

The effects of non-linear internal wave curvature on acoustic propagation

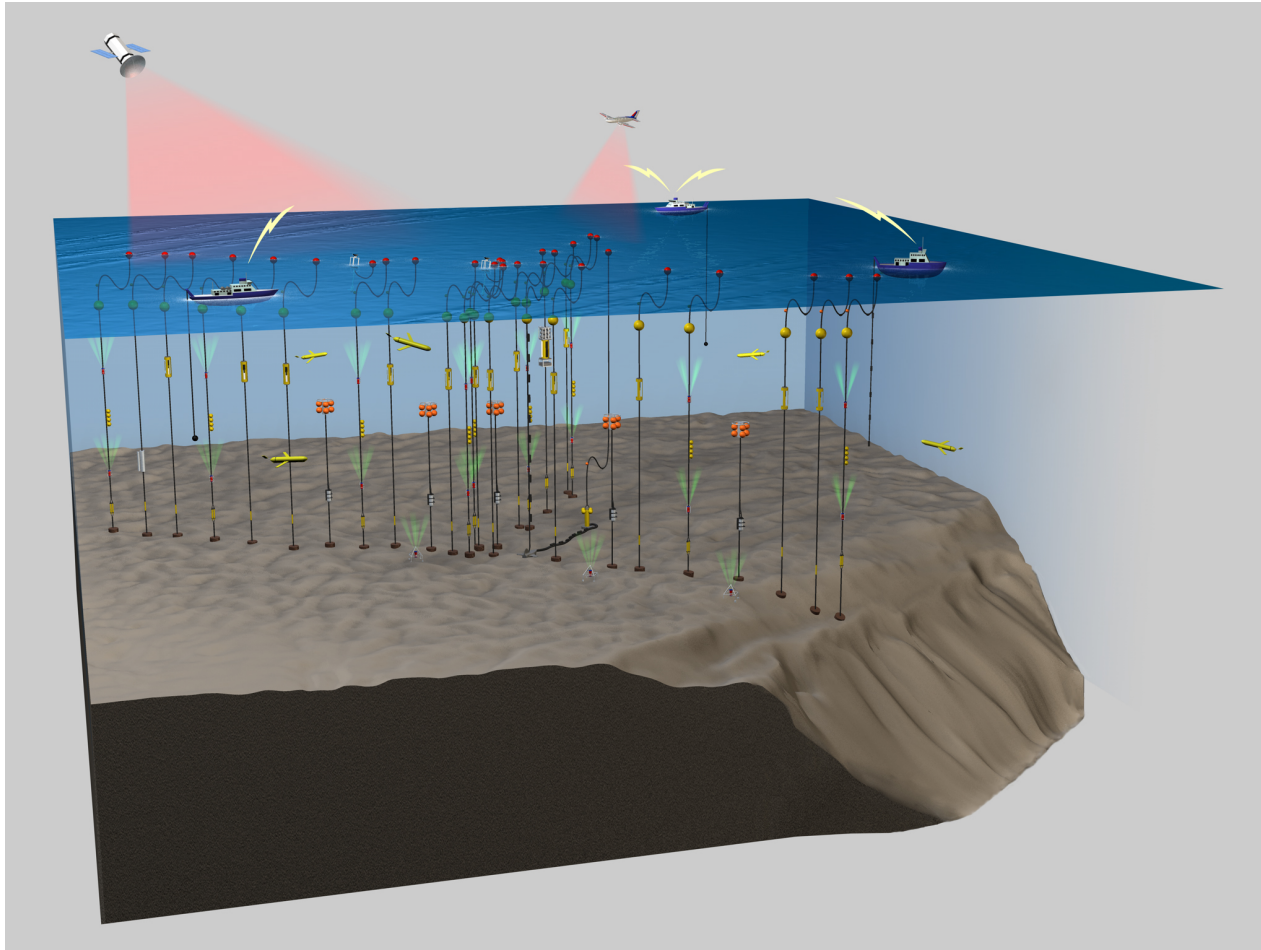
Jim Lynch, Tim Duda, Ying-Tsong Lin,
Art Newhall, Mike Caruso, and Hans
Graber

WHOI and U. Miami

Lots of work in past 20 years on acoustics and IW's

- BSPF (1992)
- SWARM (1995)
- PRIMER (1996-97)
- ASIAEX (2000-01)
- NEST (2007-08)
- SW06 (~2006)

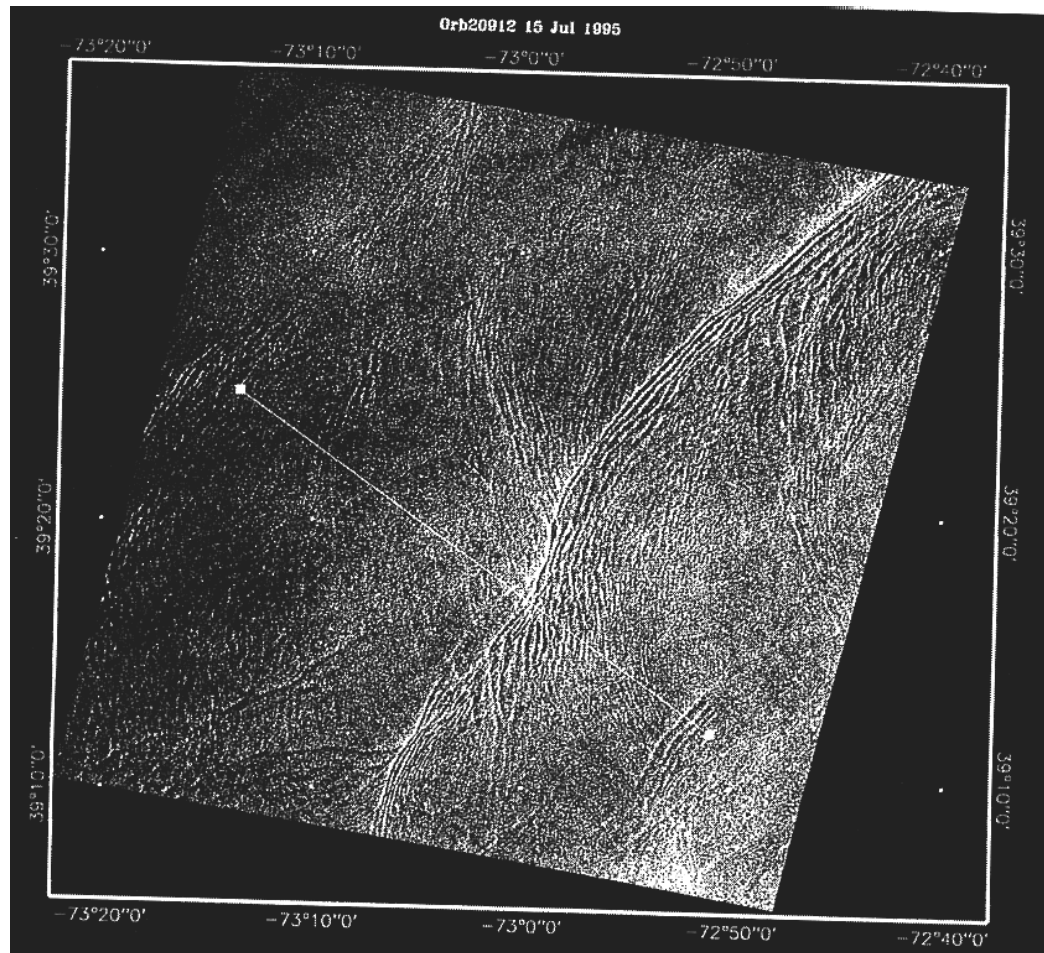
SW06 3-D View



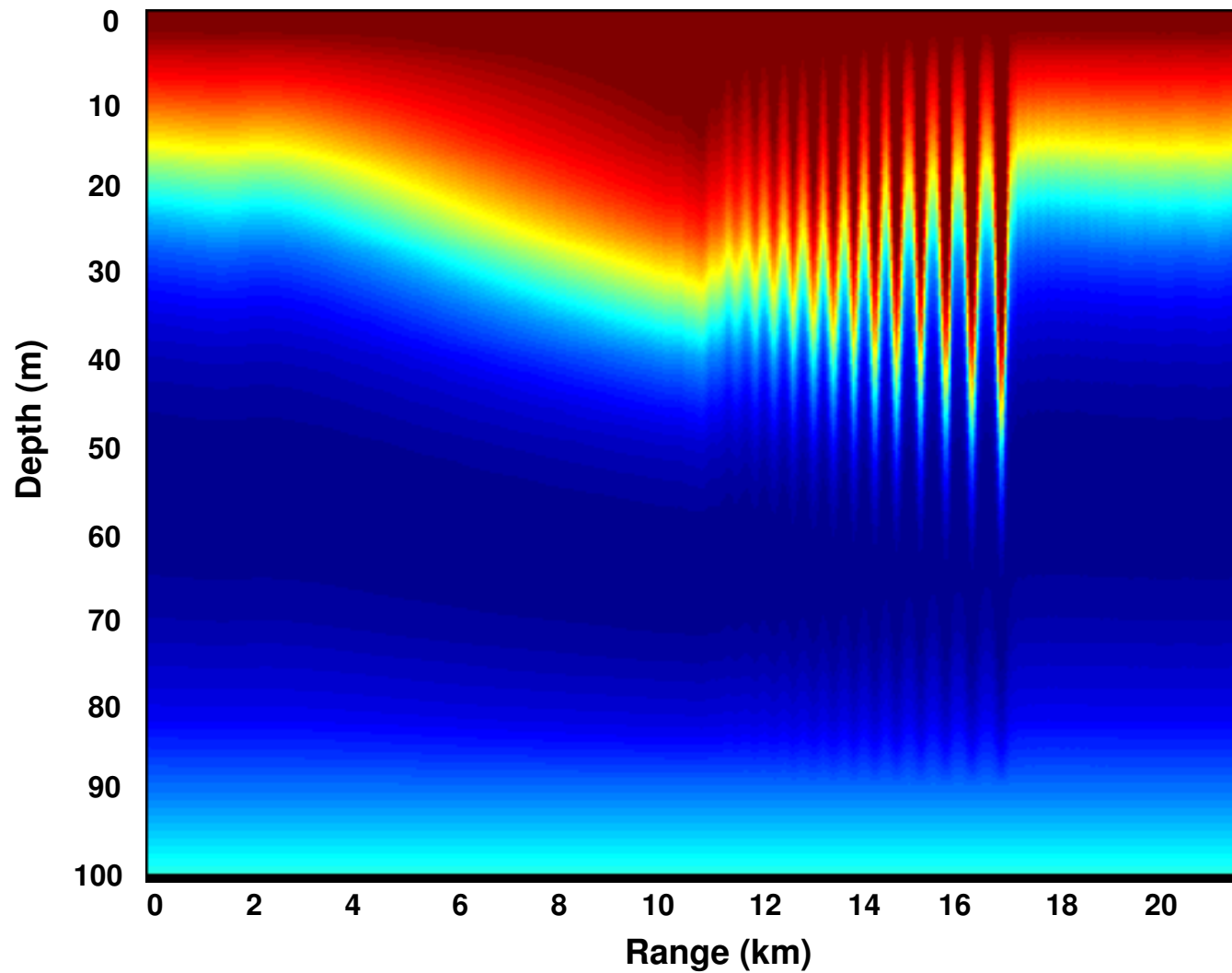
What are the big issues??

