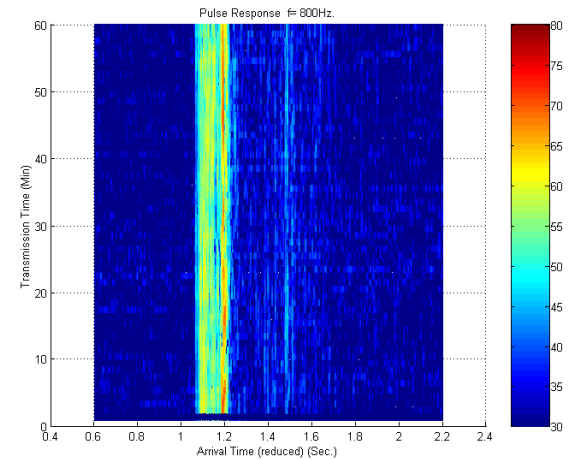
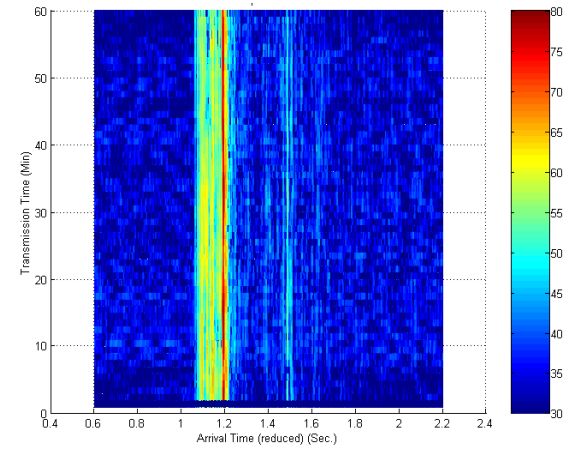
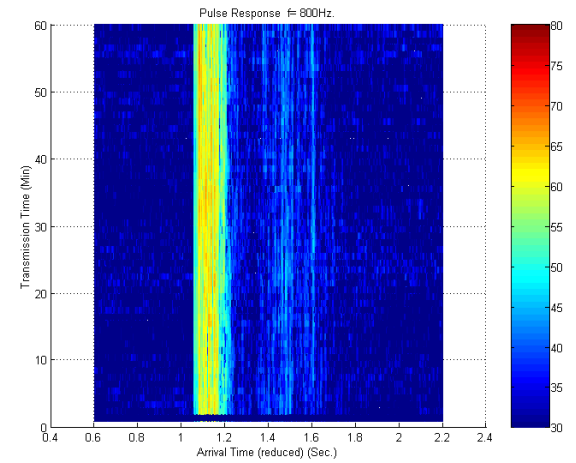
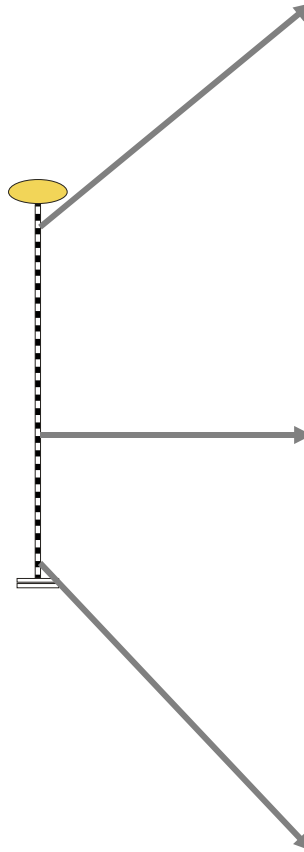
- 8 RBR and 8 SRBR @800Hz.
- 4 RBR and 4 SRBR @400 Hz.
- >
- 1 total @50 Hz.



# Depth Dependence



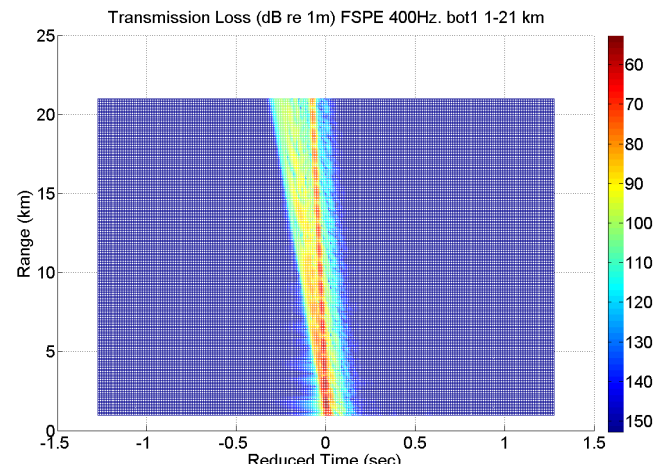
PE Prediction: Pulse Response vs. Depth



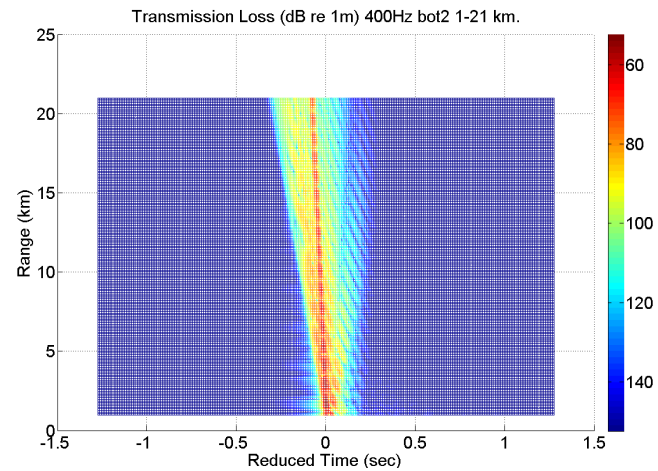
## PE Predictions for 3 Bottom Models

### Monjo Bottom

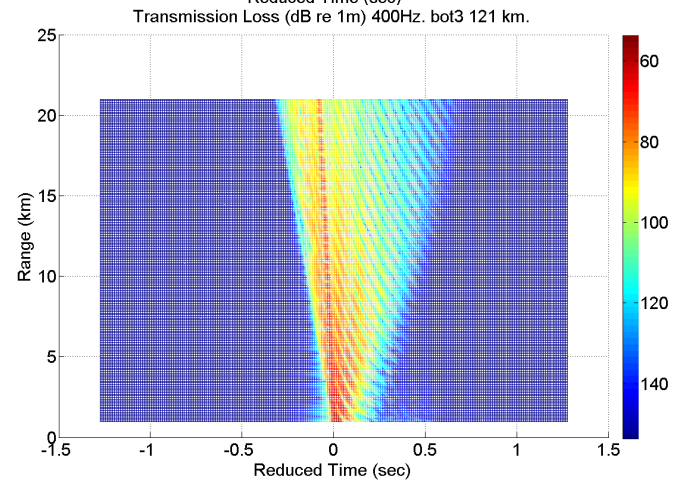
Bottom C = 1580 m/sec.



Bottom C = 1620 m/sec.



Bottom C = 1720 m/sec.

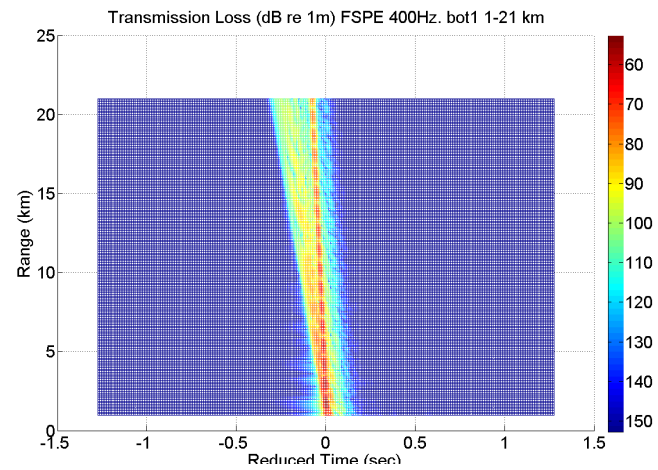




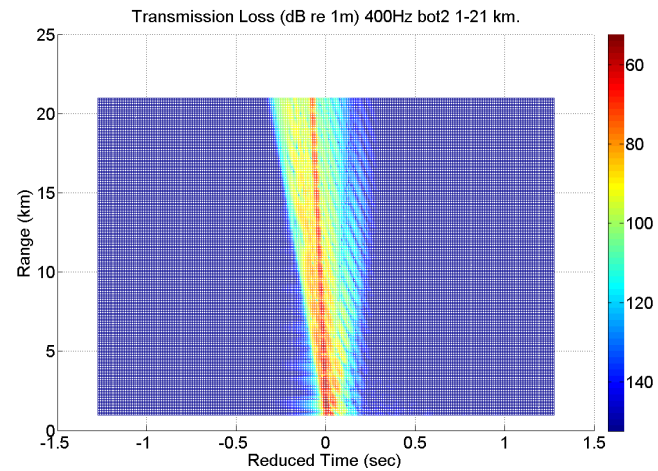
## PE Predictions for 3 Bottom Models

### Monjo Bottom

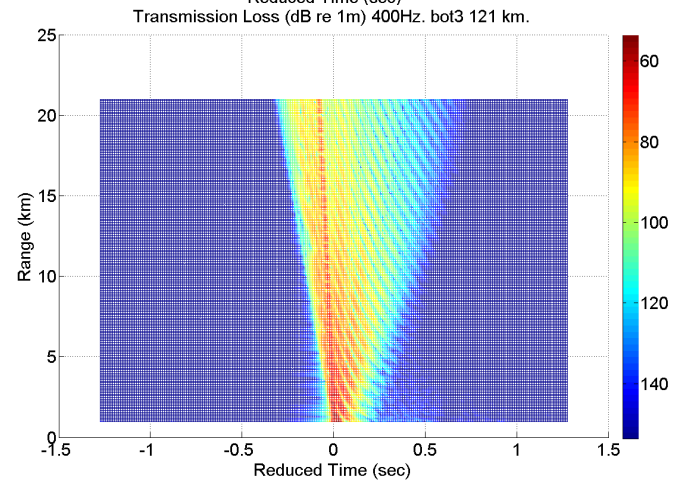
Bottom C = 1580 m/sec.