- TL and its fluctuations
- Fully 3-D acoustics - not just slices of 3-D ocean – and direction of arrivals
- Array coherence
- Inversion for bottom in presence of fluctuating ocean
- Others...

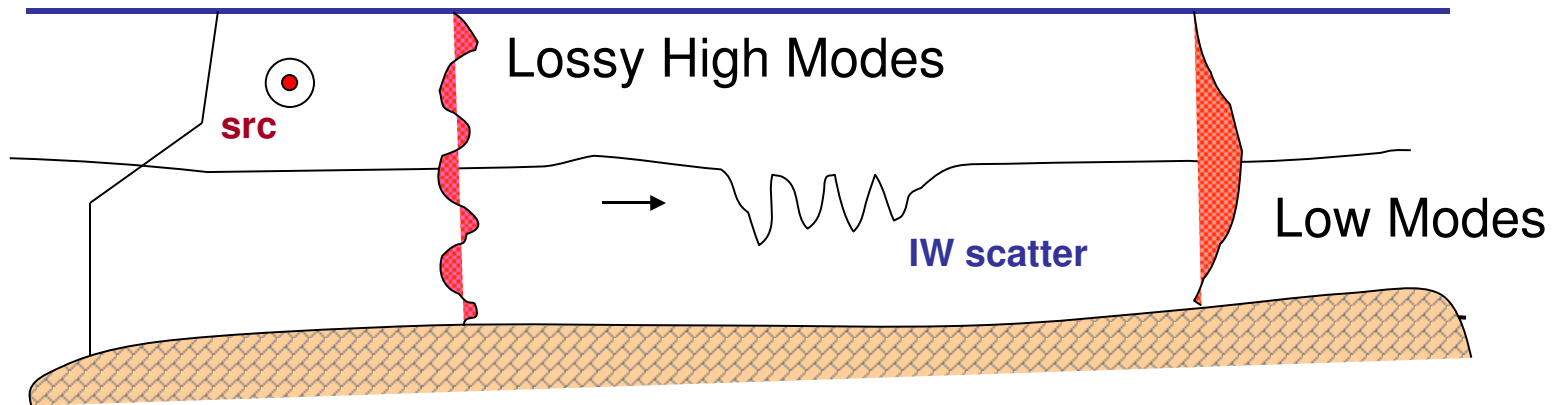
Started with SWARM - Cross Shelf



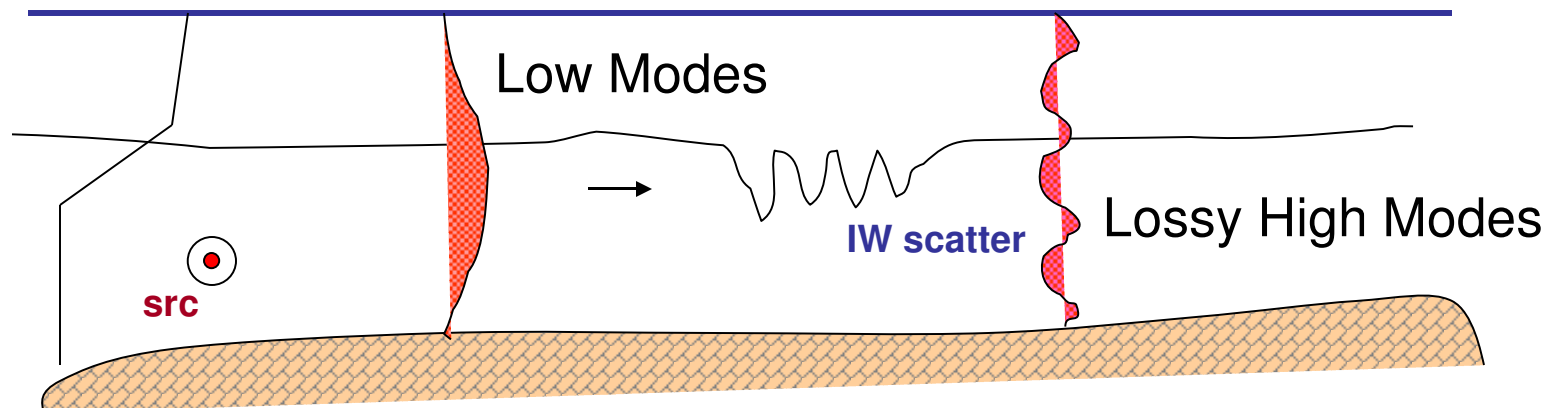
Solibore Simulation



IW Induced Coupled Propagation Gain/Loss Cases

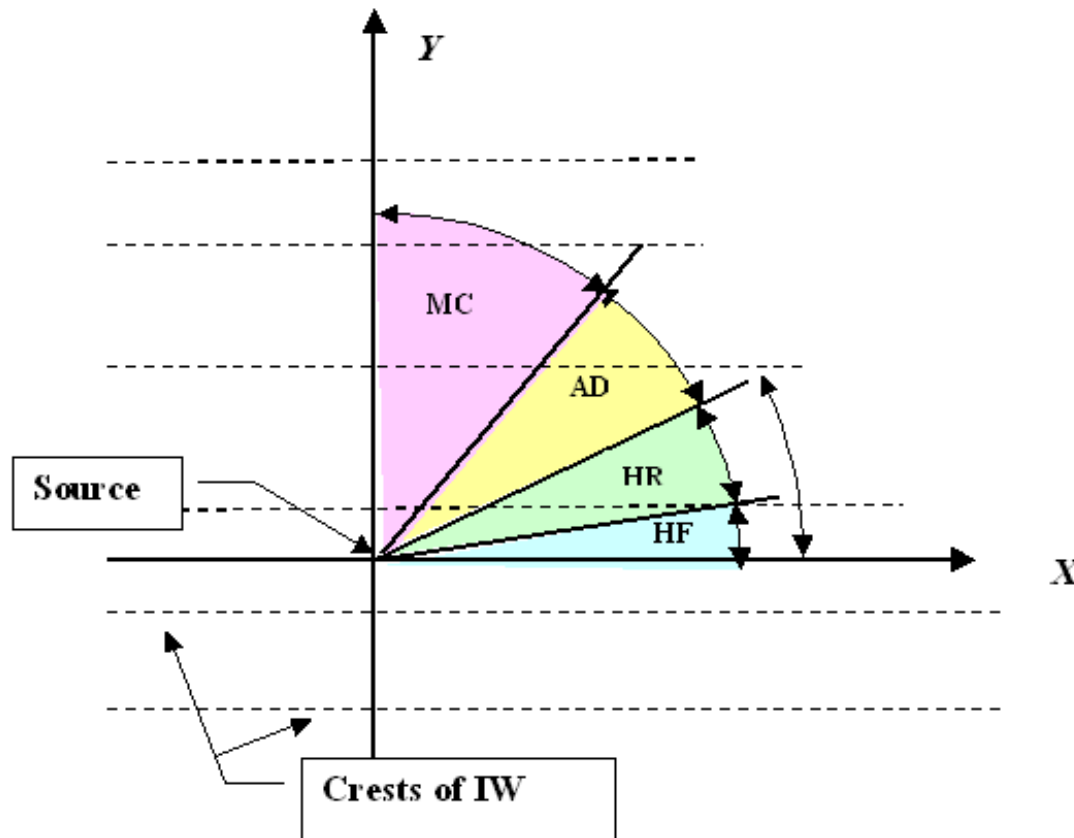


PRIMER Noise Case – Net Amplification



Zhou Yellow Sea Case – Net Attenuation

Evolution - Boris' IW Master Plan!



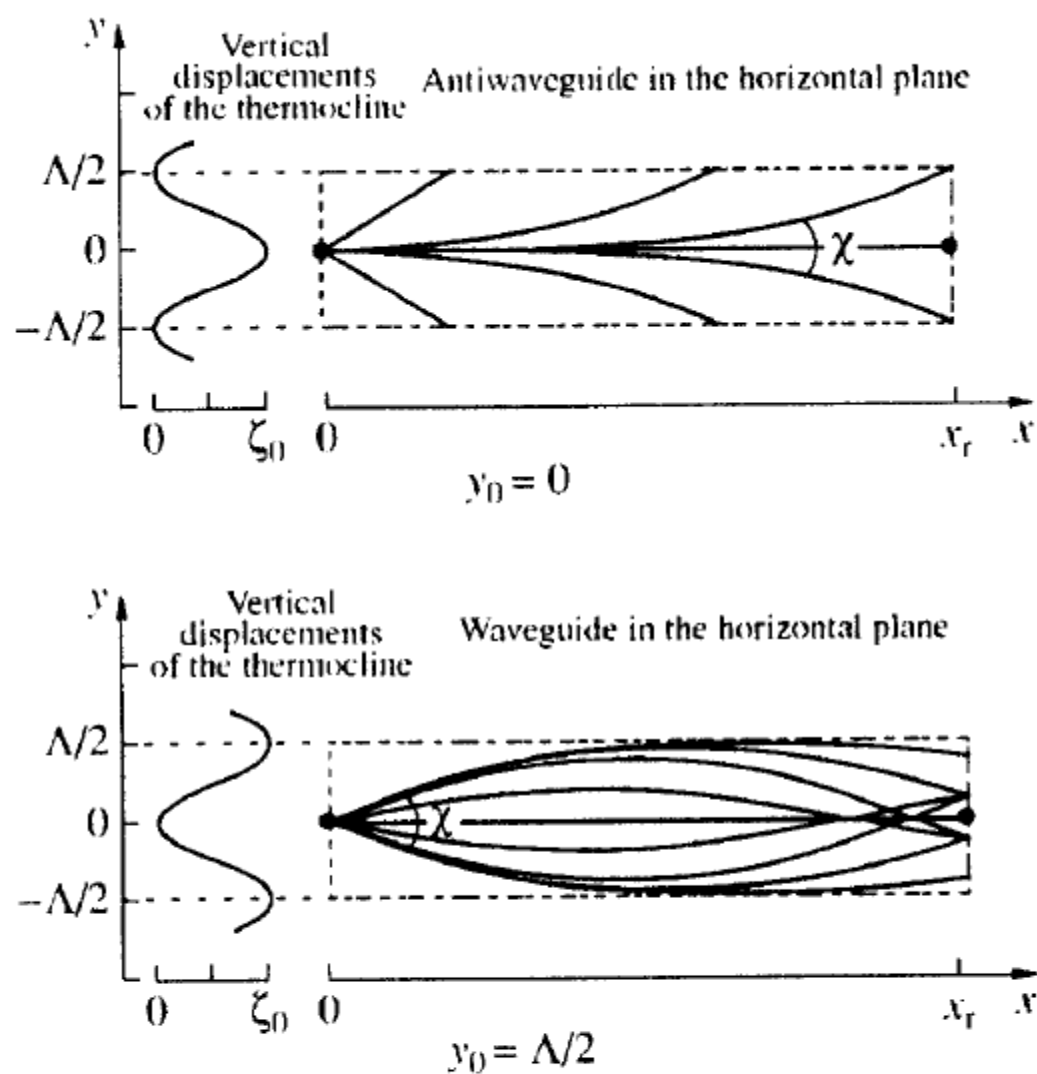
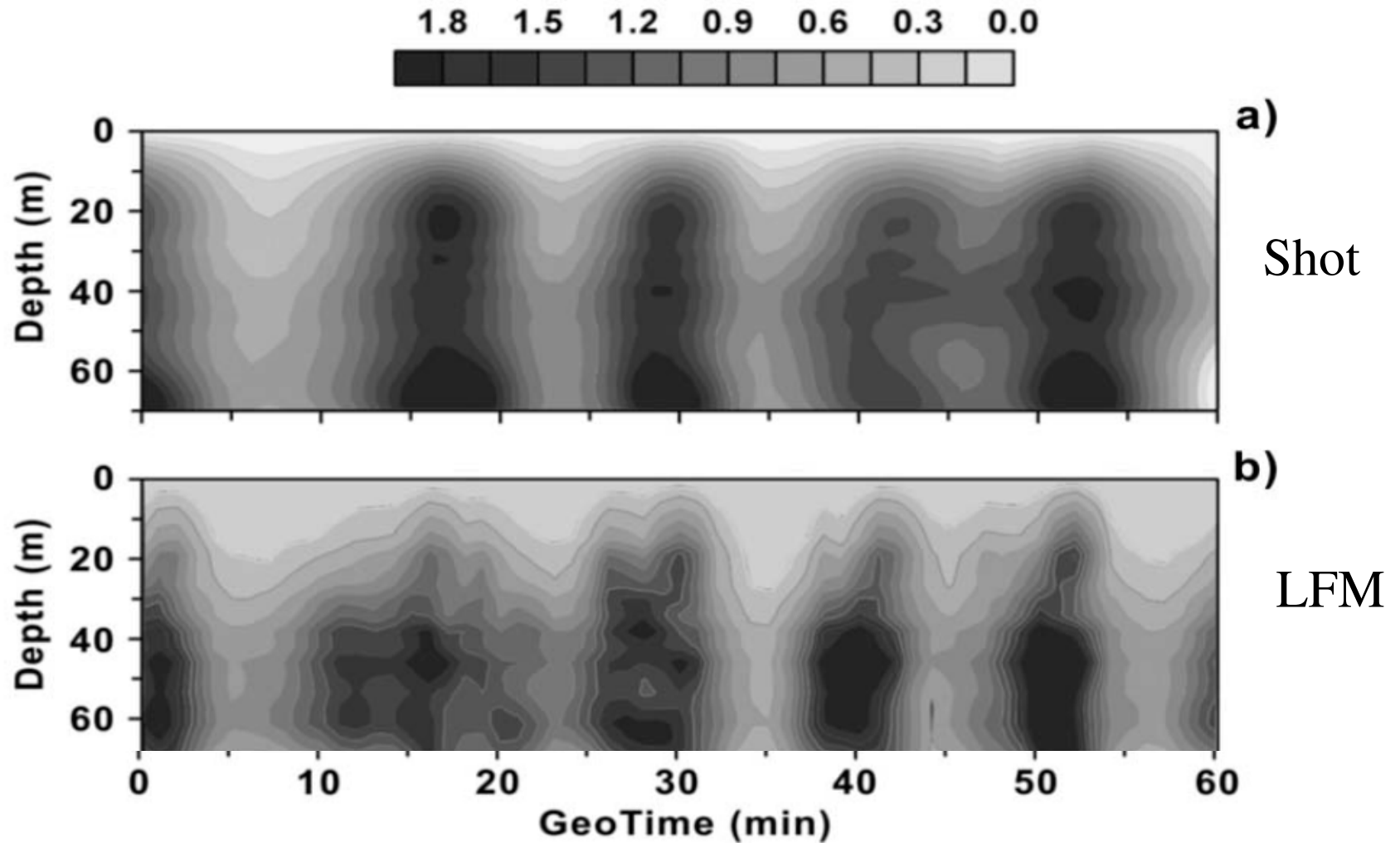


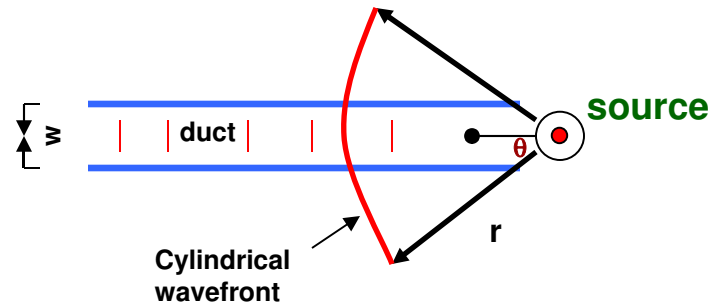
Fig. 2. Ray patterns in the horizontal plane for the case of a plane front of soliton packets. The dependence of the thermocline displacement on the transverse coordinate is shown on the left.

Temporal dependence of the sound energy for different depths in intensity gradation (relative units)



**Mean intensity increase due to ducting
(no spreading vs. cylindrical spreading)**

For IW duct, have geometry



$$R = \text{Ratio of areas} = r\theta_c/w$$

IW duct ($r_1=20$ km, $w = 1$ km, $\theta_c = 7.5^\circ$)

$$10 \log R = 7.18 \text{ dB}$$

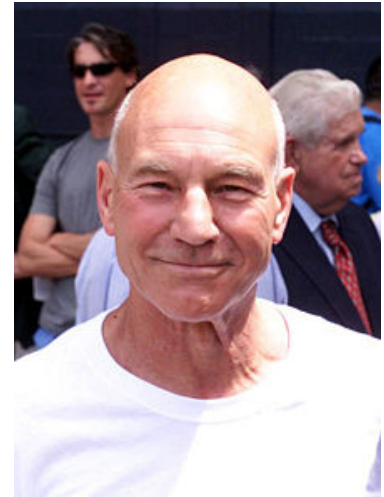
7-8 dB is a lot for sonar systems!! (And is observed))

IW Trek – The Next Generation

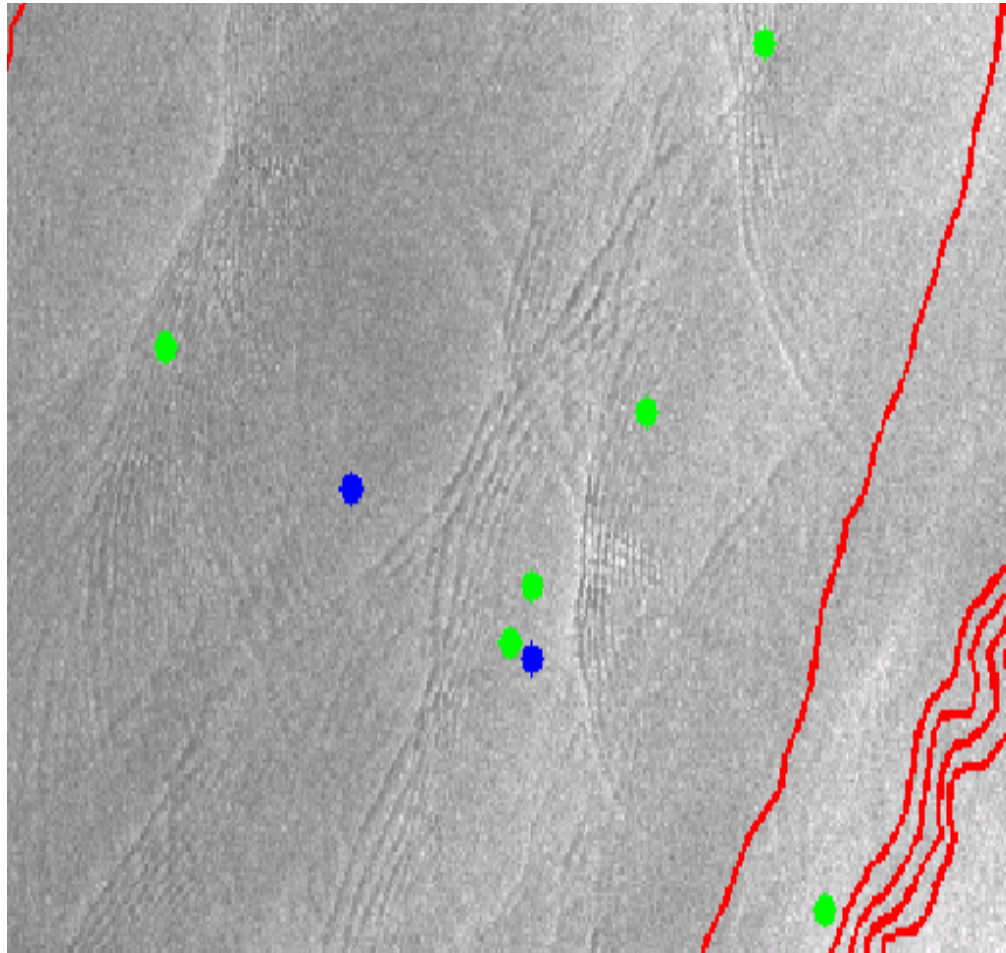
New IW Features to
Include....**funkier!**



Curved IW's
Terminating IW's
Field of IW's with
horizontal decorrelation
Horizontal Lloyd's Mirror
Crossing Wave Trains



So much for infinite plane waves...