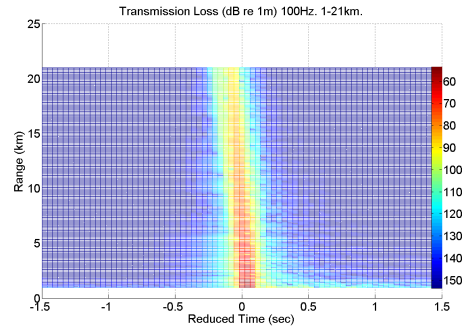
Bottom C = 1620 m/sec.



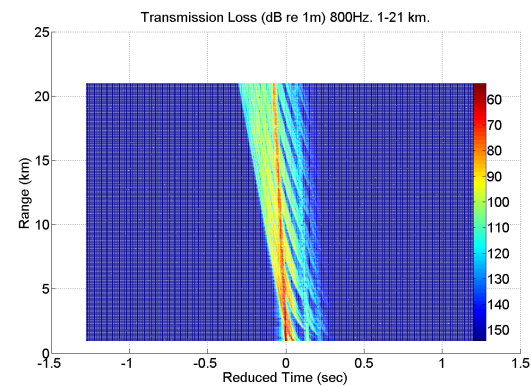
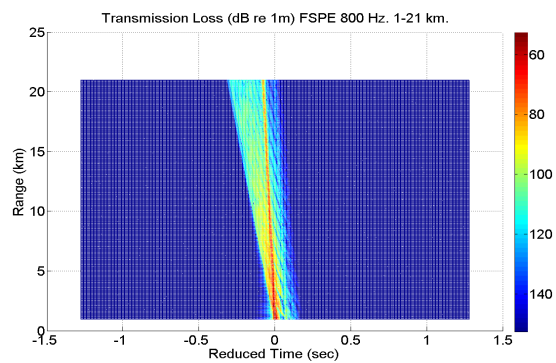
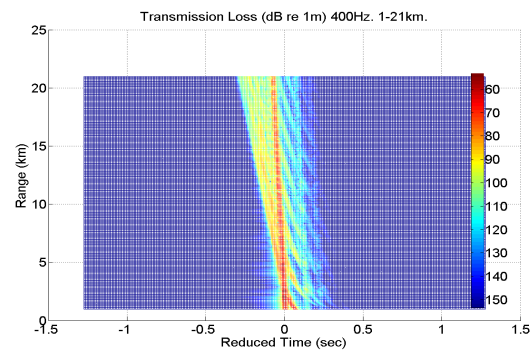
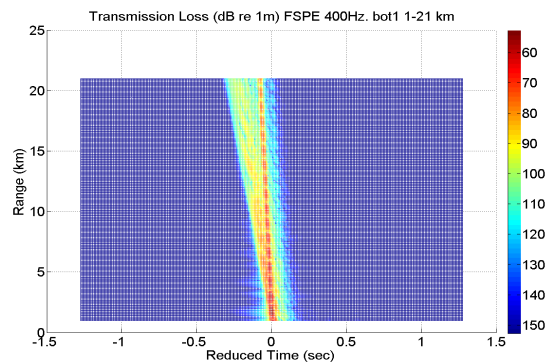
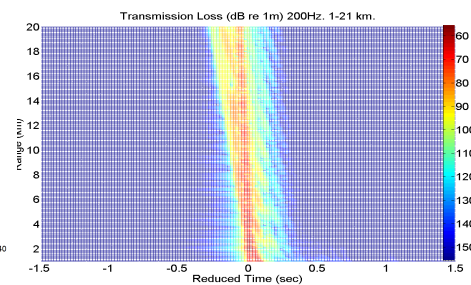
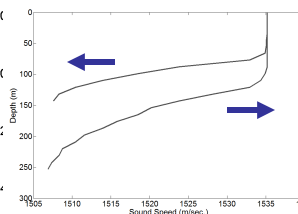
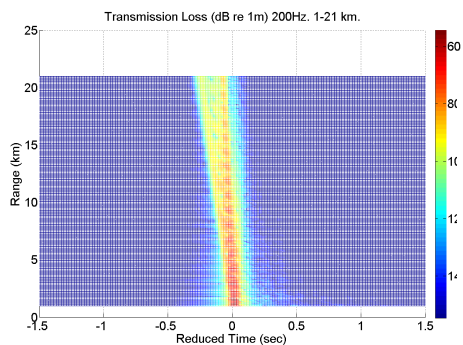
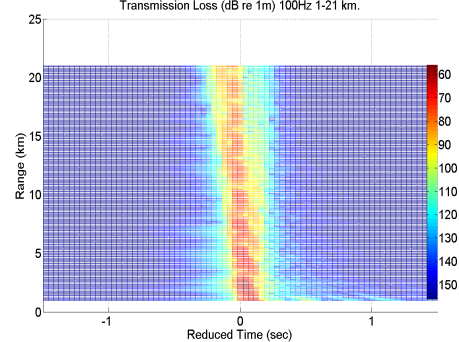
Bottom C = 1720 m/sec.



FSPE



AO



## AO Predictions:

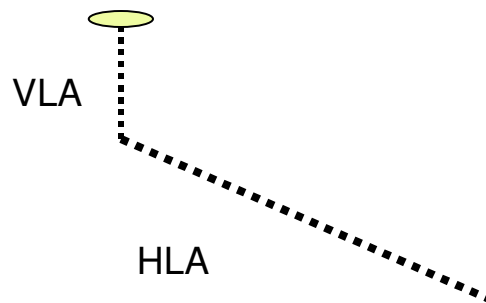
2. Propagation by RBR and SRBR modes/rays. AO interested in SRBR as noise carrying paths.
3. Summer SS profile will narrow the arrival time spread of SRBR's
4. Total number of observable SRBR modes - approx =  $f/100$ . e.g. 4 @ 400 Hz. Only 1 mode for frequencies below 100 Hz.
5. Strong downward  $C(z)$  gradients and absorbent bottom will result in very large TL for SRBR paths - difficult to measure at long ranges > 30km!
6. Temporal coherence times = >10 min → 1 hour+ for lower frequencies with SRBR 50% longer than RBR.
7. Horizontal coherence (radial, bottomed HLA) = > 100wavelengths. e.g. 1500m @100HZ.
8. Propagation model predictions match FSPE measurements best with slower 'Monjo' bottom model than with observed fast "Chapman" bottom. Geo-acoustic reasons unknown.
9. Many low-loss out-of-plane arrivals observed that possibly obscure the detection of low-level late SRBR arrivals. A potential practical problem for noise canceling algorithms.
10. AO measurements results may not differ much from those at FSPE site, (a modeling conclusion!)

# SW06 Experiments – Mid-Atlantic Bight

MSM



19.7 km Range  
85 m Depth



SHARK

MSM

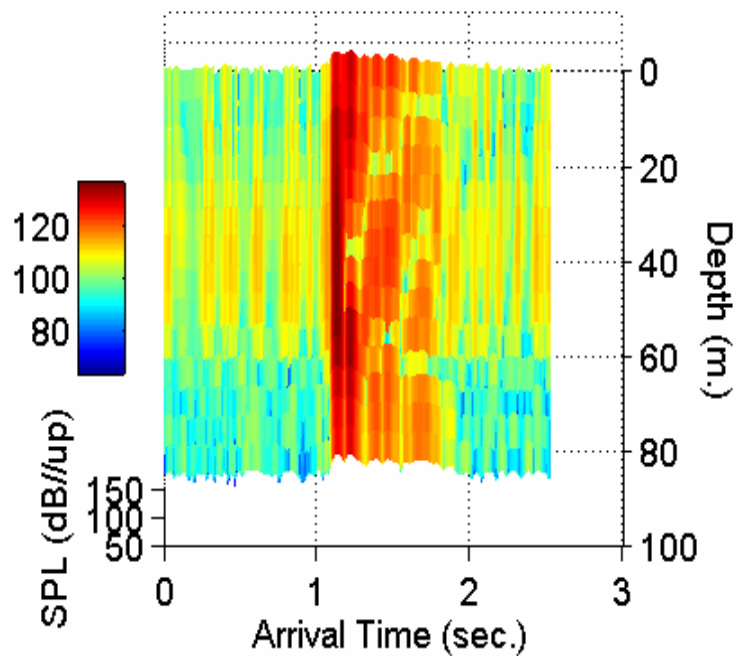
M-Sequences

Center freq.	Band
4 Hz.	25
200	50
400	100
800	200
1600	400

VLA 16 phones

HLA 32 phones 468 m (15 m spacing)

Shark VLA 100 Hz. m-sequence



PE Model (first try)  
 $C_b = 1715$  m/s Inversion  
 by K. Smith and J. Miller  
 (In the vicinity)  
 PE (second try)  
 1595 m/s

→

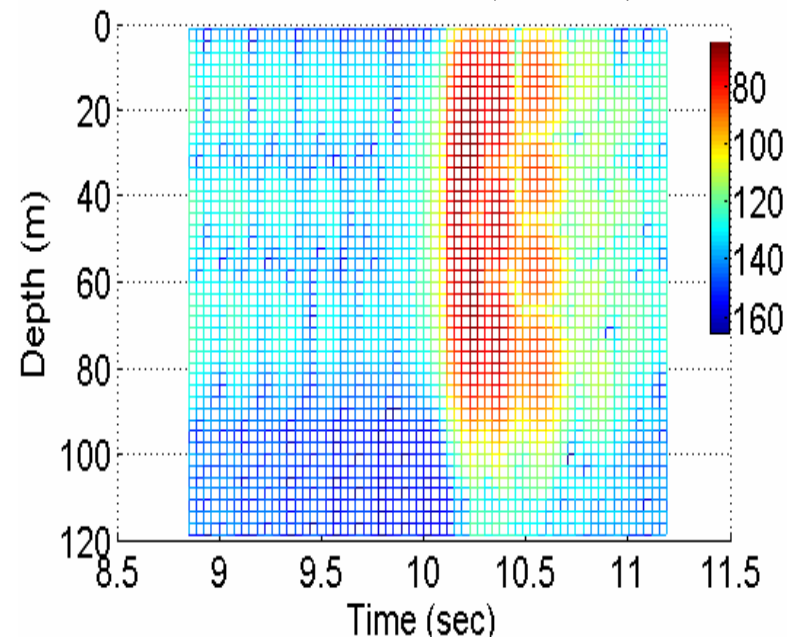
Several extra modes

→

Good Fit ! Above)

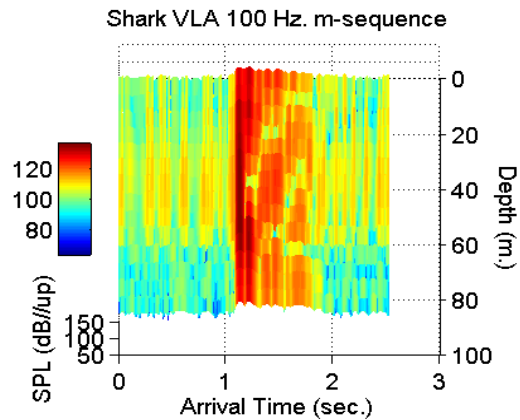
Measurements by UW (direct method) sediment pool at site of experiment  
 1600 m/s !

Transmission Loss (dB re 1m)

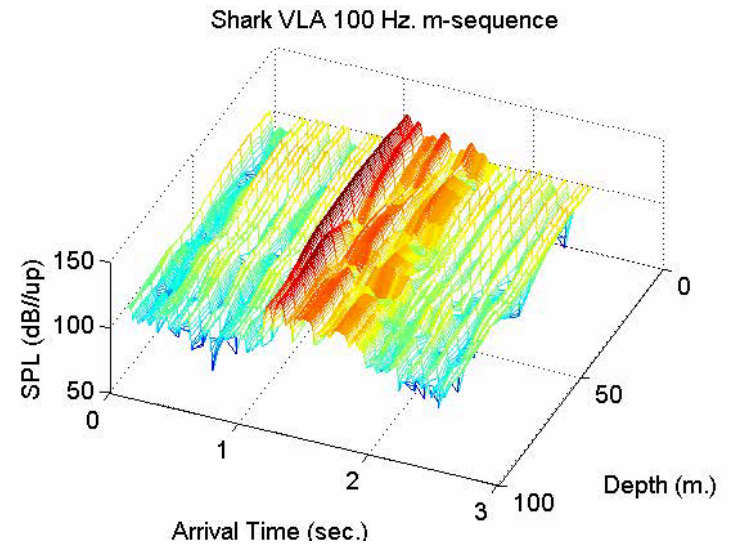
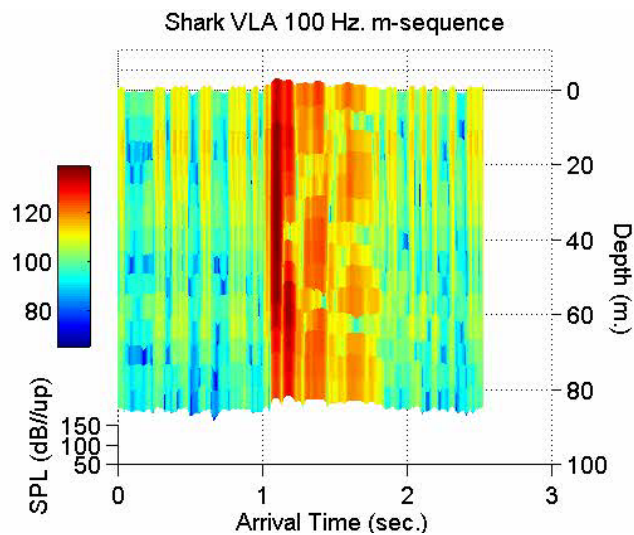
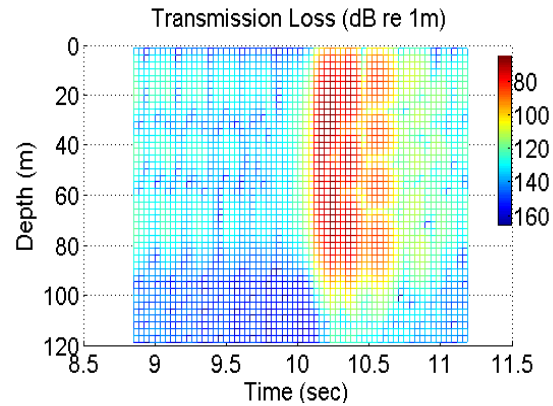


# SW06 Modes and Arrivals

Observed



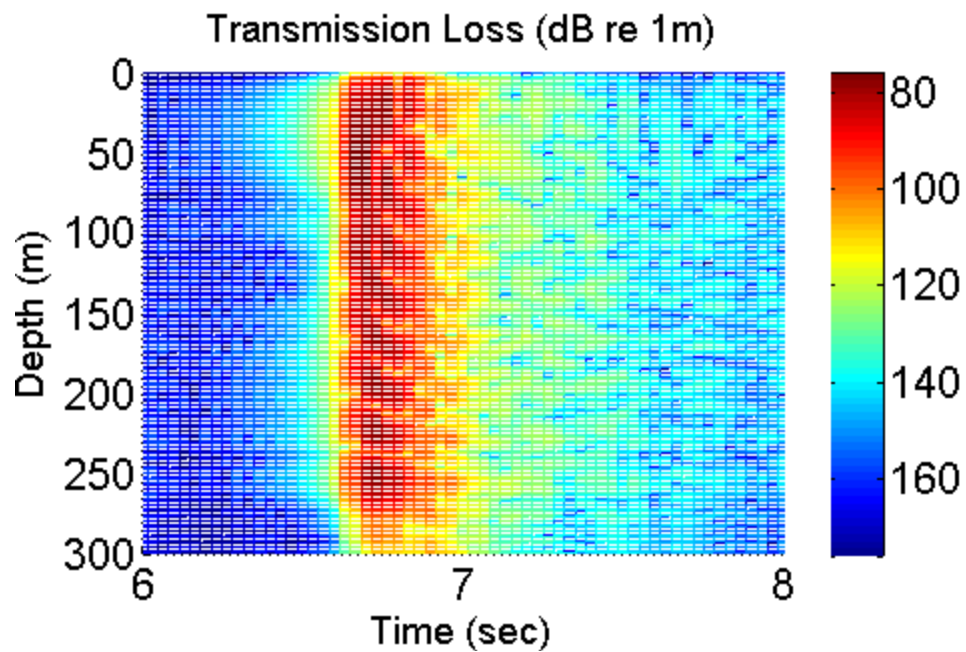
Modeled





## PE Prediction for AO

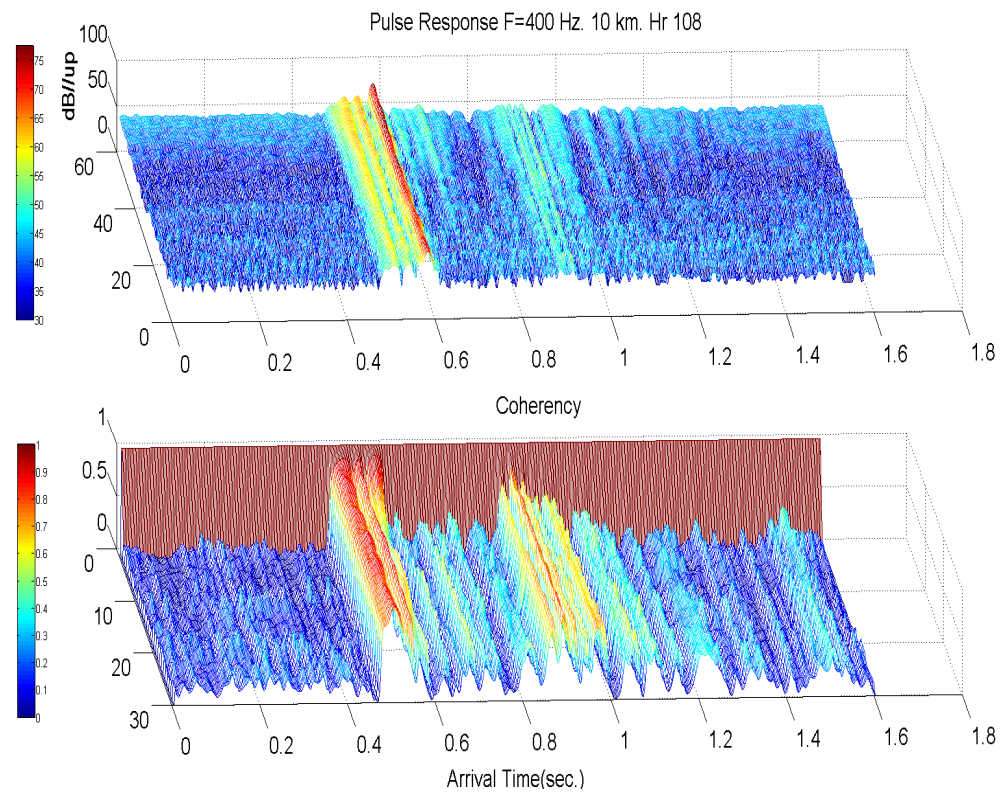
100 Hz. 25 Hz band 10 km.



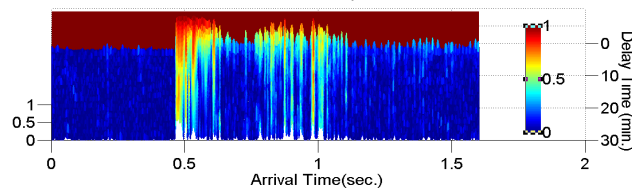
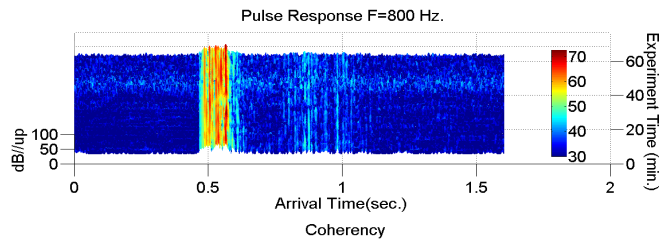
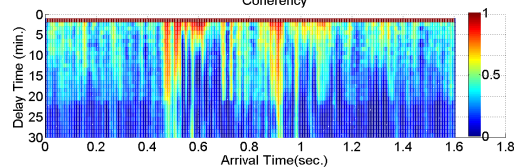
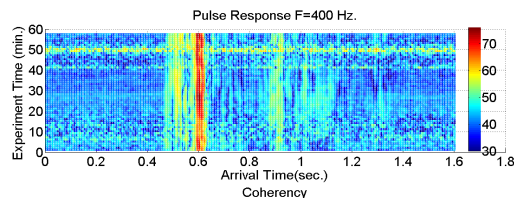
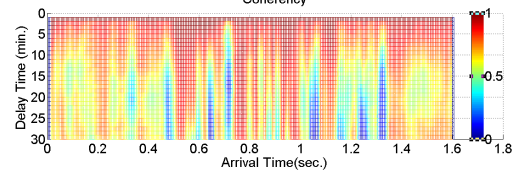
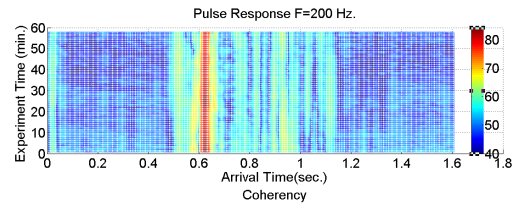
# Temporal Coherence

The diagram shows a horizontal axis for time  $t$  and a vertical axis for time delay  $\tau$ . A horizontal arrow labeled  $t$  points to the right, with  $p(t)$  written above it. A vertical arrow labeled  $\tau$  points downwards, with  $p(t+\tau)$  written to its right. A series of horizontal dotted lines extend from the vertical axis, with labels 1, 2, 3, and 4 on the right side, corresponding to different time delays.