First port of call - curvature

- First theory – Katznelson
- Computer models – Duda, Lin, et al
- Ridiculously simplified theory (“For Utter Dummies” version) – Lynch
- Shadowing by circular wavetrains - Lynch

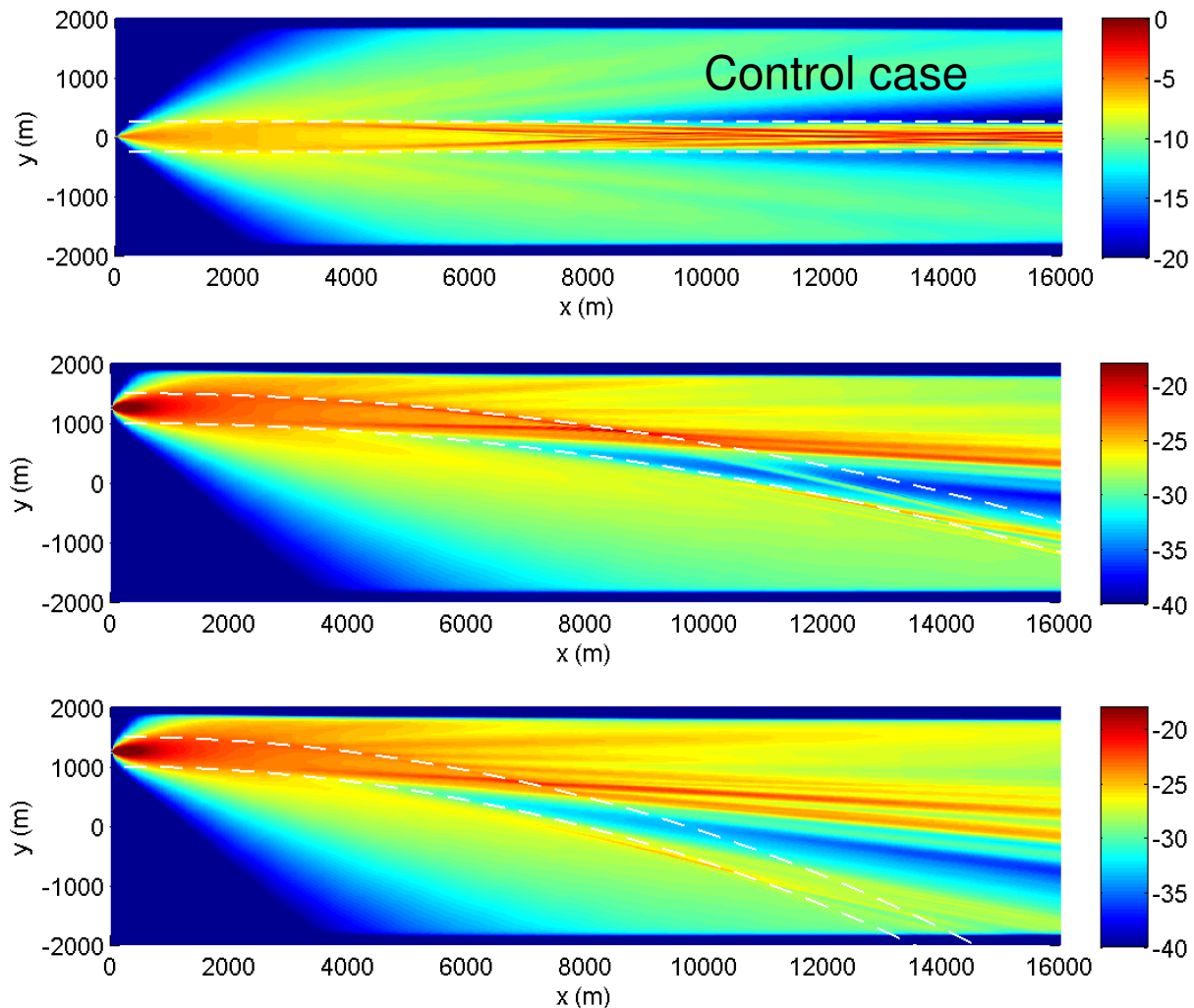
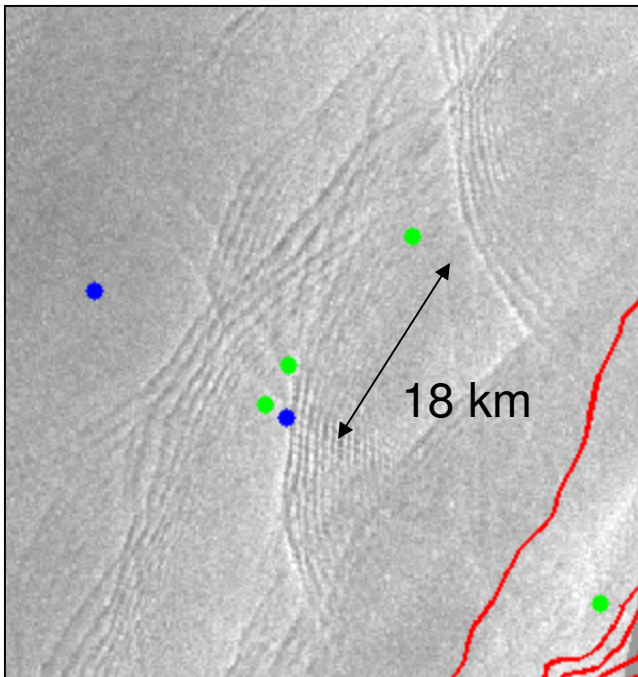
Theory

- Theory for straight and curved IW acoustic ducts first published by Katznelson et al.
- Predicted the ducting by “straight” internal waves seen by Badiey, Lynch in SWARM (1995)
- Uses Weinberg and Burridge “Vertical Modes and Horizontal Rays” 3-D theory
- Formally shows curvature effects in curvilinear coordinates... not easily transparent

Fully 3-Dimensional Curved IW Propagation Simulations

Curved pairs of nonlinear internal waves. Waves scaled to fit SW06 area observations. 200-Hz. Modes separate and beams form.

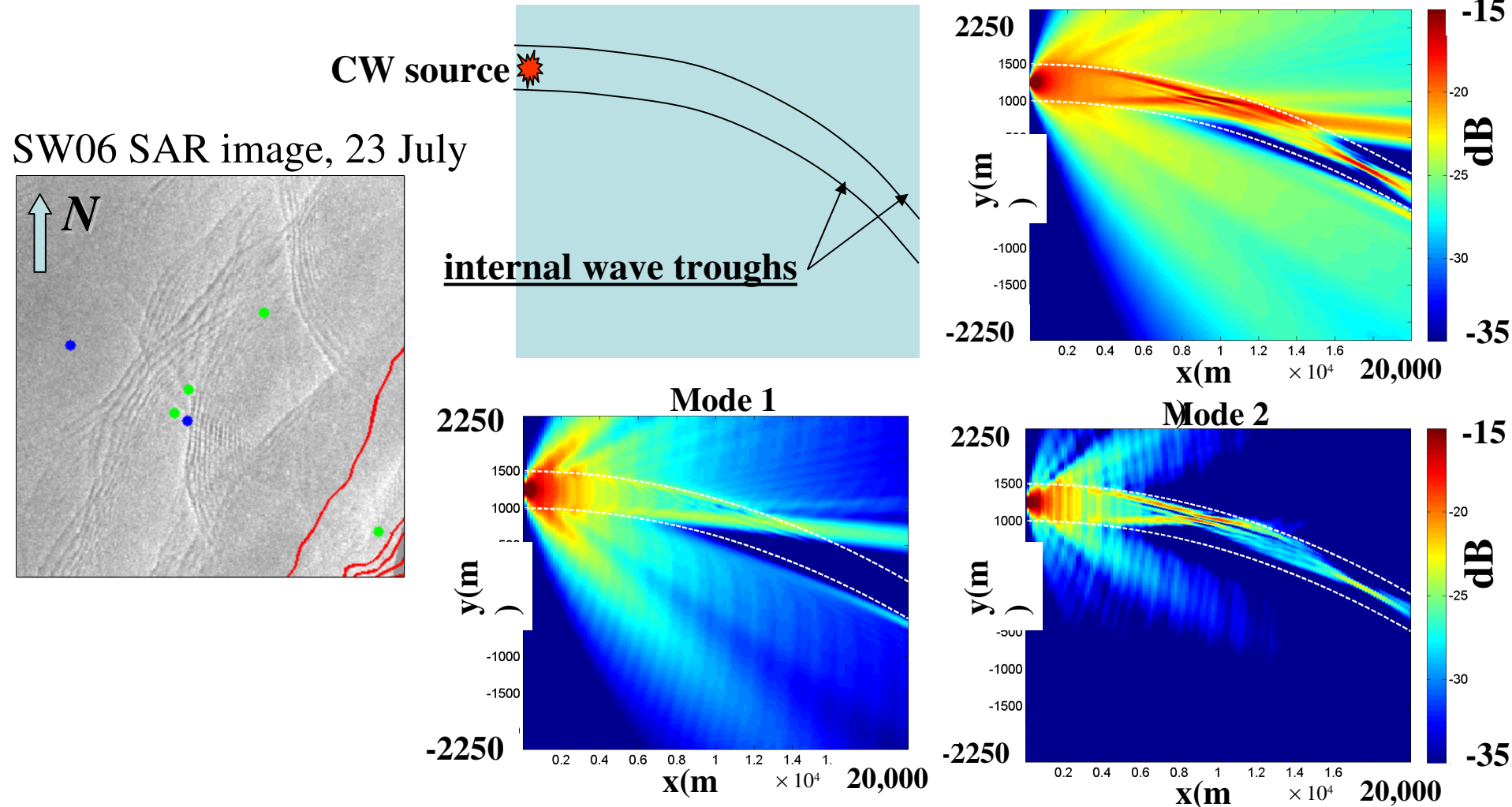
SW06 SAR image, 23 July



Effects of nonlinear gravity internal waves on 3D sound propagation

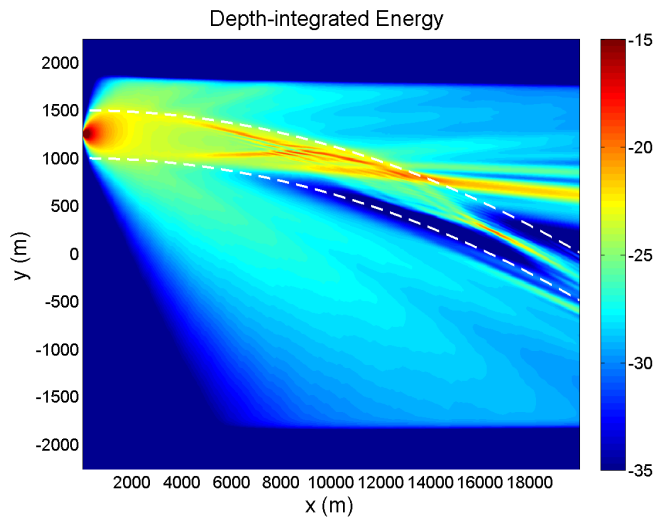
— Acoustic modal focusing in an curved internal wave duct

- Radius of curvature=135km, frequency = 100Hz
- Mode 1 penetrates through internal wave duct, but mode 2 focuses in the duct.