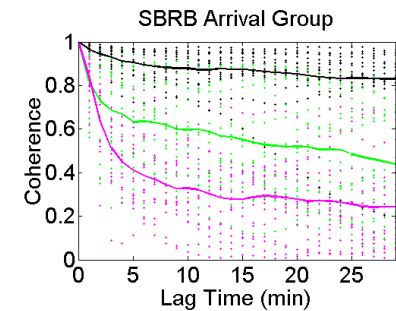
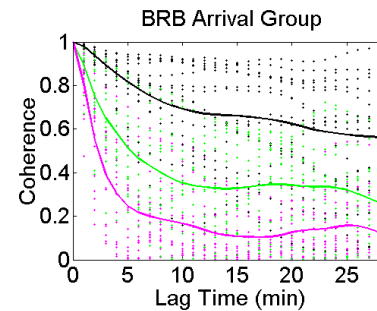
$$COH(t, \tau) = \frac{\langle |p(t) * p(t + \tau)|^2 \rangle_{\Delta t, \Delta T}}{\langle p(t)^2 \rangle_{\Delta t, \Delta T} \langle p(t + \tau)^2 \rangle_{\Delta t, \Delta T}}$$



# Temporal Coherence



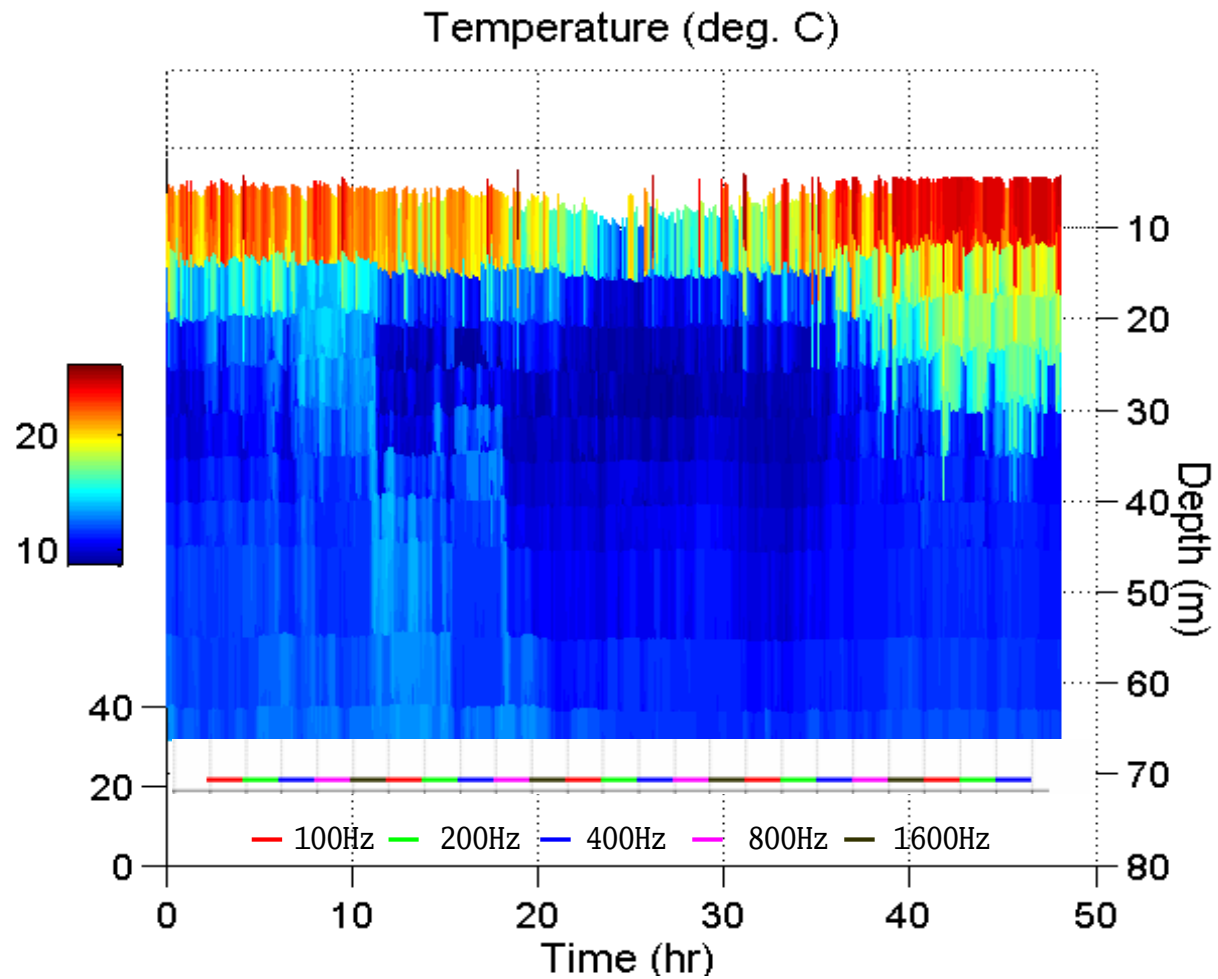
## Temporal Coherence



## Coherence time (.75 level)

BRB Group  
 800Hz. mean → 2.1 max → 6.5 minutes  
 400Hz. 3.4 12.0  
 200. 8.3 > 30

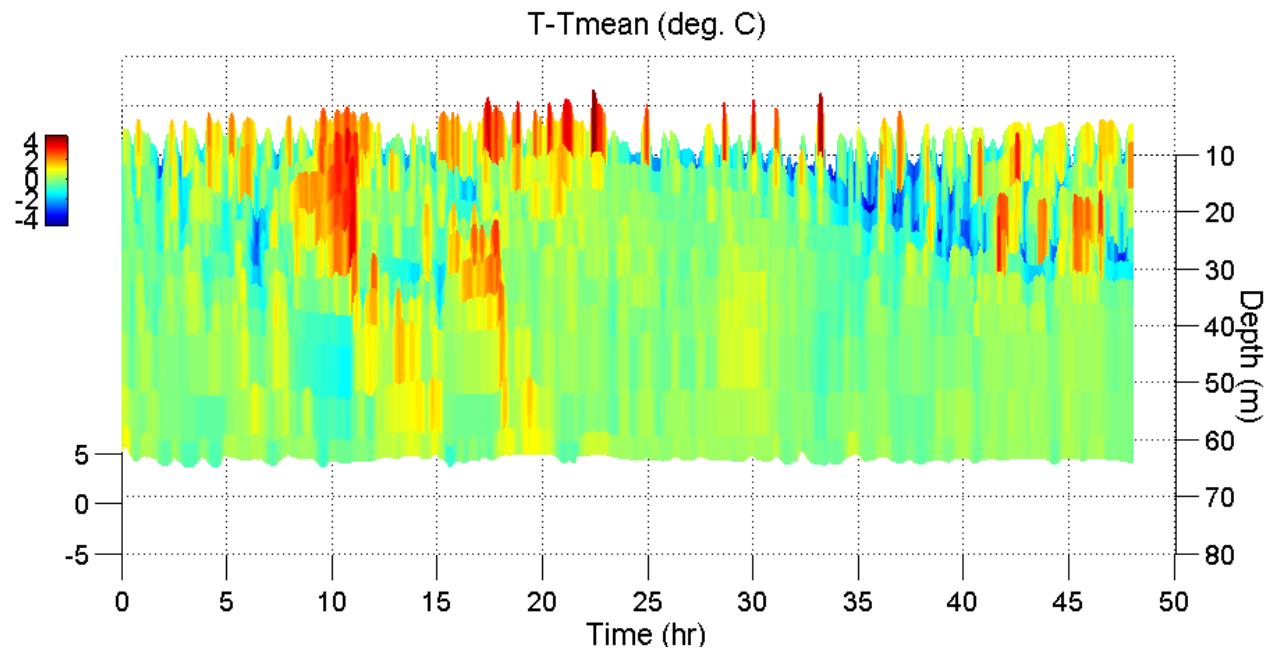
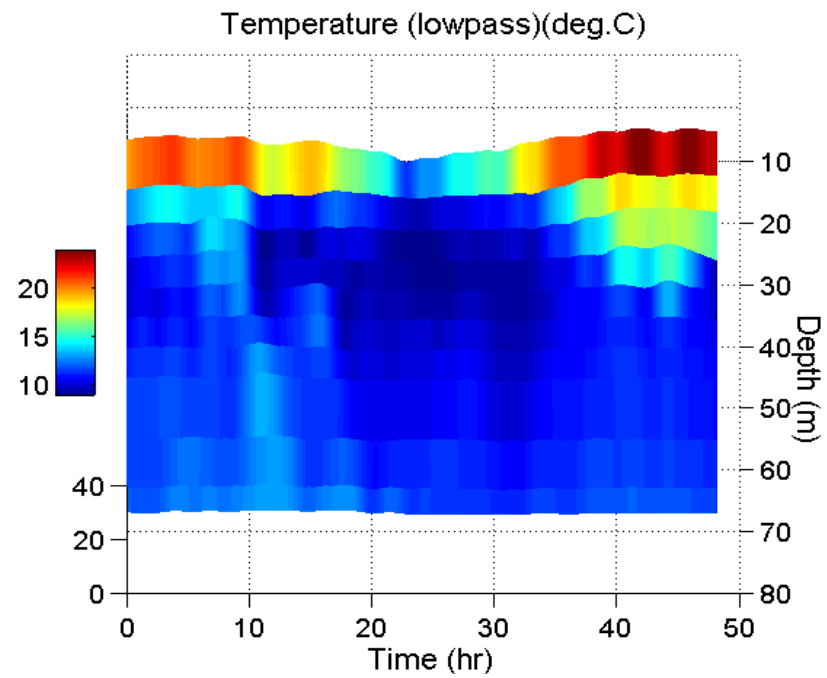
SBRB arrival  
 800Hz. mean → 2.8 max → 6.5 minutes  
 400Hz. 4.2 >30  
 200. 15.0 >> 30