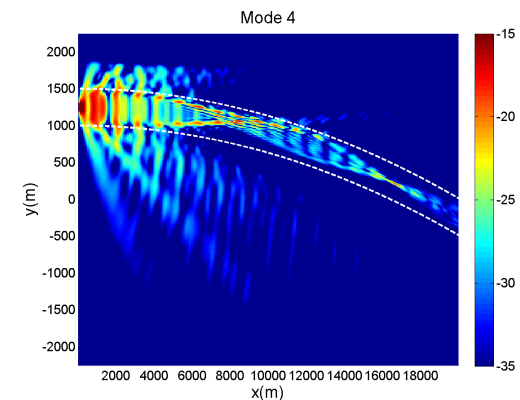
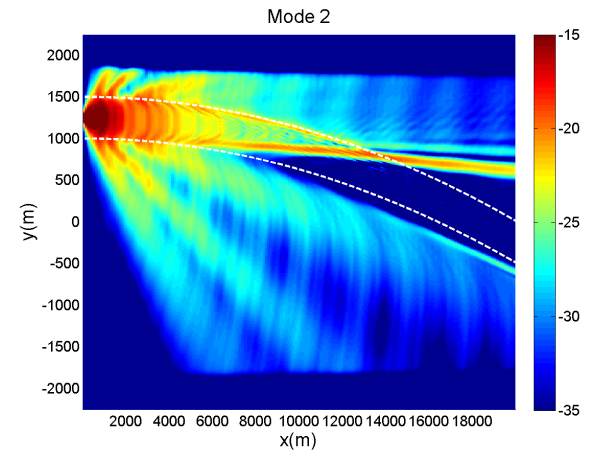


Higher modes trap better—hmmm!

- **Case 2 : curvature=135km, frequency = 200Hz**



- Modes 1 and 2 penetrate through internal wave duct, but modes 3 and 4 focus in the duct.



Some Simple Theory

- Previous work clearly displays frequency and mode dispersion effects, light piping (and leakage from curved pipe), etc.
- But doesn't have simple physical insight into how parameters of problem (frequency, mode number, IW strength, background waveguide structure, etc.) affect trapping and leakage of modes.
- Maybe looking to a simple theory picture is useful?!
- Lynch an excellent choice for *very* simple stuff

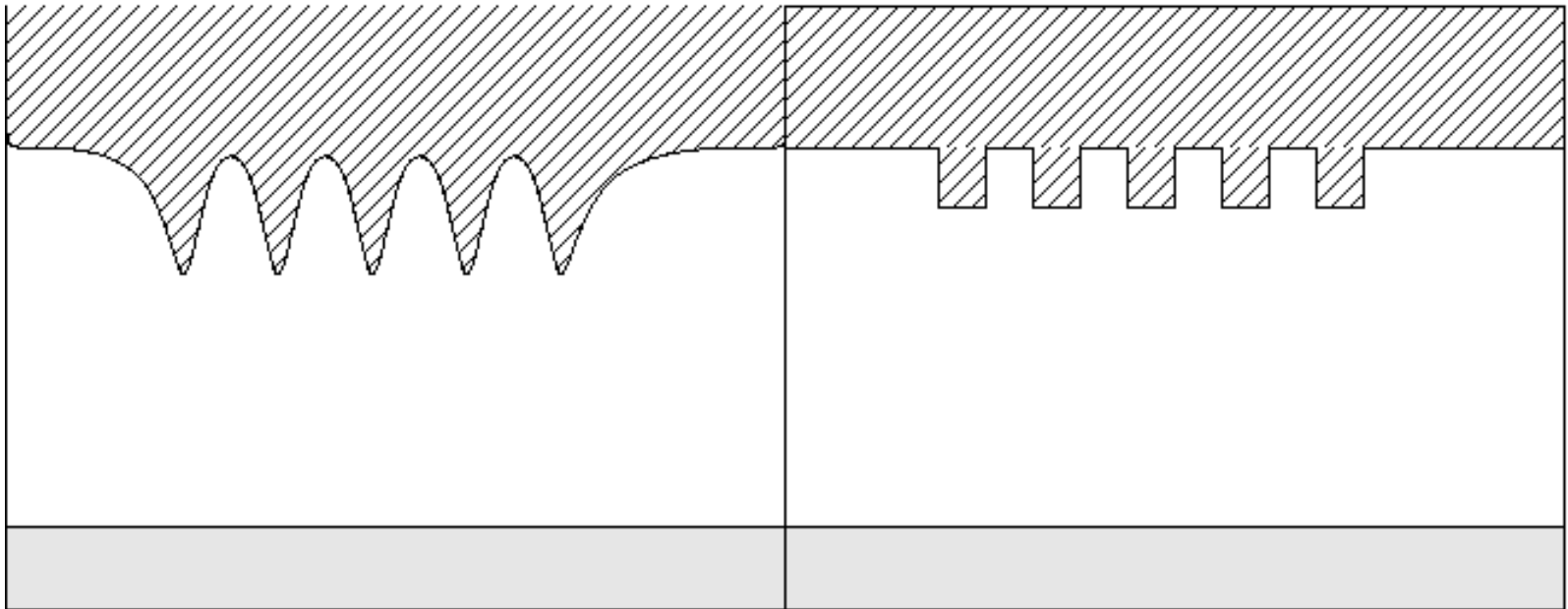
Start with Weinberg/Burridge 3-D horizontal ray/verticalmode theory

- Have a local horizontal index of refraction for each mode at a given frequency

$$n_n(x, y, \omega) = k_n(r) / k_n(0).$$

- After get the index of refraction field by computing the modes at all x,y, then trace rays in the horizontal
- Product of the ray (horizontal) and mode (vertical) gives acoustic field !!!

Trivializing wave trains 101 (and can you spot the missing line)



Simple modal waveguide model

$$\gamma_n H = (m + 1/2)\pi$$

$$k_n = (k^2 - \gamma_n^2)^{1/2}$$

$$Z_n(z) = \frac{2}{H} \sin(\gamma_n z)$$

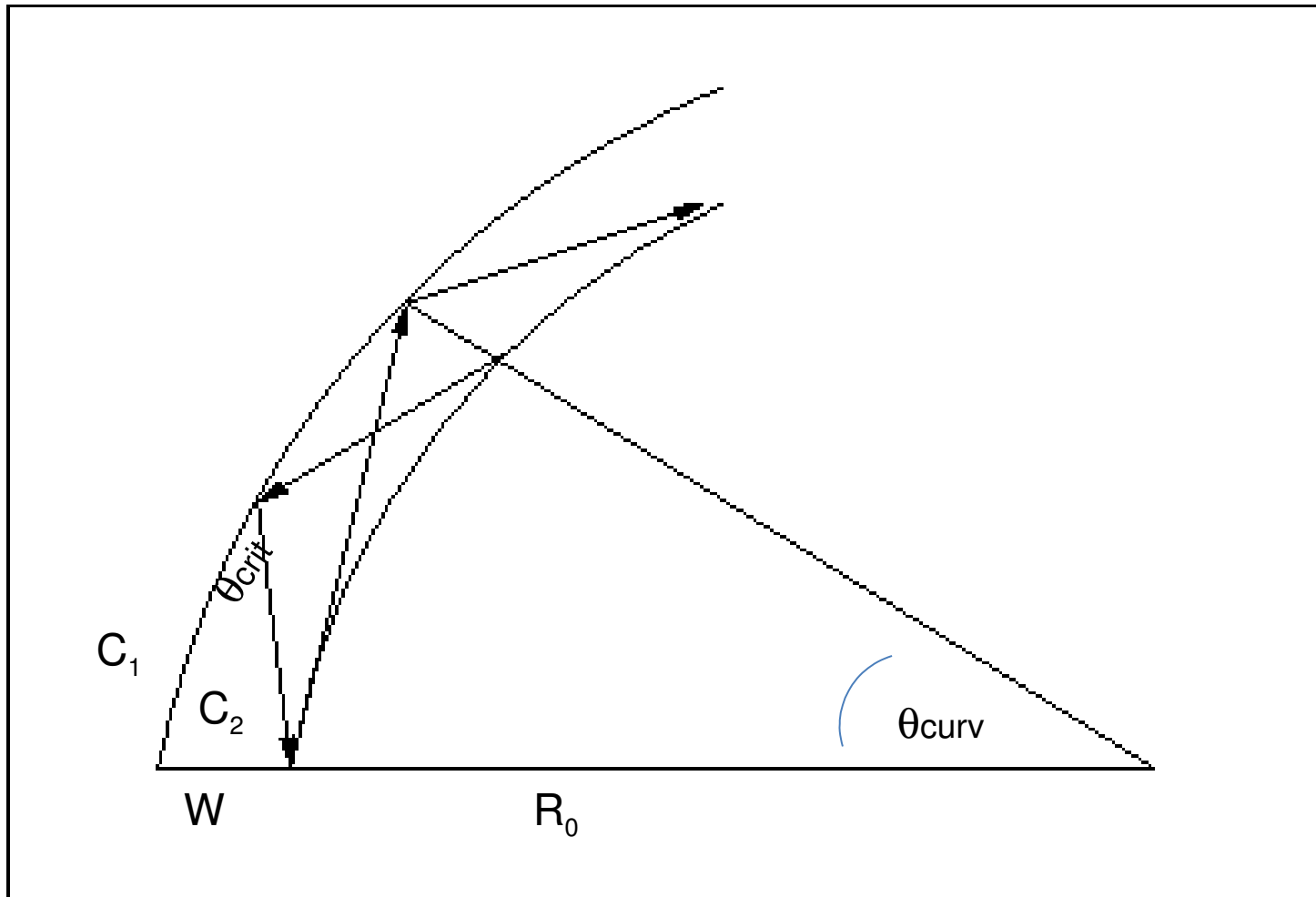
$$\Delta k_n = \frac{1}{2k_n} \int_0^D \frac{\Delta q Z_n^2(z) dz}{\rho(z)}$$

$$\Delta q = -2\Delta c(z) \frac{\omega^2}{c_0^3(z)}$$

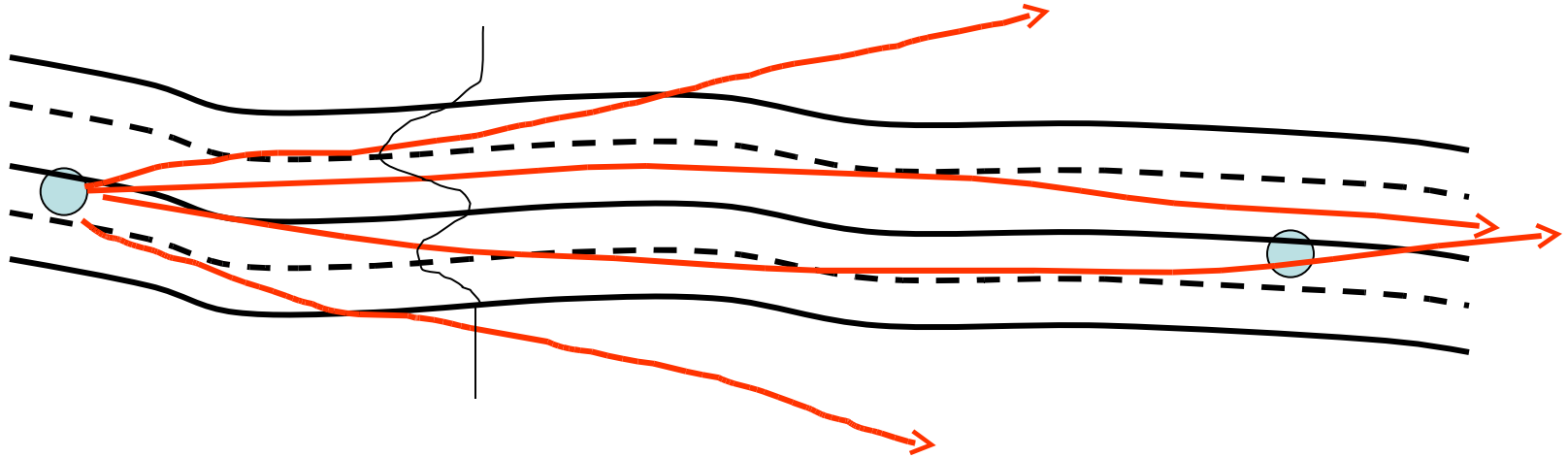
$$\Delta k_n = \frac{-(D, H) \Delta c \omega^2}{c_0^3}$$

- Simple model – rigid bottom background waveguide plus ML, IW perturbations
- The background eigenvalue plus the appropriate perturbation is what we want -> **eigenvalue at each point in (x,y)**
- The mode function vertical dependence put in via 2OPT. Shows why higher modes trap!!

See that energy will preferentially leak out the exterior and that apparent angle of source has IW curvature effects in it – can calculate with rays

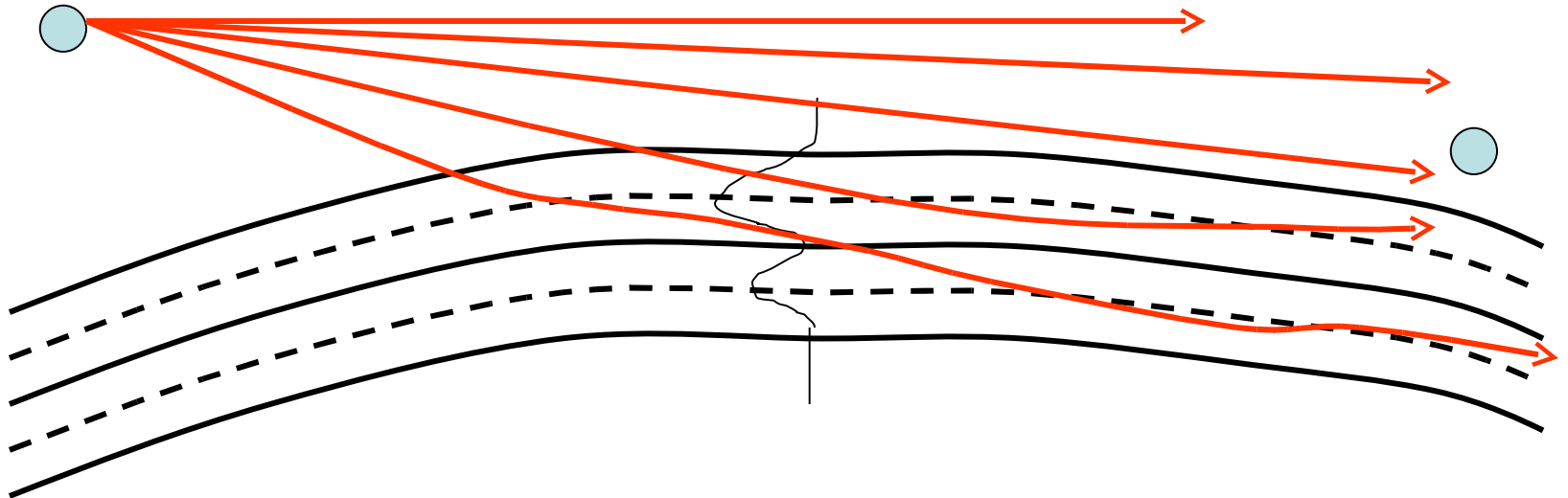


Mode Ducting... Critical angle most relevant



Mode Scattering... Fresnel scale R_F as well as critical angle

S – R Distance L ; Wavelength λ ; $R_F = (\lambda L)^{1/2}$

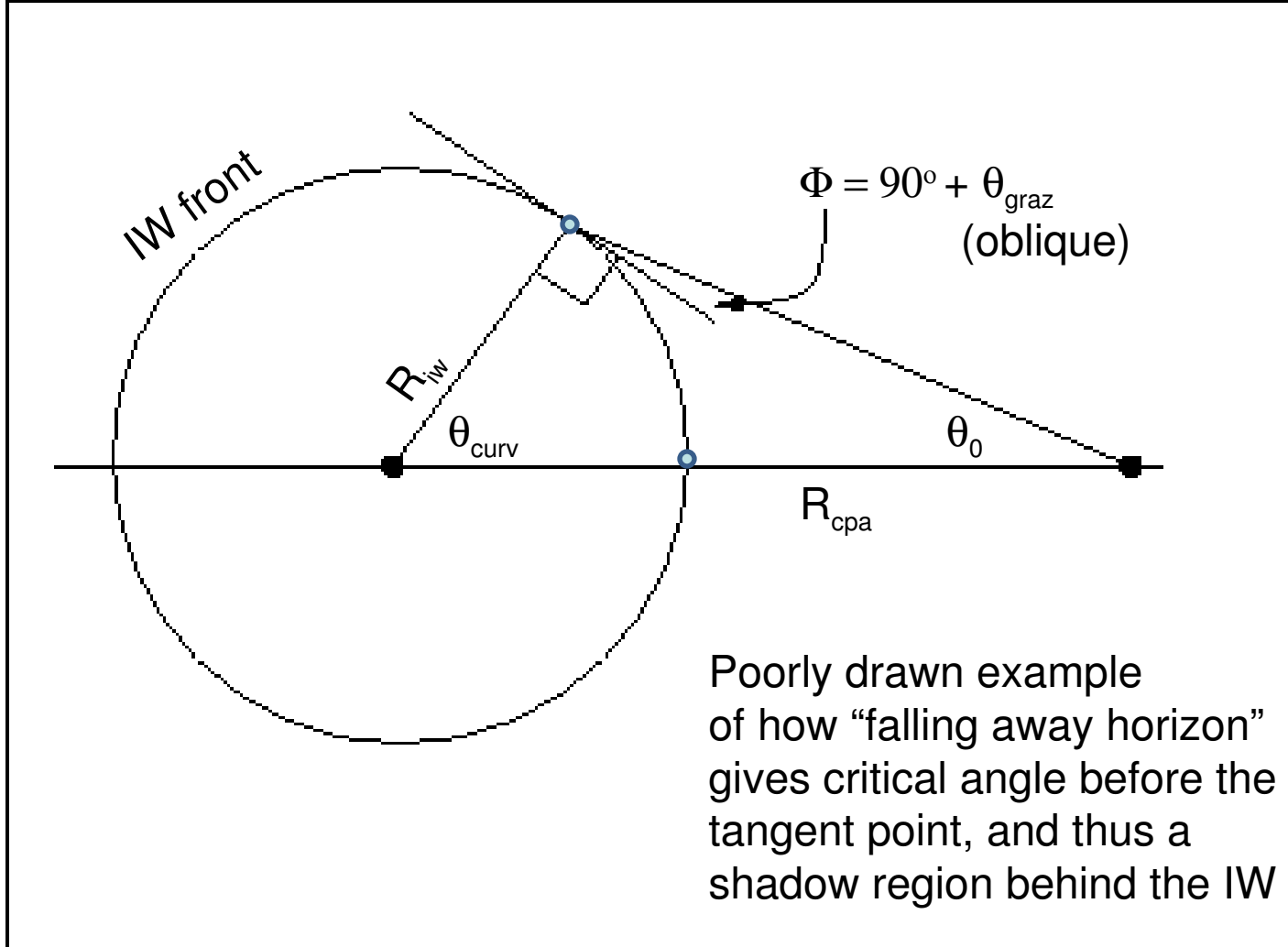


Approx Fresnel Scales (m)

<i>L</i>	Freq	100	200	300	400	500	600 Hz
<i>5 km</i>		273	194	158	137	122	112
<i>15 km</i>		474	335	274	237	212	194
<i>25 km</i>		612	433	354	306	274	250

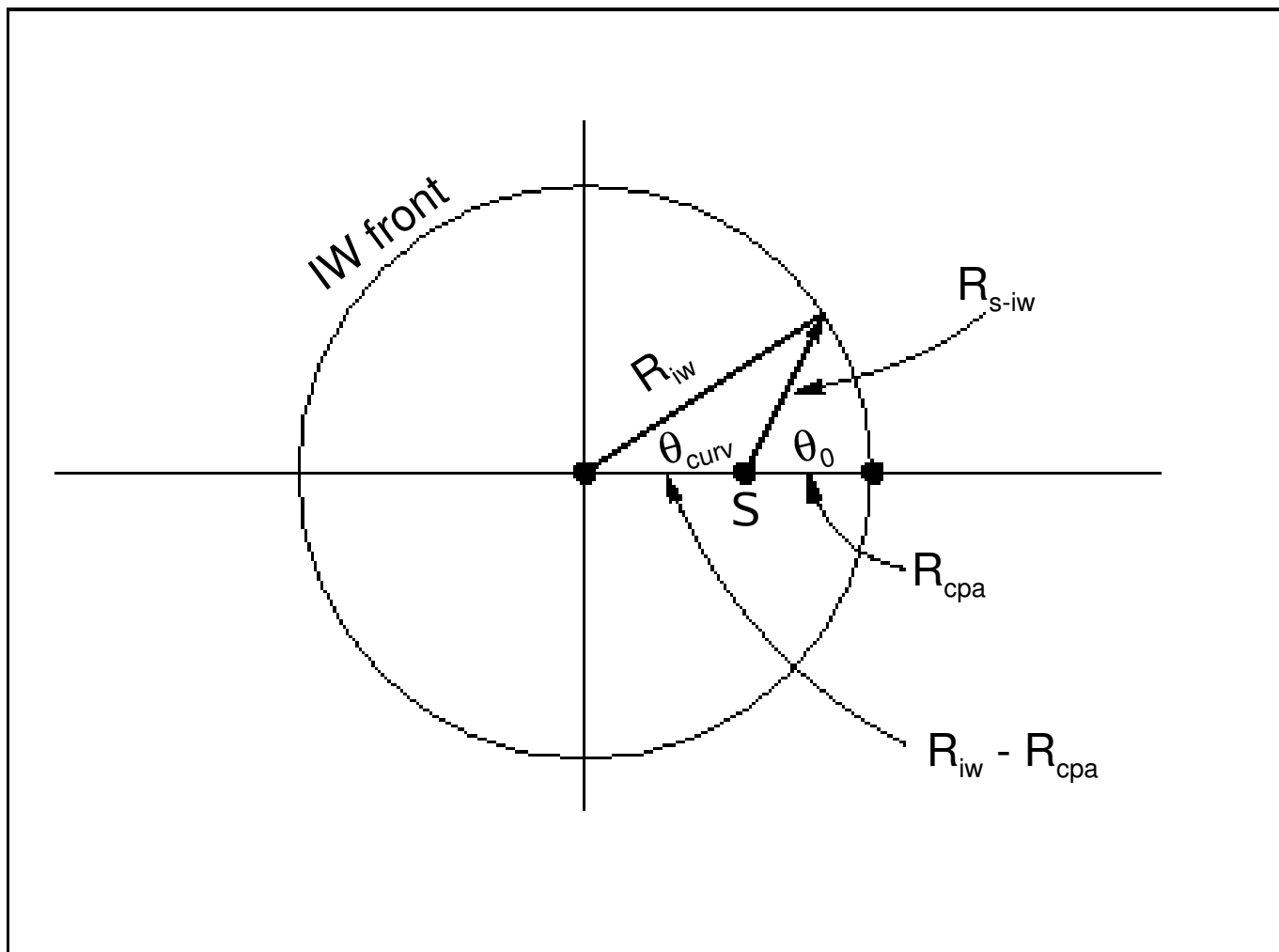
Shadowing

- IW has critical angle of ~ 5 degrees (max)
- Can give an x-y plane shadow behind a linear IW, but only if source is within 1-2 km of IW front
- Curved IW's allow one to see shadowing effect for source considerably further away
- Might be an observable effect in data..???