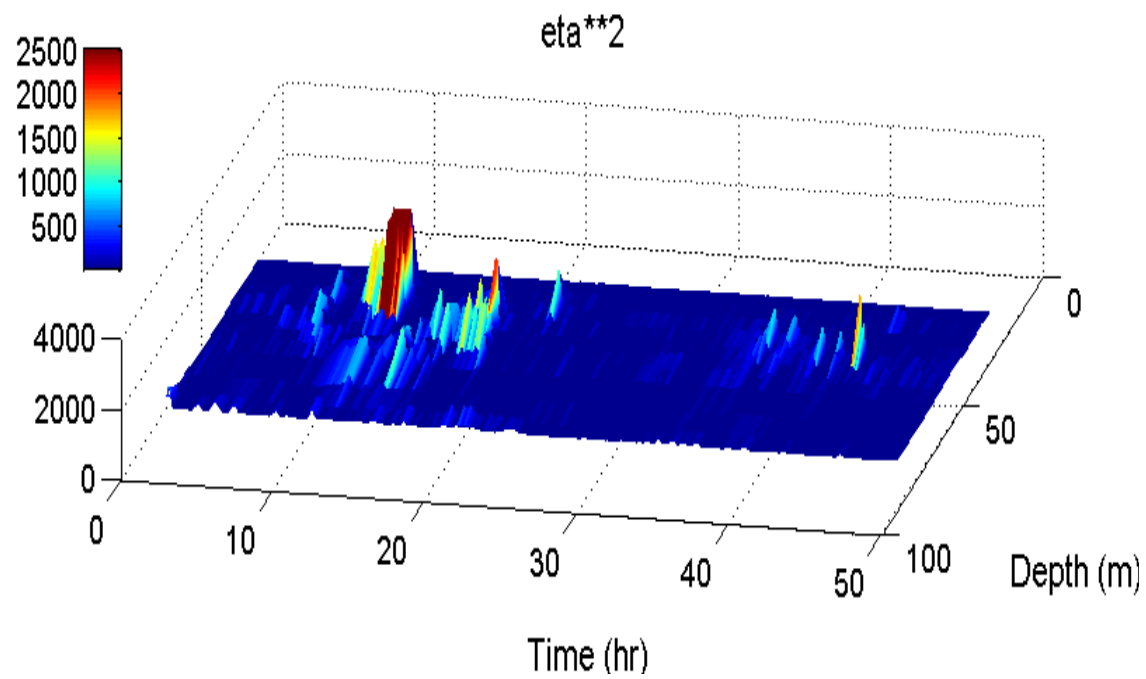
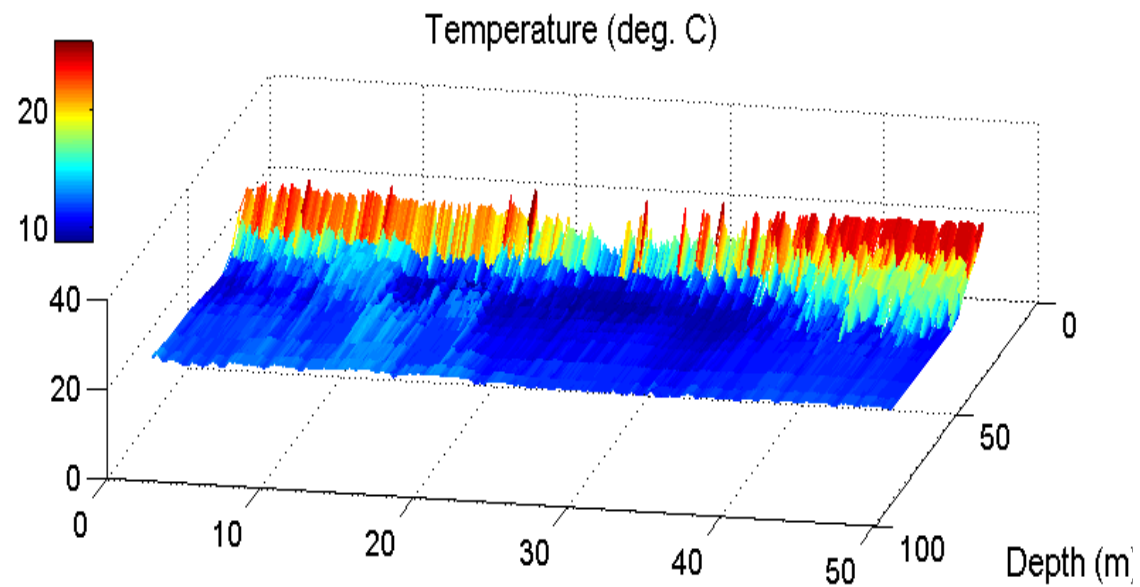
$$PE = (\rho/2)\eta^2 N^2,$$

Where, N is the buoyancy frequency,

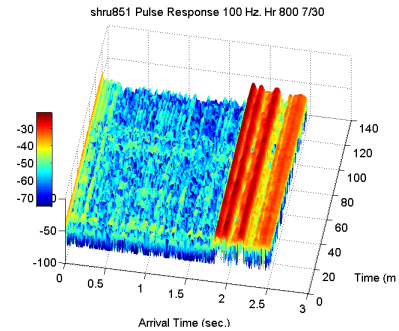
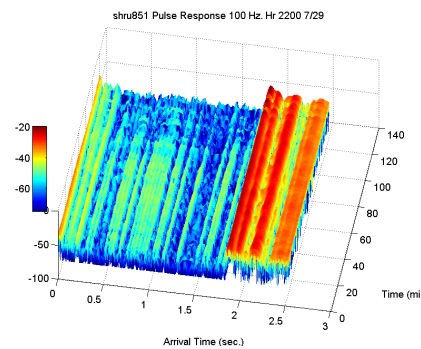
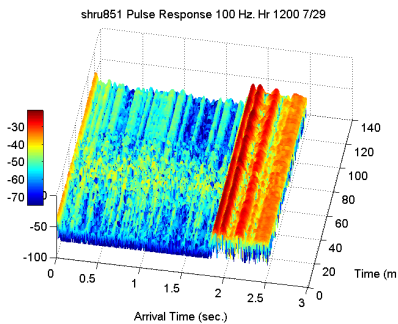
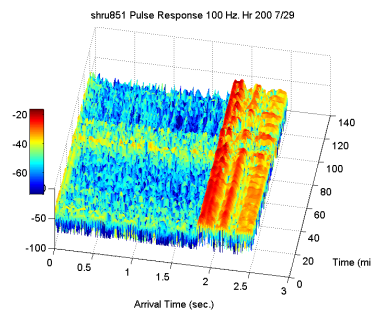
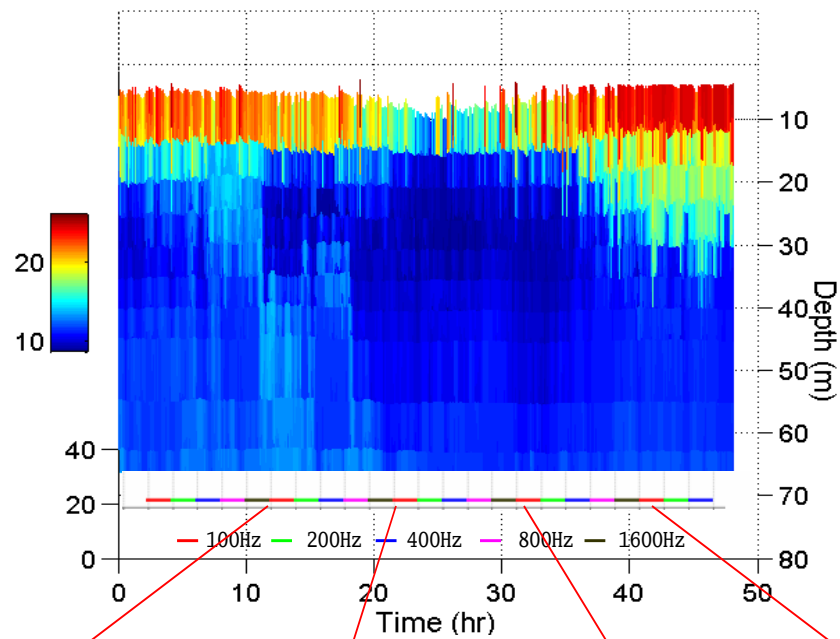
$$\text{and } \eta = T' / dT / dz .$$



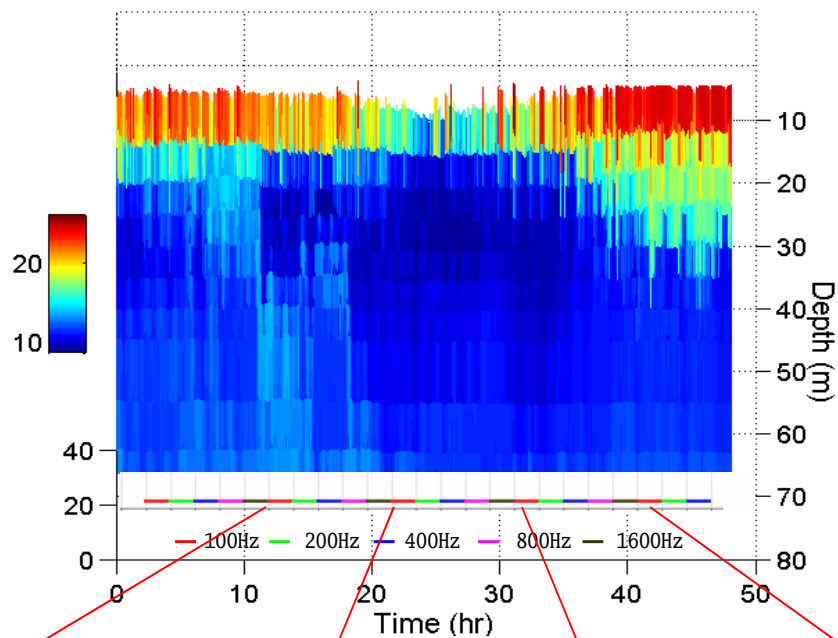
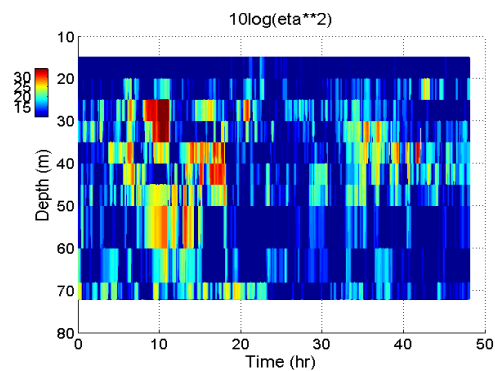