Anti-Shadowing

- Having source on interior of IW curves produces an opposite effect – makes shadowing unlikely
- Horizon curves toward the rays, making effective angle larger



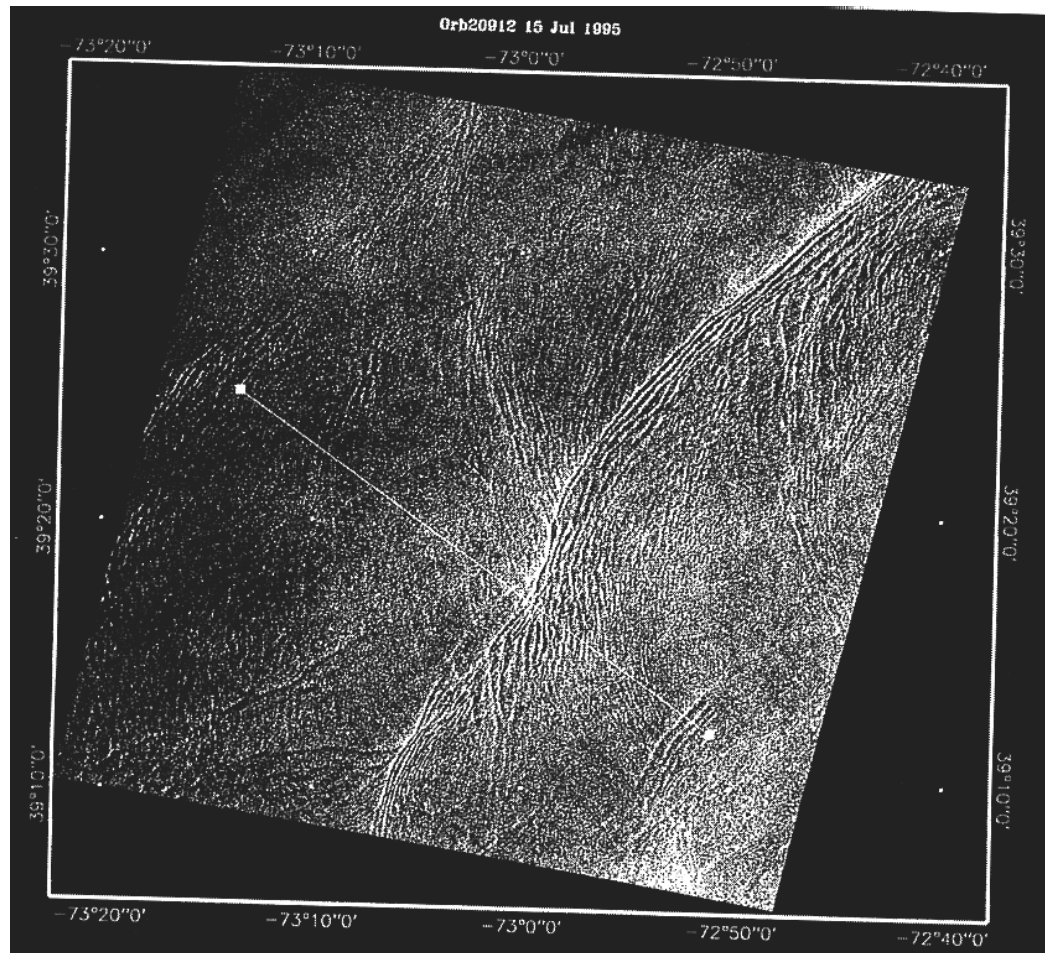
Where are we now?

- Have analytical forms for the eigenvalues, the ray paths for the geometries considered, where shadow zones are, etc.
- Are doing some examples to compare to detailed numerical models (i.e. see if we can simply explain some features in models)
- Want to [look at data](#) to see if we have some situations where the shadowing and dispersive light piping/leakage effects might be seen.
Curvature of IW's in 3-D thermistor string array region and thus near WHOI VLA looks attractive!

Some new work – if time !!

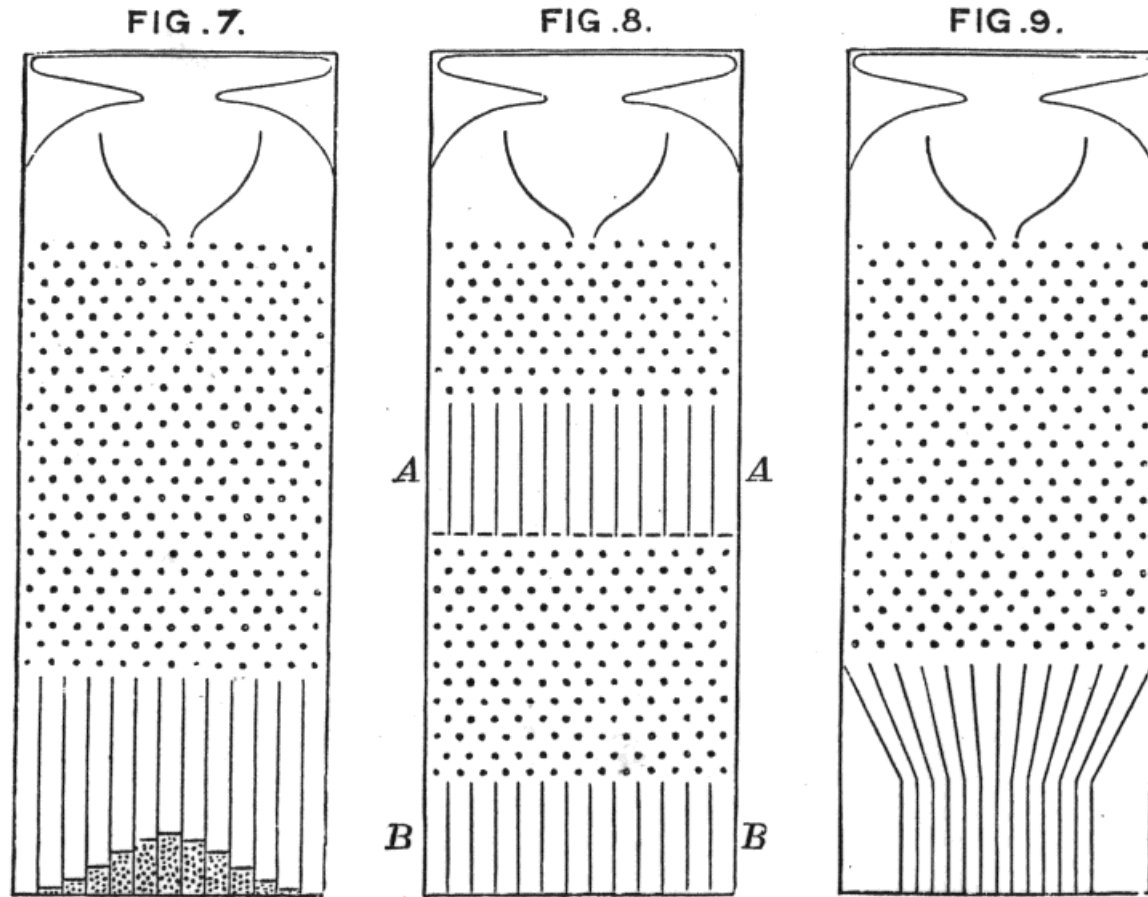
By same gang of thieves...