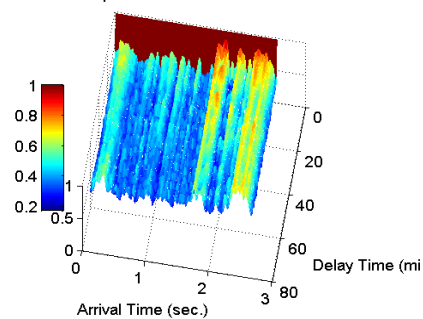
Temperature (deg. C)



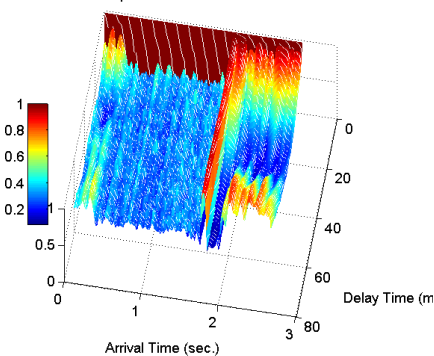
Temperature (deg. C)



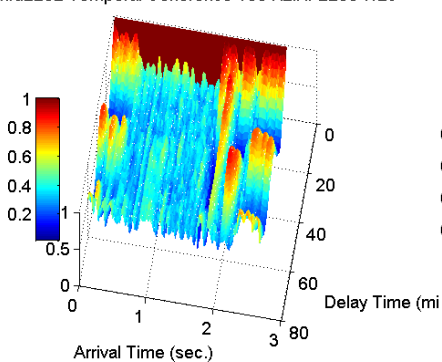
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



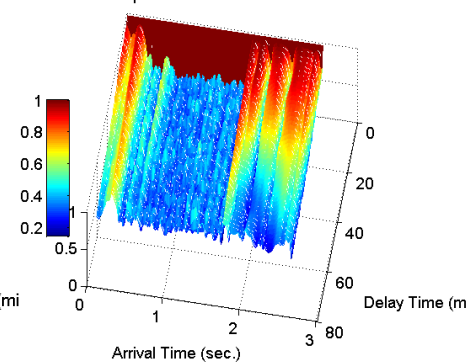
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



shru2252 Temporal Coherence 100 Hz.Hr 2200 7/29



shru852 Temporal Coherence 100 Hz.Hr0800 7/30



# Temporal Coherence and Phase Wrapping

$$COH(t, \tau) = \frac{\left\langle \left( p(t) * p(t + \tau) \right)^2 \right\rangle_{\Delta t, \Delta T}}{\left\langle p(t)^2 \right\rangle_{\Delta t, \Delta T} \left\langle p(t + \tau)^2 \right\rangle_{\Delta t, \Delta T}}$$

Coherence is a statistical measure of the change of a waveform with time

## Causes:

2. Multimode interference
    - Separate modes
  3. Slow phase shifts of undistorted waveform
    - Compute for all phase shifts or phase track.
  4. Random waveform distortion
    - Unrecoverable
- COH varies from both slow phase shifts in time that cause multipath/mode cancellation and from true randomizing effects.
  - Both usually happen at the same time (Phase wrapping, Flatte)

## Removing Phase Wrapping

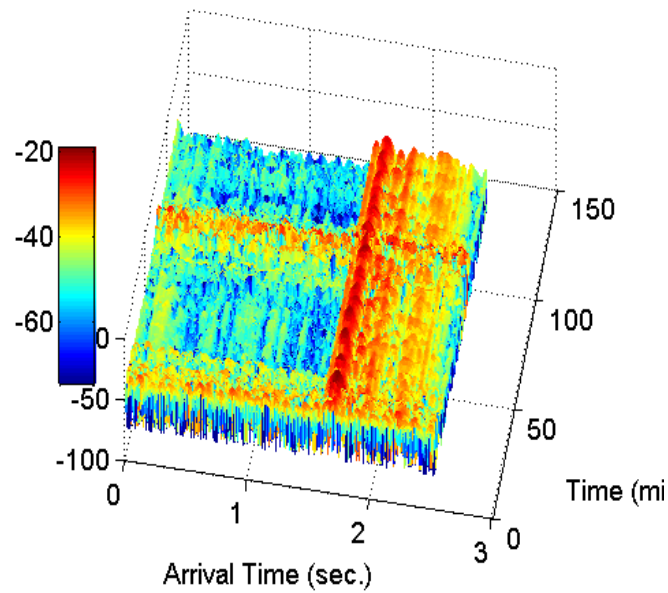
Approach:

- Back out dT/dt
- Loop through small increments of linear time shifts and re-compute COH
- Look for maximum.

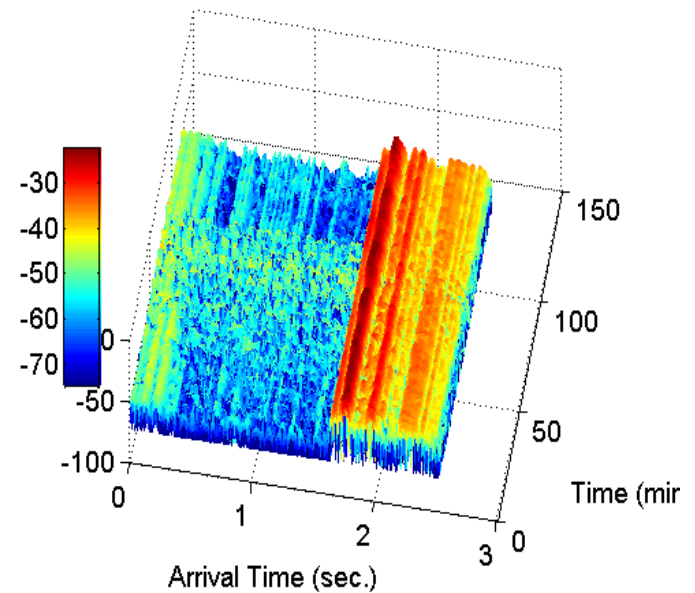
Each pulse  $p(t)$  is time shifted by  $\tau$  using the shifting theorem.

$$F^{-1}\left(F(p(t))e^{i\omega\tau}\right)$$

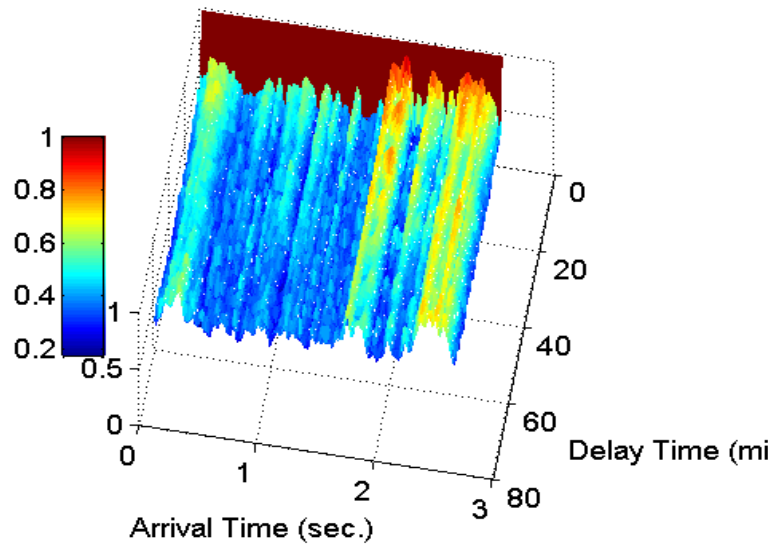
shru852 Pulse Response 100 Hz. Hr 200 7/29



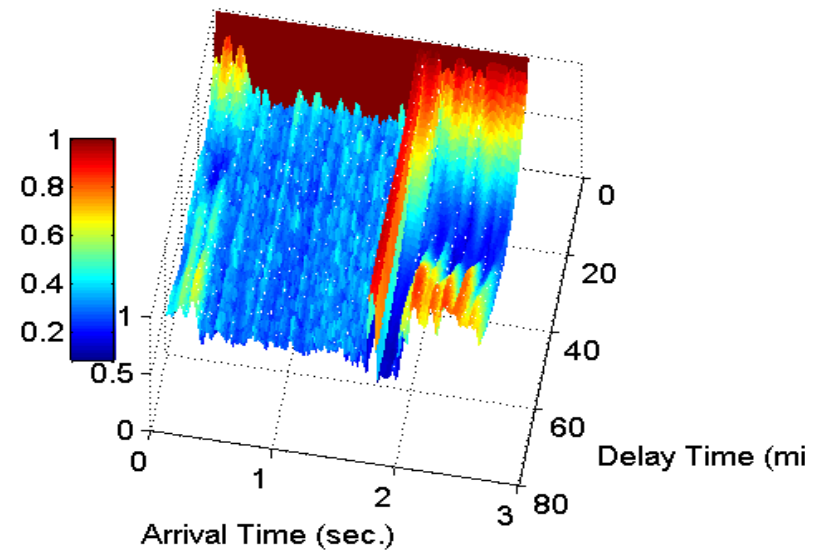
shru852 Pulse Response 100 Hz. Hr 1200 7/29



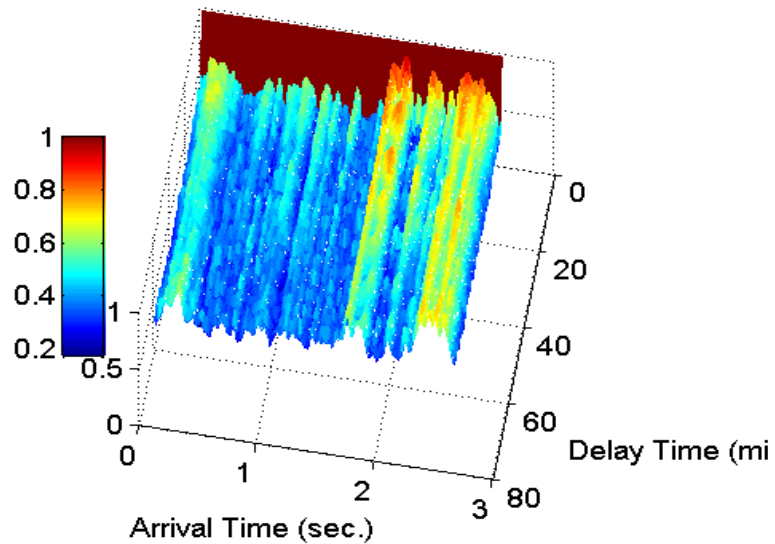
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



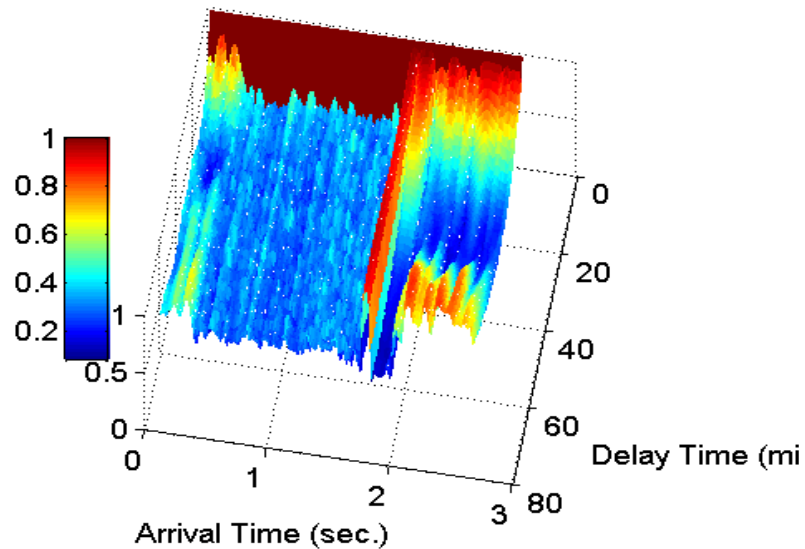
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



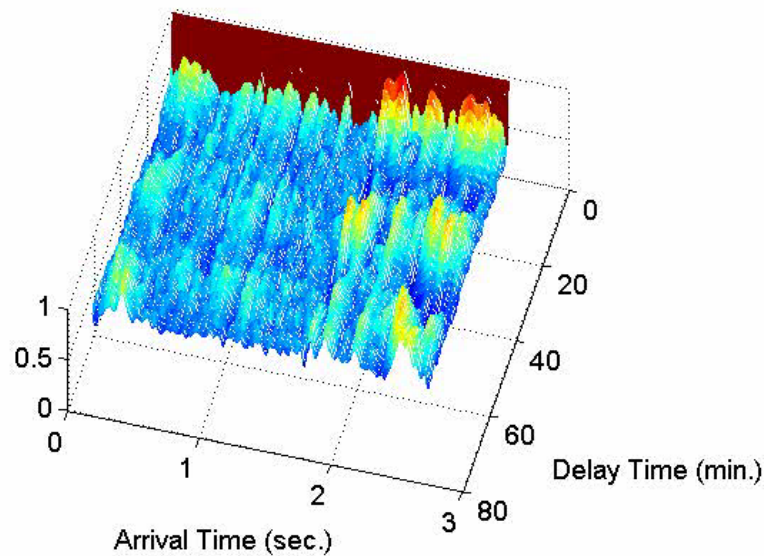
shru852 Temporal Coherence 100 Hz.Hr0200 7/29



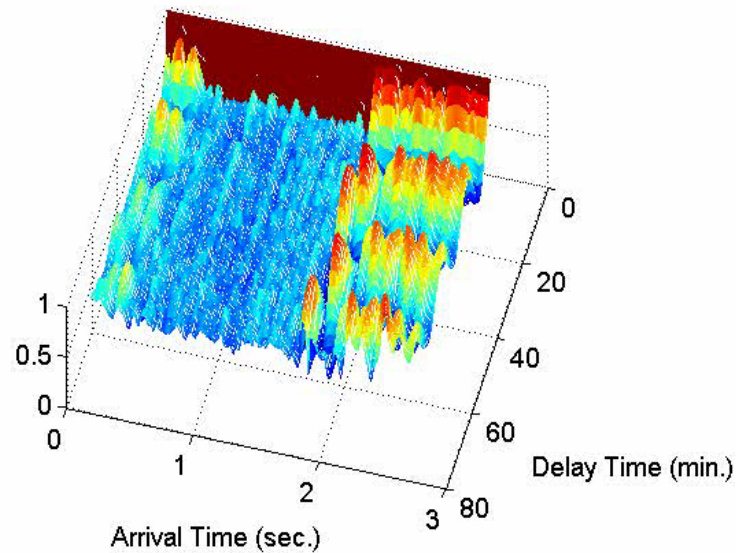
shru852 Temporal Coherence 100 Hz.Hr 1200 7/29



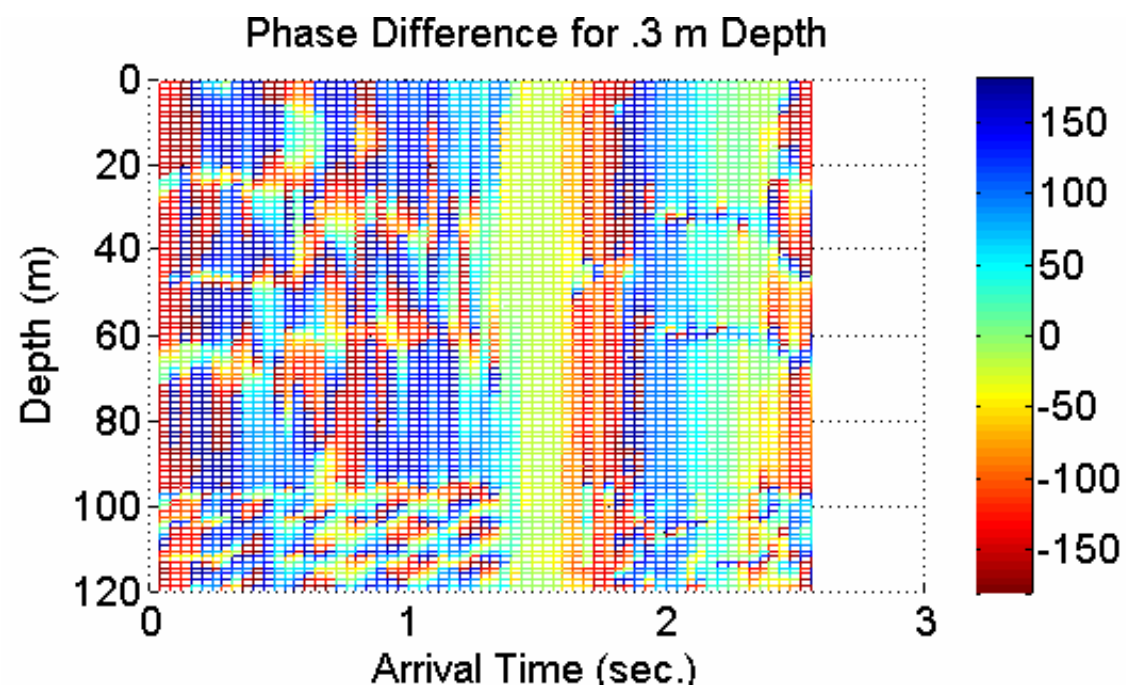
shru252 Temporal Coherence 100 Hz.



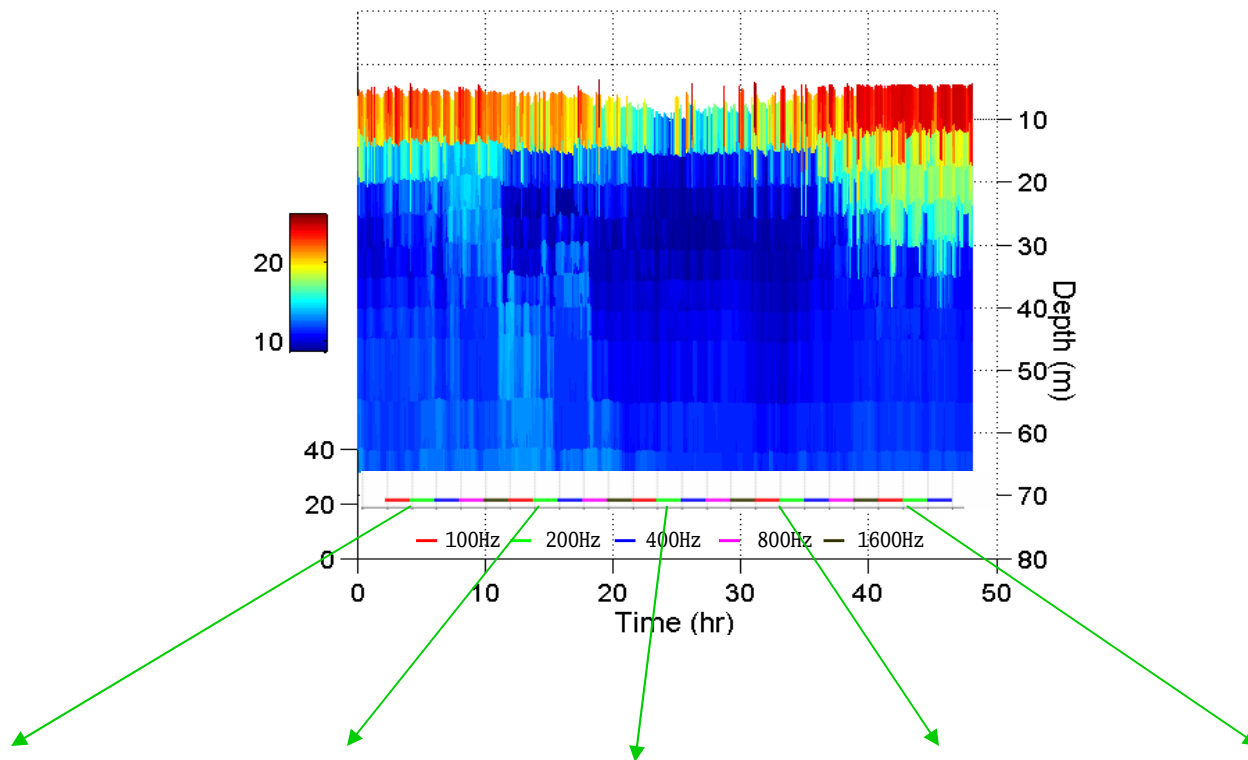
shru853 Temporal Coherence 100 Hz.