Now note horizontal
decorrelation/termination of waves

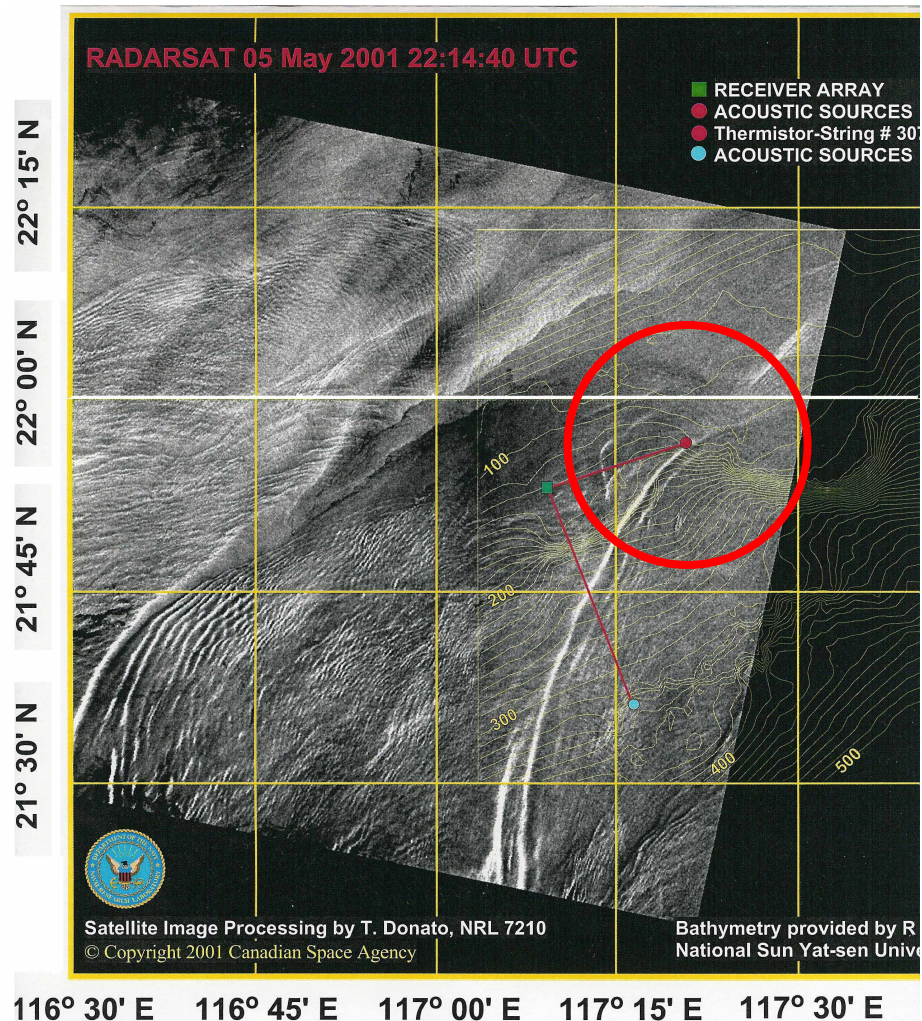


Horizontal dispersion – Galtons Box in the Ocean

Binomial-> Gaussian

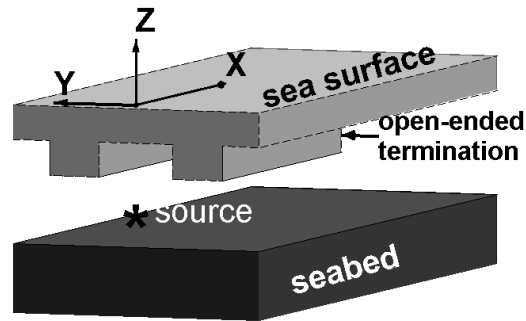


Physics of terminating duct (Lin)

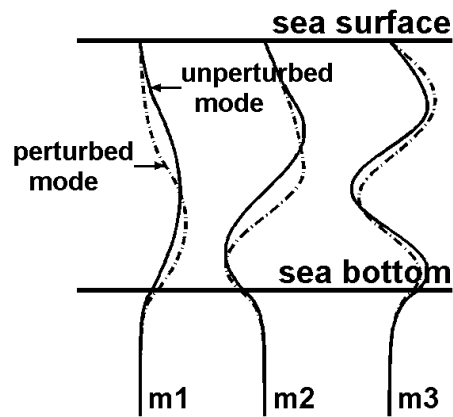


Lin's open ended duct work continued (Galton's box input gets more complicated!!)

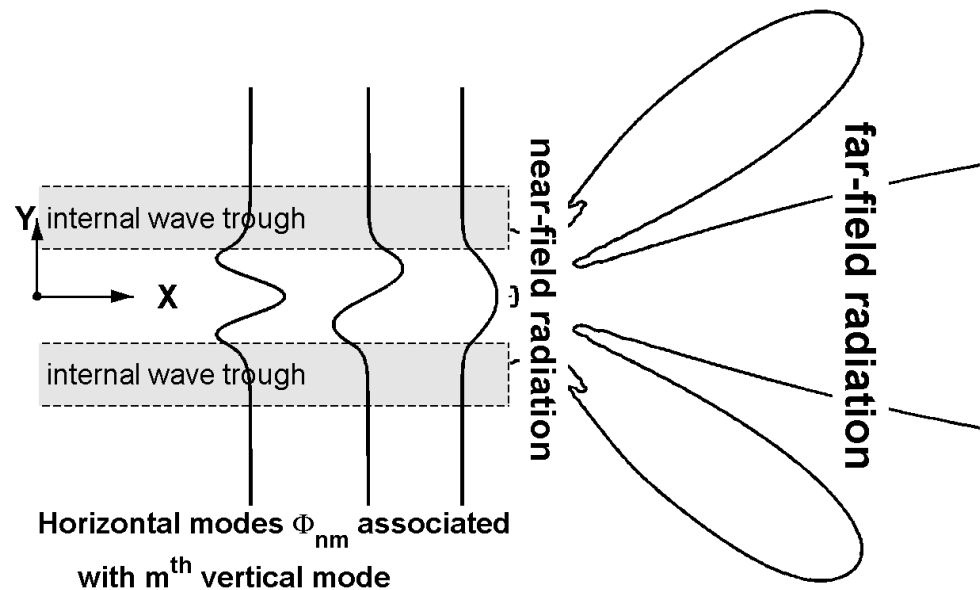
(a) Internal square wave model



(b) Vertical mode comparisons



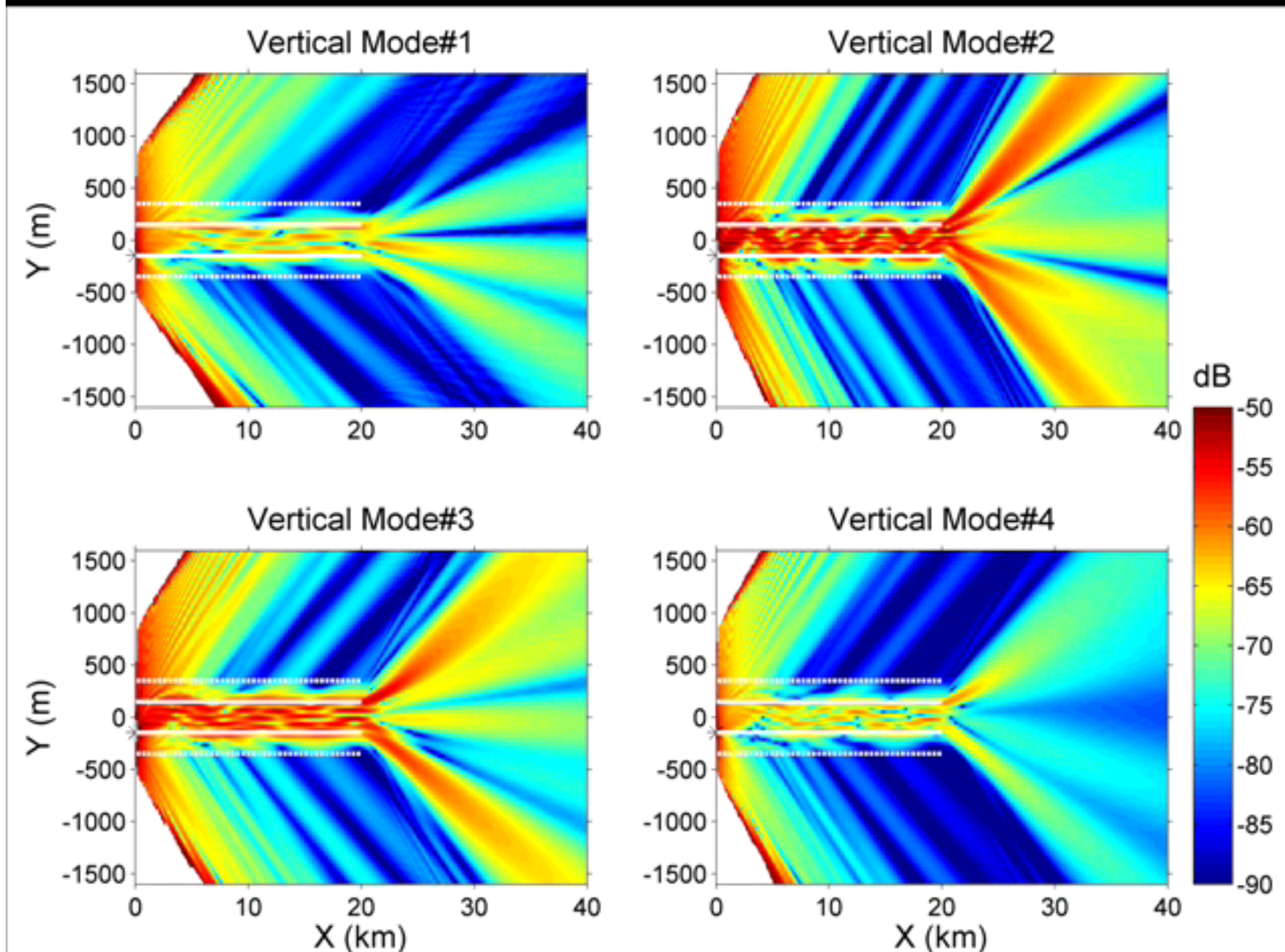
Radiation beam pattern of a vertical propagating mode
(Total radiation field = sum of all vertical mode radiations)



(c) Sound radiation from the termination

Radiation Beam Pattern

decomposed to individual vertical modes



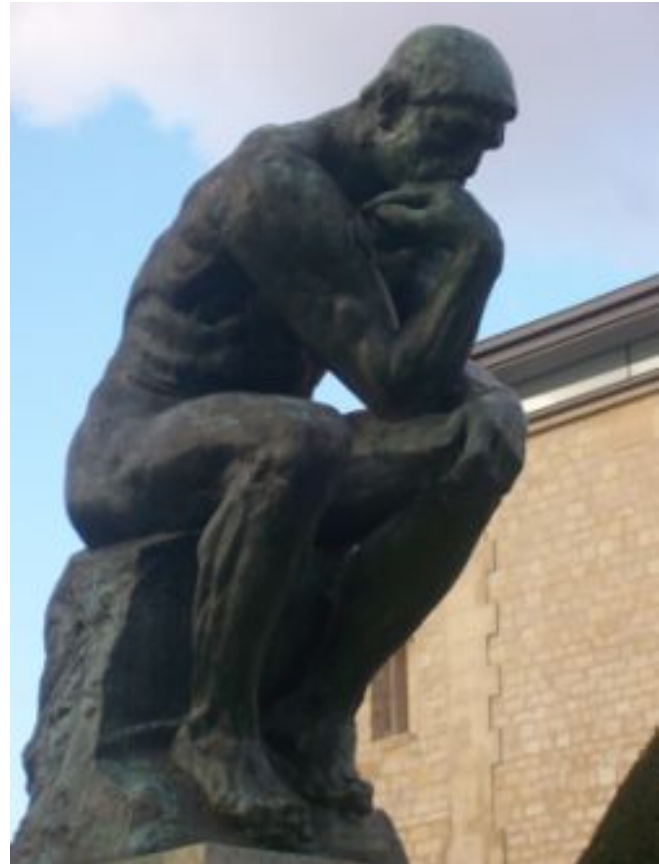
Other pieces of the menagerie to add

- Crossing internal waves (Reilly-Raska)
- Horizontal Lloyds mirror (Reilly-Raska)
- Mid-frequency (Katznelson)
- ???



Quo Vadis ?

- What does one see with *all* of this stuff present? (for sure it's **Funky !**)
- Are there distinct signals/signatures from each “process” we’ve examined, [time, angle, frequency, intensity,..] or do they produce similar, “additive” effects?
- How to describe this mess - with random medium approach...?!?
- What does this mean for naval and other ocean acoustics applications?



Questions??