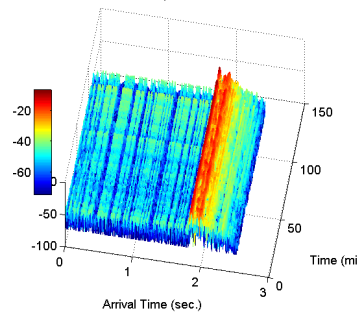




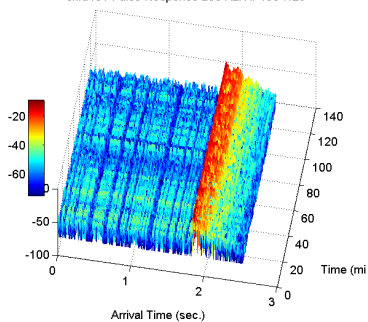
Temperature (deg. C)



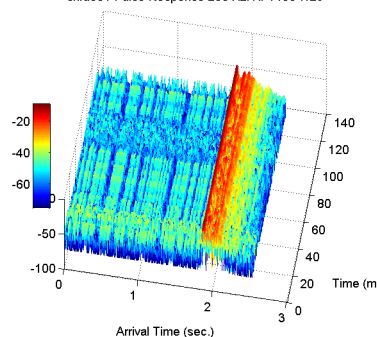
shru1851 Pulse Response 200 Hz. Hr 1800 7/28



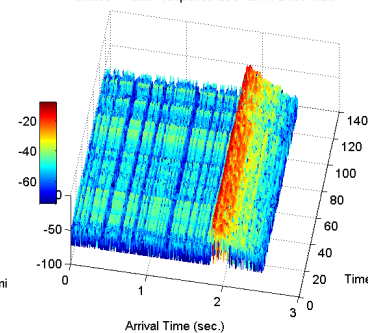
shru451 Pulse Response 200 Hz. Hr 400 7/29



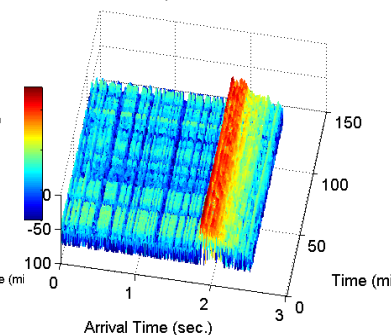
shru051 Pulse Response 200 Hz. Hr 1400 7/29



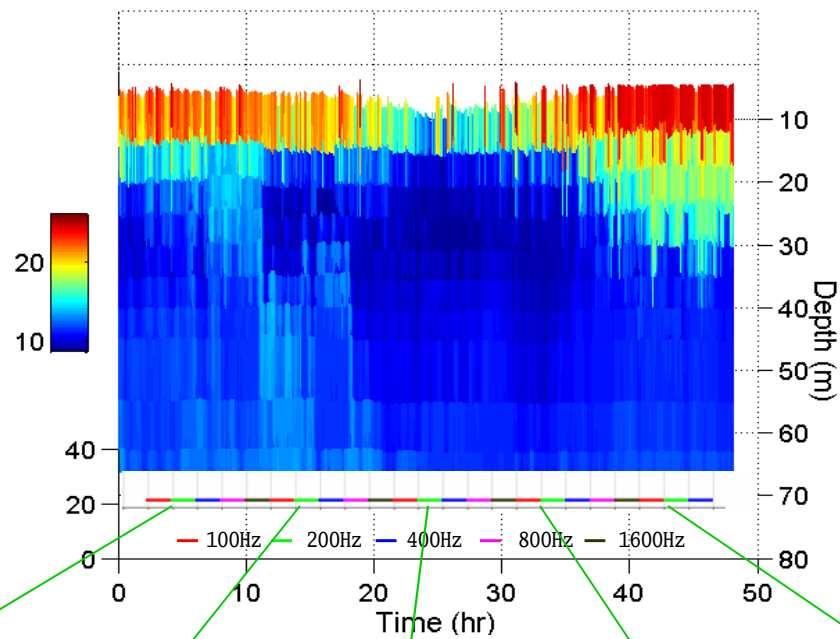
shru051 Pulse Response 200 Hz. Hr 2400 7/29



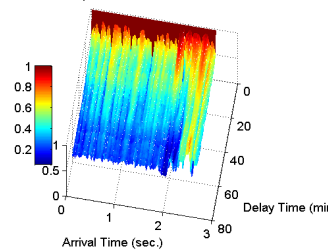
shru1051 Pulse Response 200 Hz. Hr 1000 7/30



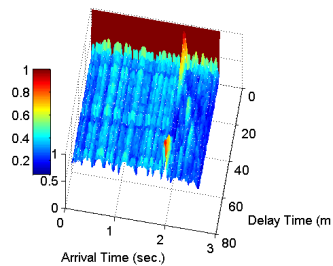
Temperature (deg. C)



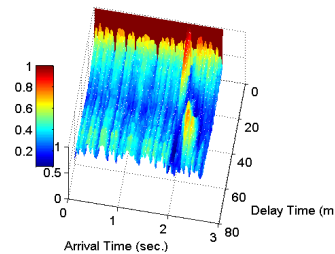
shru1851 Temporal Coherence 200 Hz. Hr 1800 7/28



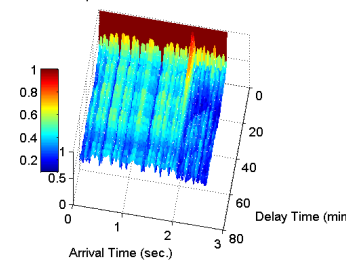
shru451 Temporal Coherence 200 Hz. Hr 400 7/29



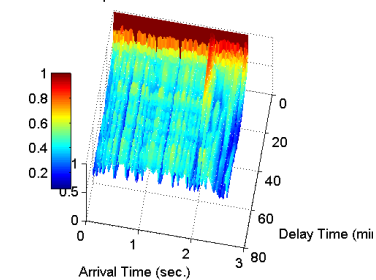
shru051 Temporal Coherence 200 Hz. Hr 1400 7/29



shru051 Temporal Coherence 200 Hz. Hr 2400 7/29

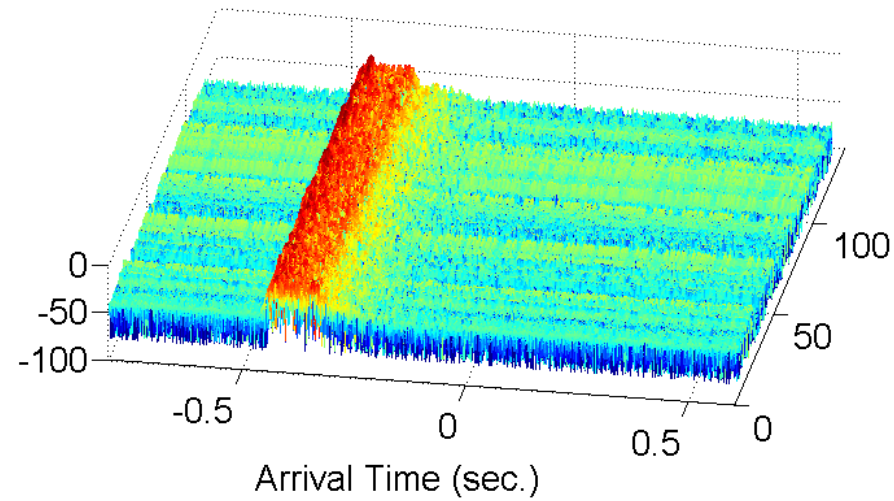


shru1051 Temporal Coherence 200 Hz. Hr 1000 7/30

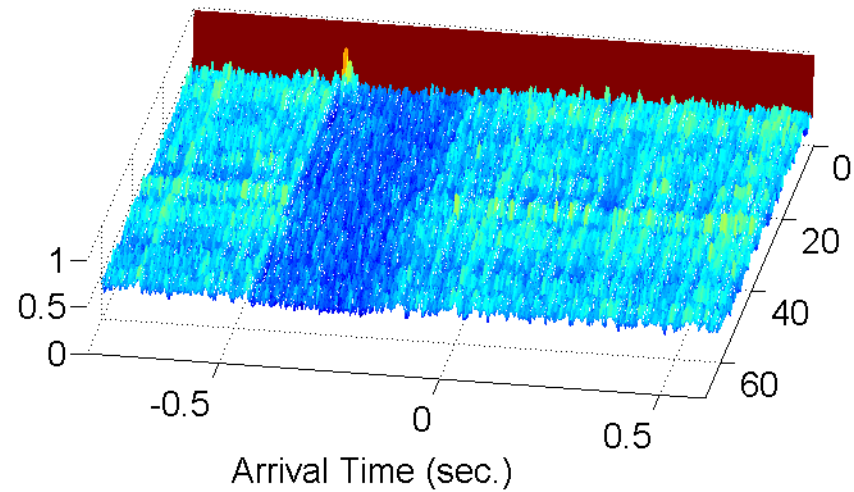


## 800 Hz.

shru3 sw53 Pulse Response 800 Hz.



shru3 sw53 Temporal Coherence 800 Hz.



# Temporal Coherence

Low Frequency  $< 100$  Hz.

- Bottom appears smooth.

- No mode distortion from scattering

- IW caused mode coupling is evident.

Mid – Frequencies  $100 >, < 800$  Hz.

- Bottom scattering become important.

- Coherence times decrease with frequency

- Coherence times decrease with increasing mode number

High frequency  $> 1000$  Hz.

- Signals are randomized by bottom scattering

